Session

REINVENTING THE TEACHING OF STATICS

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Introduction

Learning in the subject of Engineering Statics deserves significant attention. First, Statics lays the foundation for subsequent courses, namely Dynamics and Strength of Materials, both of which rely heavily on free body diagrams and on recognizing the combined effect of forces. While there are new ideas which are emphasized in engineering dynamics, instructors in this subject inevitably find that some of students' difficulties are rooted in ideas from Statics, such free body diagrams and working with forces. One of the most fundamental concepts in strength of materials is that of internal loads and its relation to external loads. This idea is wholly within the domain of Statics, yet a concept inventory for mechanics of materials currently under development rightfully points to this as one of its core concepts¹. Second, Statics, together with these courses, forms the basis for much engineering design and practice. Again, instructors in engineering design² lament the difficulties students have in using Statics for the purpose of their course. In sum, all is not well with instruction in Statics.

It appears that the ideas of Statics, if learned at all, are often not learned in ways that would enable their extension beyond the course. Many Statics problems are, at least superficially, set in a context of engineering applications and hardware, as evidenced by the problems in many Statics textbooks. Nevertheless, students tend to be largely focused on arriving at a mathematical solution, with little attention paid to how the solution is related to the physical context of the problem. Perhaps this is not surprising given strong emphasis on mathematical manipulation evident in the early chapters of most Statics textbooks. One instance where the practicalities of the actual engineering hardware beg to be considered is that of the mutual forces exerted by bodies connected in various ways. Yet, even here, textbooks largely reduce the treatment to a set of tables which students have no recourse but to memorize.

General Approaches to Improving Learning Which are Relevant to Statics

To improve the situation, instructors of Statics must gather all the tools at their disposal. Several generally accepted approaches to improving learning outcomes are potentially quite relevant to Statics. Students, who are actively engaged in learning, learn more. While it can be more time consuming, ideas that are reached through discovery may be more firmly grasped than those that are acquired through typical lecture or textbook. Students learn through a constant iterative process of assimilating new information and testing out their evolving understanding with feedback from instructors; thus the integration of assessment into the learning process can be of great benefit. This process is aided when new information is placed in the context of knowledge which students have previously acquired; that is, students build on they already know. Students can learn a great deal from one another; collaboration, if harnessed appropriately, is a powerful tool in learning. Finally, for many subjects in the sciences or technologies, physical referents or manipulatives can serve to enhance learning. Instructional methods which draw together many of these techniques have recently been introduced in Statics³.

Implications of Conceptual Difficulties Associated with Statics

While the techniques alluded to above can be valuable, how should Statics instruction reflect the conceptual difficulties which are peculiar to Statics? Statics instruction faces the following dilemma. There are a significant number of concepts, which go beyond those addressed in freshman physics, which students must learn and use, in combinations, to solve Statics problems. Moreover, these concepts must be learned in a deep way in the sense of relating the relevant symbols and theory to what they physically represent⁴. Yet, it is known from research into physics education⁵⁻⁷ that students doubt the existence of forces between unmoving, relatively rigid, inanimate objects. How is one to engage students in learning the concepts of Statics when its core element – the forces between parts of machines and structures – are not viewed as real by significant numbers of students?

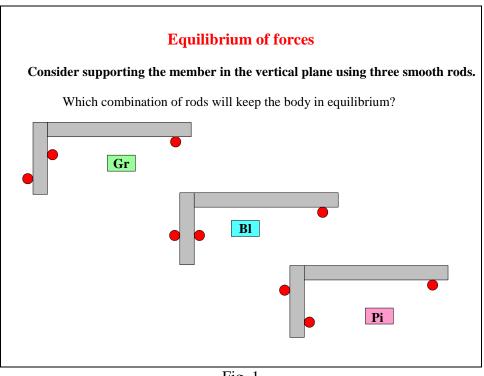
To overcome this dilemma, we have completely reframed our instruction in Statics. The fundamental elements in our instructional approach are: (i) to teach the concepts first entirely in the context of situations in which the forces are indeed real to students, namely ones they can experience by the senses of touch and sight (by sensing deformation or motion); and (ii) to decouple concepts from each other and treat them sequentially, with new concepts building on those which have already been covered.

