

# High thermal conductivity in soft elastomers with elongated liquid metal inclusions

Michael D. Bartlett<sup>a,1,2</sup>, Navid Kazem<sup>b,1</sup>, Matthew J. Powell-Palm<sup>a,1</sup>, Xiaonan Huang<sup>a</sup>, Wenhuan Sun<sup>a</sup>, Jonathan A. Malen<sup>a,c</sup>, and Carmel Majidi<sup>a,b,d,3</sup>

<sup>a</sup>Department of Mechanical Engineering, Carnegie Mellon University, Pittsburgh, PA 15213; <sup>b</sup>Department of Civil and Environmental Engineering, Carnegie Mellon University, Pittsburgh, PA 15213; <sup>c</sup>Department of Materials Science & Engineering, Carnegie Mellon University, Pittsburgh, PA 15213; and <sup>d</sup>Robotics Institute, Carnegie Mellon University, Pittsburgh, PA 15213

Edited by John A. Rogers, University of Illinois, Urbana, IL, and approved January 13, 2017 (received for review October 1, 2016)

**Soft dielectric materials typically exhibit poor heat transfer properties due to the dynamics of phonon transport, which constrain thermal conductivity ( $k$ ) to decrease monotonically with decreasing elastic modulus ( $E$ ). This thermal–mechanical trade-off is limiting for wearable computing, soft robotics, and other emerging applications that require materials with both high thermal conductivity and low mechanical stiffness. Here, we overcome this constraint with an electrically insulating composite that exhibits an unprecedented combination of metal-like thermal conductivity, an elastic compliance similar to soft biological tissue (Young’s modulus < 100 kPa), and the capability to undergo extreme deformations (>600% strain). By incorporating liquid metal (LM) microdroplets into a soft elastomer, we achieve a  $\sim 25\times$  increase in thermal conductivity ( $4.7 \pm 0.2 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$ ) over the base polymer ( $0.20 \pm 0.01 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$ ) under stress-free conditions and a  $\sim 50\times$  increase ( $9.8 \pm 0.8 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$ ) when strained. This exceptional combination of thermal and mechanical properties is enabled by a unique thermal–mechanical coupling that exploits the deformability of the LM inclusions to create thermally conductive pathways in situ. Moreover, these materials offer possibilities for passive heat exchange in stretchable electronics and bioinspired robotics, which we demonstrate through the rapid heat dissipation of an elastomer-mounted extreme high-power LED lamp and a swimming soft robot.**

liquid metal | thermal conductivity | soft materials | soft robotics | stretchable electronics

**M**aterials with high thermal conductivity are typically rigid and elastically incompatible with soft and mechanically deformable systems (1–6). In the general case of nonmetallic and electrically insulating solids, this limitation arises from kinetic theory and the Newton–Laplace equation, which imply that thermal conductivity ( $k$ ) will increase with a material’s elastic modulus ( $E$ ) according to the approximation  $k \approx (E/\rho)^{1/2}(C_V\ell/3)$ , where  $C_V$  is the volumetric heat capacity,  $\ell$  is the average mean free path of phonons, and  $\rho$  is the density (7, 8). For polymers like polyethylene, thermal conductivity can be enhanced through macromolecular chain alignment (from  $k \approx 0.3 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$  to  $100 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$ ), but this also leads to a dramatic increase in elastic modulus from  $\sim 1 \text{ GPa}$  to  $200 \text{ GPa}$  (9). Likewise, glassy polymer blends have been engineered to increase thermal conductivity through interchain hydrogen bonding (1), and relatively higher thermal conductivity has been observed in amorphous polythiophene ( $k \approx 4.4 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$ ) (2), but the high elastic modulus ( $E \approx 3 \text{ GPa}$ ) and low strain at failure (<5% strain) of films make them unsuitable for soft functional materials (3).