Thus, we address all the basic concepts of statics (forces, moments, couples, static equivalency, free body diagrams, equilibrium in 2-D and 3-d, friction) in sequence, without recourse to forces between inanimate objects: students feel all the forces. Some elements of this sequence were presented previously⁸⁻⁹. Only after that are students gradually introduced to contacts between inanimate objects; each time, the student first exerts the force by hand, prior to witnessing its application by another object.) As explained below, this gradual transition from manually exerted forces to contact between inanimate objects prepares students for a far sounder understanding of the loads acting at connections between bodies.

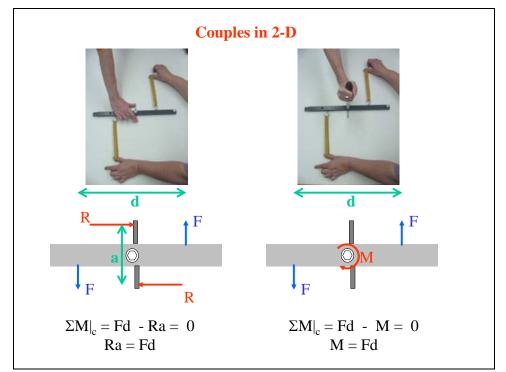
Sequence of Concepts

As point out, we have reformulated the concepts of Statics so as to build sequentially on one other. Although, our lecture-by-lecture schedule involves a fine-grained breakdown of concepts, and includes a series of modules to be used in the classroom, for the purposes of this paper we present a higher-level view of the development of concepts. We explain these steps in a concrete way by showing excerpts of PowerPoint presentations through which we address these concepts in the classroom. More about the classroom implementation is given below. While we focus here on *Statics* concepts, it must also be pointed out that the requisite mathematical skills, such as vector algebra, need to be developed as appropriate if the desired level of problem solving ability is to be attained.

1. Equilibrium of bodies requires consideration of both the translational and rotational effects of forces; that is, that the forces and moments must balance. We consider simple situations (Figure 1), some based on an L-shaped object used extensively in class, in which a set of forces maintains the body in equilibrium



- Fig. 1
- 2. Statics involves combinations of forces; one combination of forces can have the equivalent effect as many other combinations. In particular, we focus on combinations of forces which have a tendency only to rotate a body, and the representation of this combination as a couple (Figure 2a). Supporting an elongated object at one end can be seen to occur in many ways (Figure 2b), all of which are declared to be statically equivalent. These concepts are pursued first in 2-D situations, and later in 3-D. For example (Figure 2c), loads are also observed to be statically equivalent by virtue of the deformations they cause. Once students can use both



forces and couples, they consider equilibrium of objects acted upon by such combinations (Figure 2d).