To overcome this fundamental tradeoff with thermal transport in soft materials, attempts have been made to engineer composites with various fillers (10), including metals (11, 12), ceramics (13), carbon fibers (14), and nanomaterials such as carbon nanotubes and graphene (4, 15, 16). Anisotropic thermal conductivity can arise in composite systems by using 1D fillers such as carbon fibers where thermal transport preferentially occurs along the major dimension of the filler (14). Thermal anisotropy can also be induced in polymeric materials during drawing processes that increase chain alignment

(17). Although these composites exhibit increased thermal conductivity, they typically use rigid fillers that result in mechanically stiff materials that cannot support stretchable functionality (4–6) and, in the case of carbon-based fillers, become electrically conductive even at low-volume loadings, which can interfere with functionality (18). To date, the combination of low elastic modulus on the order of biological tissue, large mechanical deformability, and high thermal conductivity remains elusive.

Here, we show that a soft-matter composite consisting of elongated liquid metal (LM) microdroplets dispersed in a highly deformable silicone elastomer (Fig. 1 *A–D*) exhibits an unprecedented combination of high thermal conductivity ( $4.7 \pm 0.2 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$  under stress-free conditions;  $9.8 \pm 0.8 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$  at 400% strain) with a low modulus ( $89 \pm 2 \text{ kPa}$  after 200% prestrain) and high strain limit (>600%). This approach overcomes the Newton–Laplace scaling because the inclusions have a thermal conductivity that is dominated by electrons, rather than phonons, and can deform with the surrounding matrix to support strain and thermal–mechanical coupling (*Electronic Contribution to Thermal Conductivity of EGaIn* and Fig. 1 *C* and *D*). Previously, we showed that LM-embedded elastomers can be engineered to exhibit dramatic enhancements in electrical permittivity (19) and conductivity (20) without sacrificing the elastic properties of the matrix elastomer. A subsequent effort by another group attempted to show enhanced thermal conductivity with a polydisperse suspensions of irregularly shaped LM inclusions (12). Although an enhanced thermal conductivity of  $2.2 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$

## Significance

**Efficient thermal transport is critical for applications ranging from electronics and energy to advanced manufacturing and transportation; it is essential in emerging domains like wearable computing and soft robotics, which require thermally conductive materials that are also soft and stretchable. However, heat transport within soft materials is limited by the dynamics of phonon transport, which results in a trade-off between thermal conductivity and compliance. We overcome this by engineering an elastomer composite embedded with elongated inclusions of liquid metal (LM) that function as thermally conductive pathways. These composites exhibit an extraordinary combination of low stiffness (<100 kPa), high strain limit (>600%), and metal-like thermal conductivity (up to  $9.8 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$ ) that far exceeds any other soft materials.**

Author contributions: M.D.B., N.K., M.J.P.P., X.H., W.S., J.A.M., and C.M. designed research; M.D.B., N.K., M.J.P.P., X.H., and W.S. performed research; M.D.B., N.K., M.J.P.P., X.H., J.A.M., and C.M. analyzed data; and M.D.B., N.K., M.J.P.P., J.A.M., and C.M. wrote the paper.

The authors declare no conflict of interest.

This article is a PNAS Direct Submission.

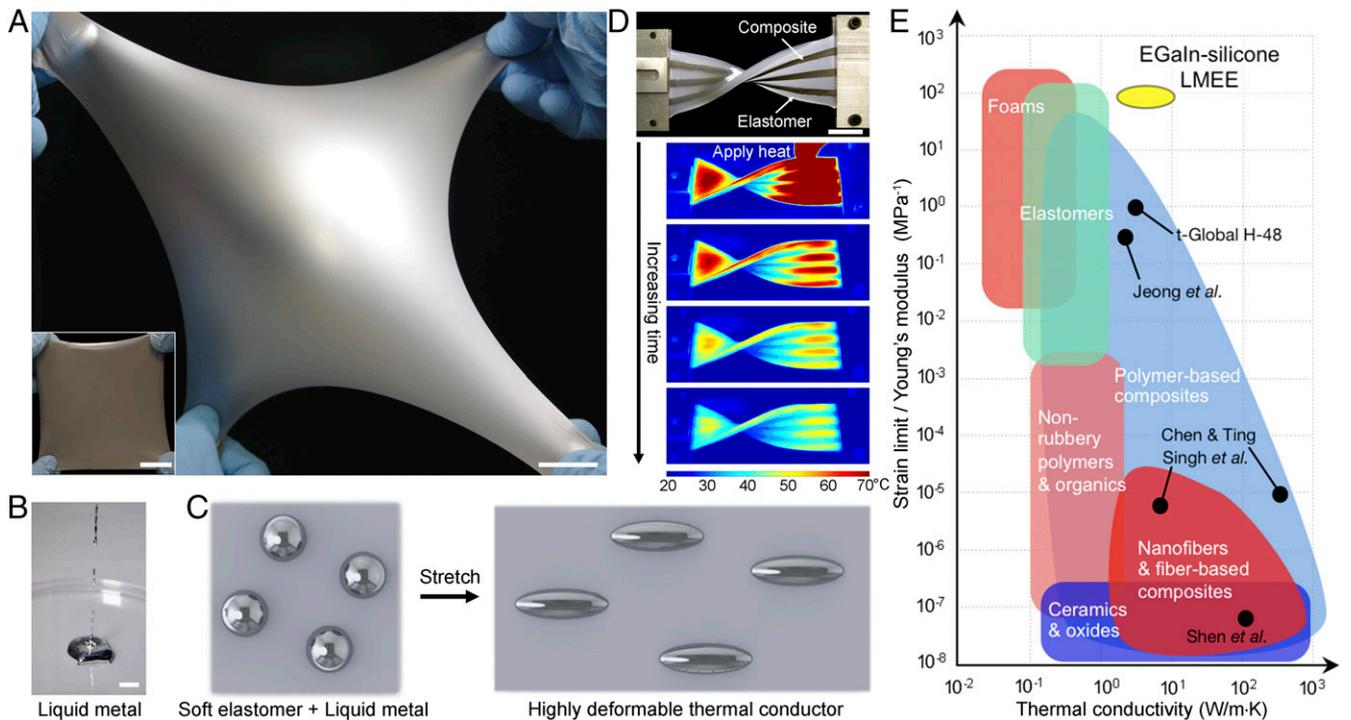
Freely available online through the PNAS open access option.

<sup>1</sup>M.D.B., N.K., and M.J.P.P. contributed equally to this work.

<sup>2</sup>Present address: Department of Materials Science & Engineering, Iowa State University, Ames, IA 50011.

<sup>3</sup>To whom correspondence should be addressed. Email: cmajidi@andrew.cmu.edu.

This article contains supporting information online at [www.pnas.org/lookup/suppl/doi:10.1073/pnas.1616377114/-DCSupplemental](http://www.pnas.org/lookup/suppl/doi:10.1073/pnas.1616377114/-DCSupplemental).



**Fig. 1.** Soft, thermally conductive composite. (A) Highly deformable LMEE. (scale bars, 25 mm.) (B) EGaIn alloy is liquid at room temperature and shows fluid characteristics as demonstrated by falling droplets. (Scale bar, 10 mm.) (C) Schematic illustration of the LMEE composite where LM microdroplets are dispersed in an elastomer matrix and, upon deformation, the LM inclusions and elastomer elongate in the direction of stretching. (D) Alternating strips of LMEE and unfilled elastomer are heated with a heat gun, and the IR photo time sequence shows the LMEE dissipating heat more rapidly than the elastomer (images correspond to  $t = 0, 5, 10,$  and  $15$  s after the heat source is removed). (Scale bar, 25 mm.) (E) The  $\phi = 50\%$  LMEE composites described here occupy a unique region of the material properties space when comparing thermal conductivity with the ratio of strain limit to Young's modulus. (Data points are from refs. 2, 9, 12, and 14.)

was measured at high LM volume fraction (66% by vol.; 92.5% by weight), these samples exhibited an increased stiffness (Young's modulus increased from 0.65 MPa to 3.3 MPa) and reduced stretchability (strain limit decreased from 150 to 50%), which limits the ability to elongate LM droplets in situ. Comparing previous results with the exceptional performance reported here (Fig. 1E) highlights the critical importance of LM microstructure (and not just material composition) in enabling elastomers to exhibit metal-like thermal conductivity without altering their natural elasticity.