Fig. 2a

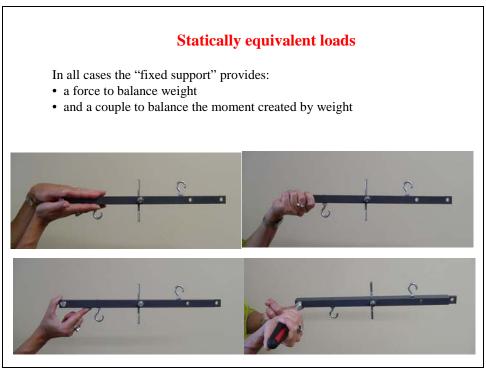


Fig. 2b

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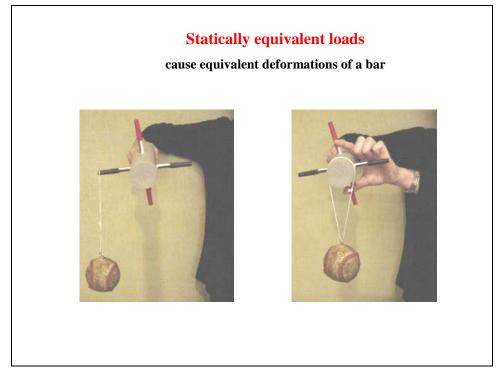
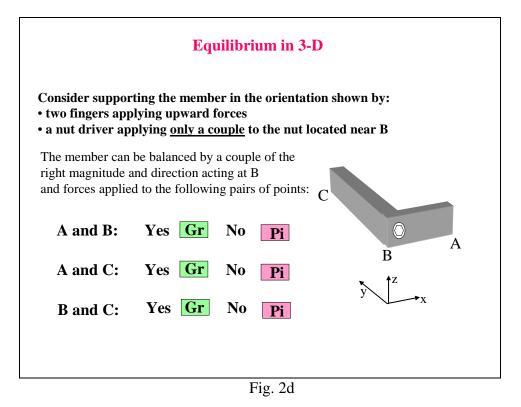


Fig. 2c



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3. To this point, we have focused on situations in which the frictional forces are low. Next, we consider the distinction between forces acting tangential to surfaces (friction) and normal forces. Concepts involving friction are conveyed again using simple objects that can be balanced by forces or couples applied by the hands. One idea is that frictional forces attempt to resist motion and in some instances can maintain a body in equilibrium; the distinction between the frictional force and the *upper limit* on the frictional force (μ N) is emphasized (Figure 3a). Also important is the idea that combinations of friction forces can provide couples (Figures 3b and 3c). We view it is critical to set the stage for connections between parts, which we treat later. There we simplify the possible loads at a connection (say no couple at an ideal pin joint). Only if students have had experience observing what friction.

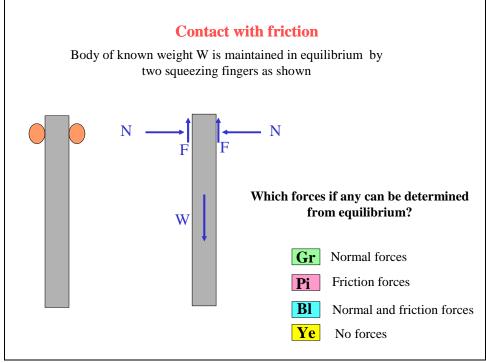


Fig. 3a

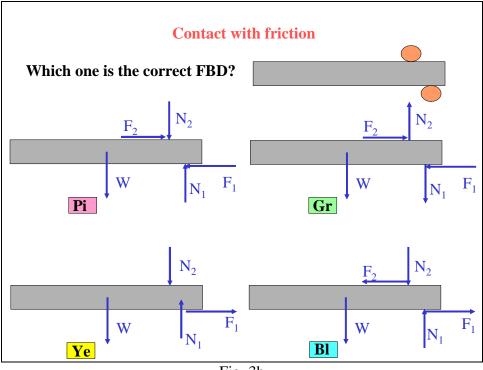
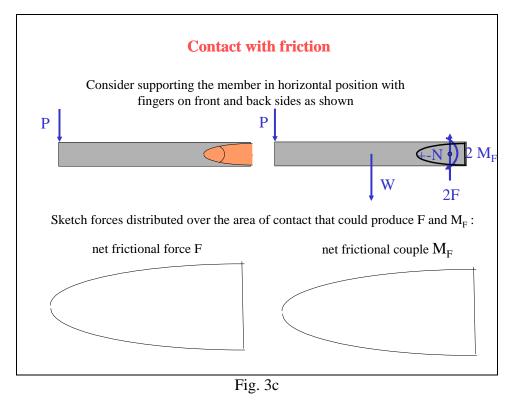
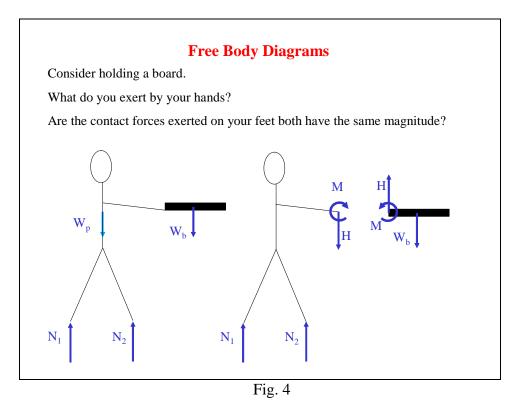


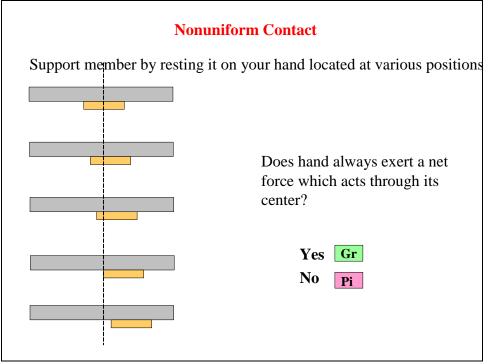
Fig. 3b



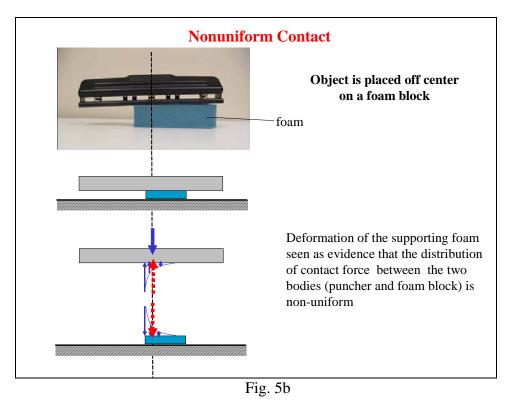
4. Fewer concepts are more pivotal to Statics, and the basis for more errors, than the ideas that every force acts between two bodies (usually in contact), and that a body must be chosen before equations of equilibrium can be derived (equilibrium always pertains to a body). Again, with recourse only to forces that can be *felt*, we have students gain experience in dismembering systems, associating with each force the two acting bodies, and considering equilibrium for various subsets of the system. One example of this is shown in Figure 4, in which a human body which supports the object; these can be considered as single body, or can be separated, when imposing equilibrium.



5. When bodies contact one another over an extended surface (rather than at a point), their interaction, can be viewed as a distribution of force. The differing intensities when the same load is acting over different areas can be readily felt by students (e.g., by contrasting the feel of supporting a package either by grasping a wide or narrow strap). Students can also observe how a distribution of contacting force can be uniform or non-uniform, both through supporting a board at different locations by hand (Figure 5a) and through observing deformation of the supporting foam (Figure 5b).



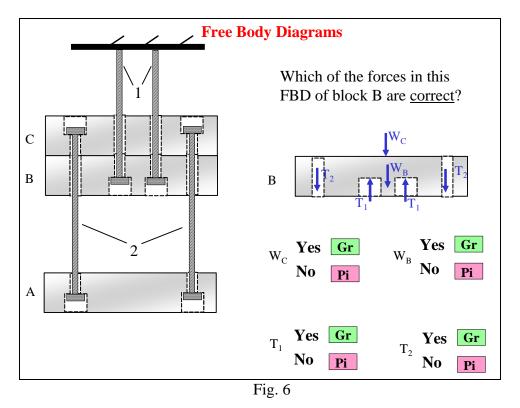




Following the above, our sequence turns to consider interactions between inanimate objects.