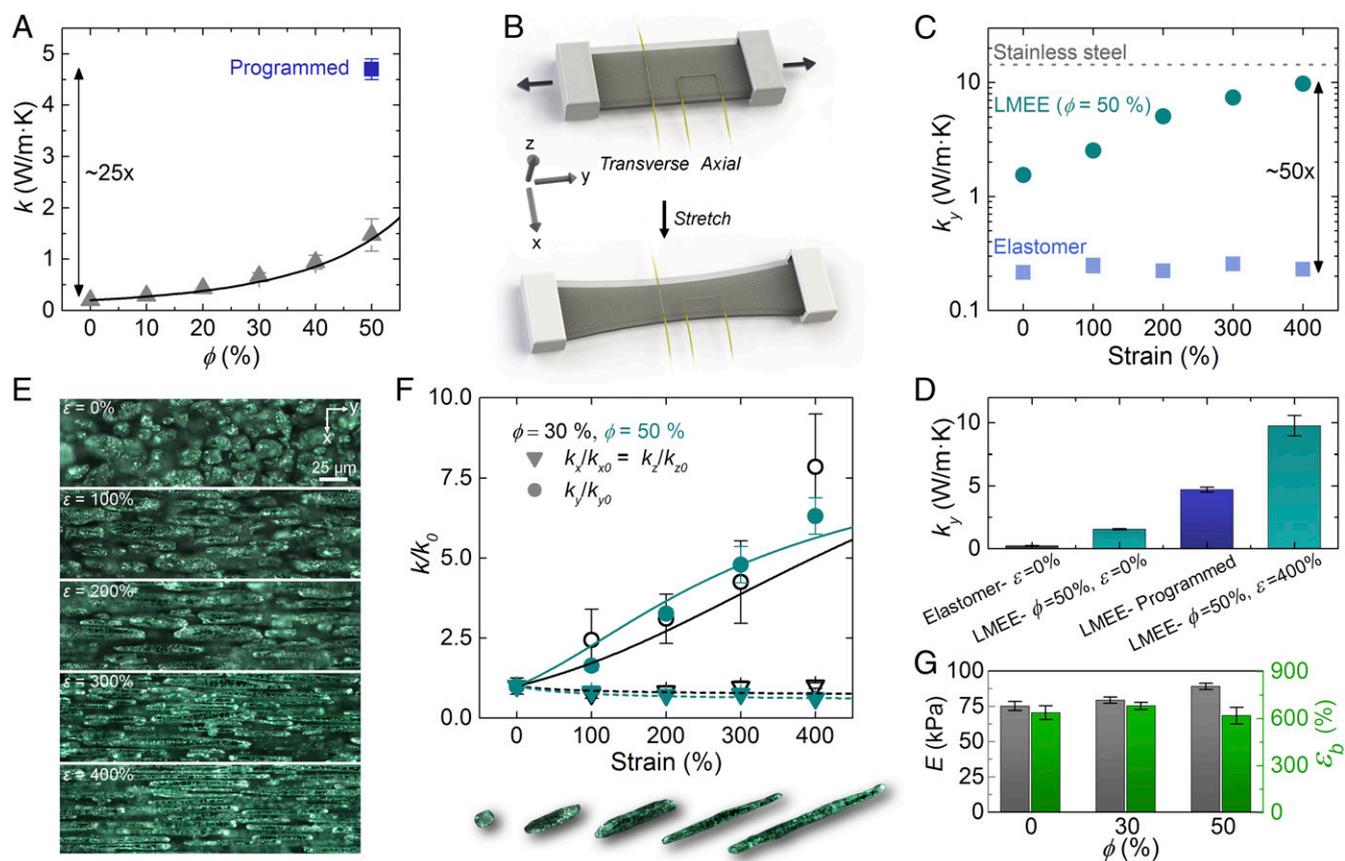
### Experimental Results

The LM embedded elastomer (LMEE) is composed of a Pt-catalyzed silicone elastomer embedded with a randomly distributed, polydisperse suspension of nontoxic (21), liquid-phase eutectic gallium–indium (EGaIn) microdroplets (19, 20, 22). As shown in Fig. 1D and Movie S1, stretched and twisted strips of LMEE exhibit rapid thermal dissipation compared with adjacent strips of unfilled elastomer subject to the same initial heating. Compared with previous attempts with LM-filled elastomers (12), we have discovered that strain creates thermally conductive pathways through the in situ elongation of the deformable liquid inclusions, which significantly enhances thermal conductivity in the stretching direction. For permanent (stress-free) and strain-controlled elongation of the LM inclusions, this enhanced  $k$  is nearly 25 $\times$  to 50 $\times$  greater than the unfilled elastomer ( $0.20 \pm 0.01 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$ ) and approaches the limit for the parallel rule of mixtures of an EGaIn–silicone composition (23) without the aid of percolating networks. Referring to Fig. 1E, the exceptional combination of high thermal conductivity, low elastic modulus, and high strain limit allows the LMEE composites to occupy an uncharted region of the material properties space.

The thermal composite is fabricated by shear mixing EGaIn alloy (75% Ga, 25% In, by weight; Gallium Source) with an uncured silicone elastomer (Ecoflex 00-30; Smooth-On) (see Methods for material fabrication). During mixing, the LM droplets form a

self-passivating  $\text{Ga}_2\text{O}_3$  coating that helps prevent coalescence and eliminates the need to add surfactants or other dispersing agents (24). The droplets have a statistically uniform spatial distribution and are polydisperse, with a median diameter of  $\sim 15 \mu\text{m}$  (19). Thermal conductivity is measured using the transient hotwire (THW) method in which an