6. Equilibrium of contacting bodies for which the position and direction of the net forces are obvious.

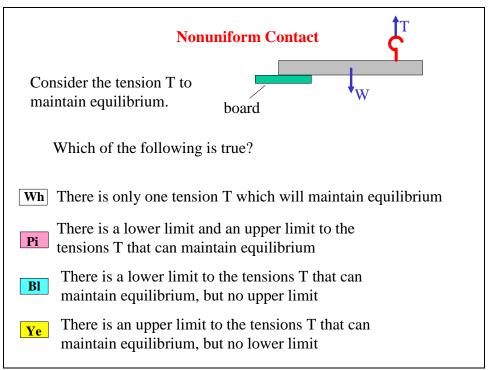
Here students are first solving problems that require separation of contacting *inanimate* bodies (Figure 6). Like in Step 4 above, students must learn to exercise due care in attributing each force to specific pair of bodies and in clearly identifying the body upon which equilibrium is imposed. This exercise also attempts to dispel the common notion of students that the normal force is equal to the weight, rather than merely equaling whatever is necessary to maintain equilibrium.



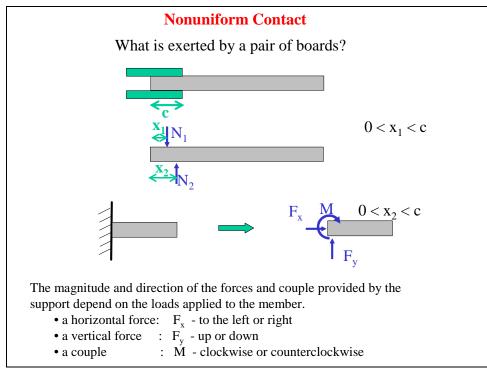
7. Normal contact between bodies, with distributed forces having a net force not acting at the center of contact.

Students can now draw together the ideas of Step 5 regarding possible nonuniformity of force distribution with Step 6 regarding separating bodies in various ways to quantify the forces between them. As seen in Figure 7a students learn to use the conditions of equilibrium to infer the *position* of the net load of contact. This reinforces the important idea that the normal force does not necessarily act at the center of the contact area.

Gripping a body firmly against translation and rotation by a pair of bodies (providing a fixed or cantilevered support, (as seen in Figure 7b) can now be understood: it combines the idea that the net force due to a distribution can act anywhere along the contact length, with the idea that a pair of oppositely directed forces can provide a balancing couple.









8. Forces exerted by bodies connected by typical joints, with greatest emphasis on pin joints. Much of the conceptual understanding developed above sets the stage for this significant topic. First, we address the very purpose of a joint – to allow for some motions, usually with minimal frictional resistance, and to prevent other motions (Figure 8a). Then, we recognize that this joint is based on contact between a rod and a sleeve. Moreover, through the experience of manually gripping a rod and with previous work on distributed forces and frictional forces, it can be seen that certain loads are only transmitted through friction, whereas others can occur through normal forces (Figure 8b). Next, the loads generated when a single sleeve supports a rod is contrasted with the support provided by a pair of sleeves (Figure 8c). This development paves the way for understanding why symmetric pin joints are preferable, and under what circumstances it is acceptable to model the load at a pin joint with a single transverse force and neglect the transverse couples (Figure 8d). With this approach the stage is set for comprehending how other joints are modeled, based on the shape of the contacting surfaces controlling the motions of the connecting bodies, and on distinguishing between effects of frictional and normal forces. Additionally, this approach can make students more aware of distinctions between circumstances in which slip is to be prevented versus promoted, and of design considerations seeking to minimize forces.