embedded wire simultaneously acts as a resistive heat source and thermometer that measures the change in temperature ( $\Delta T$ ) as a function of time ( $t$ ), which is related to thermal conductivity through the cylindrical heat diffusion equation (Methods and Fig. S1). Experimental measurements are presented in Fig. 2A and show that, as LM volume fraction ( $\phi$ ) increases, thermal conductivity increases (Fig. S2). These values are in good agreement with theoretical predictions obtained from the Bruggeman effective medium theory (EMT) formulation (25) for a uniform dispersion of spherical EGaIn inclusions [ $k = 26.4 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$  (23)] in a silicone matrix ( $k = 0.20 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$ ).

We further configure the THW method to enable directional measurements of thermal conductivity upon deformation by laminating LMEE strips around wires that are parallel (axial) and perpendicular (transverse) to stretch, as shown in Fig. 2B. Ellipsoidal heat spreading yields effective anisotropic thermal conductivities in the axial and transverse directions that can be transformed to measure the orthotropic ( $k_x, k_y, k_z$ ) bulk values (see EMT for derivation) (26, 27). This configuration enables examination of the thermal–mechanical coupling between thermal conductivity and deformation. We find that, upon stretching the unfilled ( $\phi = 0\%$ ) homogenous elastomer, the thermal conductivity in the direction of stretch ( $k_y, \approx 0.20 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$ ) remains largely unchanged (Fig. 2C). However, when stretching the  $\phi = 50\%$  LMEE, the thermal conductivity in the longitudinal direction ( $k_y$ ) dramatically increases and reaches a value of  $9.8 \pm 0.8 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$  at 400% strain (Figs. S3 and S4). This represents an increase of  $\sim 50\times$  relative to the unfilled material and a value that approaches