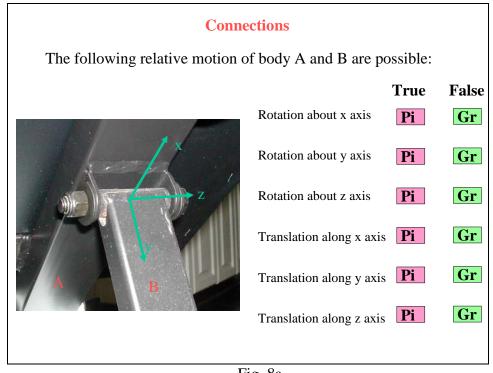
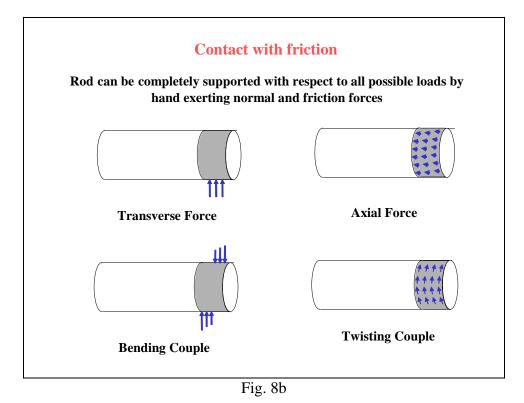
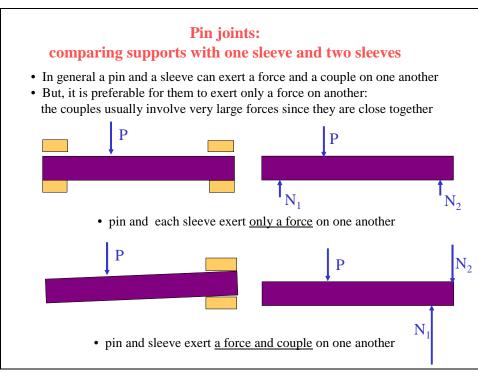


Fig. 8a







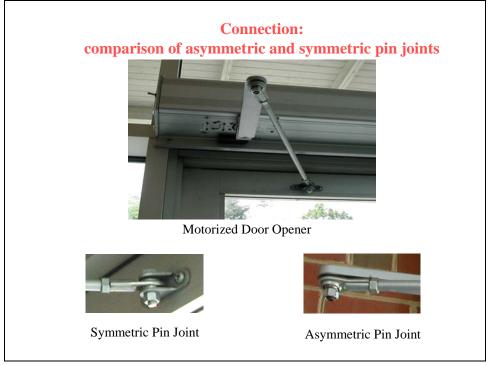


Fig. 8d

Implementation

The succession of concepts just described can be addressed through a combination of activities. In the classroom, we use so-called Learning Modules, which include classroom desktop experiments or demonstrations (featuring the objects shown above), PowerPoint Presentations and, often, Concept Questions. Students manipulate the objects, maintaining them in equilibrium, or creating their motion or deformation, in pursuit of various goals. The instructor controls the PowerPoint Presentations which guide students through the ideas that can be gleaned from manipulating the objects. These presentations typically contain Concept Questions (CQ's), akin to Mazur's ConcepTests¹⁰: multiple-choice questions that assess student understanding of concepts, and which usually require little or no analysis. Students vote for the different answers, and, depending on the response, they are encouraged to discuss the question further with peers and to manipulate the object. More details on classroom implementation can be found in other papers by the authors ^{3,9}.

Summary

While many active engagement classroom techniques are available to the instructor, it is up to the instructor to fill in the content which is the substance of these techniques. Moreover, since students learn based on what they know, this substance should be organized in a way that allows knowledge to be built steadily. We have undertaken this reorganization of the conceptual content of Engineering Statics. This reorganization must reflect the significant misconception on the part of many students that rigid, unmoving, inanimate objects do not exert forces. With this in mind, we have rebuilt our instructional approach to Statics by addressing all important concepts sequentially, but, notably, in the context of situations where all relevant forces can be

perceived through the senses of touch and sight. Thereafter, we gradually transition students to address the situations of traditional interest in Statics, where forces are exerted by inanimate parts of machines and structures. The sequence of concepts is addressed in class through the use of learning modules, which involve collaboratively manipulating objects, and responding to conceptual questions.

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