**Fig. 2.** Thermal–mechanical behavior of the LMEE composite. (A) Thermal conductivity versus LM volume fraction ( $\phi$ ) in the stress-free state. The programmed sample refers to a composite that has been stretched to 600% strain and then relaxed to an unloaded state. Here the symbols are the experimental measurements, and the solid curve represents the theoretical prediction from the Bruggeman EMT formulation ( $n = 100$  volume fraction dependence,  $n = 5$  programmed samples). (B) Schematic of the THW method to measure anisotropic thermal conductivity under deformation. (C) Plot of thermal conductivity in the stretch direction versus strain for the elastomer and the LMEE composites. Upon stretching, the LMEE approaches the thermal conductivity of stainless steel and is 50 $\times$  greater than the unfilled elastomer ( $n = 5$ ). (D) Thermal conductivity comparison for different LM volume fractions ( $\phi$ ) and stress states ( $n = 5$ ). (E) Optical micrographs of the 30% LMEE microstructure during stretching, with the images corresponding to 0 to 400% strain in 100% increments (from top to bottom). (F) Normalized thermal conductivity as a function of strain (blue open symbols are  $\phi = 30\%$ , and cyan closed symbols are  $\phi = 50\%$ ;  $n = 5$ ). The solid line represents the predicted behavior for the  $y$  direction, and the dashed line is the prediction for the  $x$  and  $z$  direction from our model. The images are representative images of the LM inclusions during the deformation process. (G) Mechanical properties of the LMEE composites with elastic modulus on the left axis and strain at break on the right axis ( $n = 3$ ). All error bars represent  $\pm 1$  SD.

the thermal conductivity of some metals like bismuth and stainless steel. These measurements, which were taken at room temperature, are in good agreement with tests performed on samples that were either cooled to 0 °C or heated to 60 °C (Fig. S5). In addition, the material is robust to cyclical loading, with only a slight increase in thermal conductivity measured after 1,000 cycles of 200% strain (Fig. S6). Furthermore, we can “program” the material to achieve permanently elongated LM inclusions in a stress-free state by stretching a virgin sample of LMEE to 600% strain and then unloading to zero stress. An unrecoverable plastic strain of 210% is induced, enabling elongated inclusions in an unloaded (stress-free) state (Methods and Fig. S7). As shown in Fig. 2A, thermal conductivity of the programmed LMEE sample in the longitudinal direction ( $k_y$ ) is  $4.7 \pm 0.2 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$ , which is  $\sim 25\times$  greater than that of the base elastomer (Fig. 2D). It is important to note that, when unstrained, both the  $\phi = 0$  and 50% samples exhibit values of  $k$  that are typically observed in other polymeric composites (12, 28).

Such an unprecedented enhancement in  $k$  arises from the discovery of a unique thermal–mechanical coupling in which the deformable LM inclusions elongate into needle-like microstructures along the prestrained or mechanically loaded direction to create enhanced thermally conductive pathways (Fig. 2E). This is further demonstrated in Fig. 2F, in which compositions with  $\phi = 30\%$  and 50% EGaIn (by volume) are subject to strains ranging from 0 to 400% in increments of 100% (Methods and

Figs. S3 and S4). As shown, the thermal conductivity in the  $y$  (stretching) direction increases by greater than a factor of 5 beyond 300% strain. To theoretically capture this behavior, we create an EMT model based on the Bruggeman formulation to explain the relative increase in directional thermal conductivity as a function of axial strain ( $\epsilon$ ) (see EMT for details). As seen in Fig. 2F, we find good agreement between the experimentally measured values (markers) and our theoretical predictions (curves), which capture the large increase in thermal conductivity in the stretching direction ( $k_y$ ) and the slight decrease in the orthogonal directions ( $k_x$ ,  $k_z$ ). The agreement with theory is achieved without data fitting and supports the claim that the observed anisotropic thermal–mechanical response is controlled by the directional change in aspect ratio of the LM inclusions (Fig. 1C). Lastly, for all volume fractions, the composite materials have an elastic modulus less than 90 kPa (Fig. S8) and can support uniaxial strains above 600%, properties that are similar to those of the homogeneous elastomer (Fig. 2G). The modest increase in elastic modulus ( $<20\%$ ) for the LMEE composites can be attributed to surface tension at the liquid–solid interface. For liquid inclusions in a compliant matrix, Style et al. (29) have previously shown that surface tension can induce mechanical resistance to droplet deformation and result in an overall stiffening of the composite. Together, these results show that the EGaIn droplets greatly enhance thermal conductivity of soft materials

without degrading their mechanical properties. Significantly, these materials display nearly an order of magnitude enhancement in thermal conductivity and strain at break while possessing an order of magnitude lower modulus than commonly available thermal tapes and previously studied LM-filled composites (12).

### Selected Applications

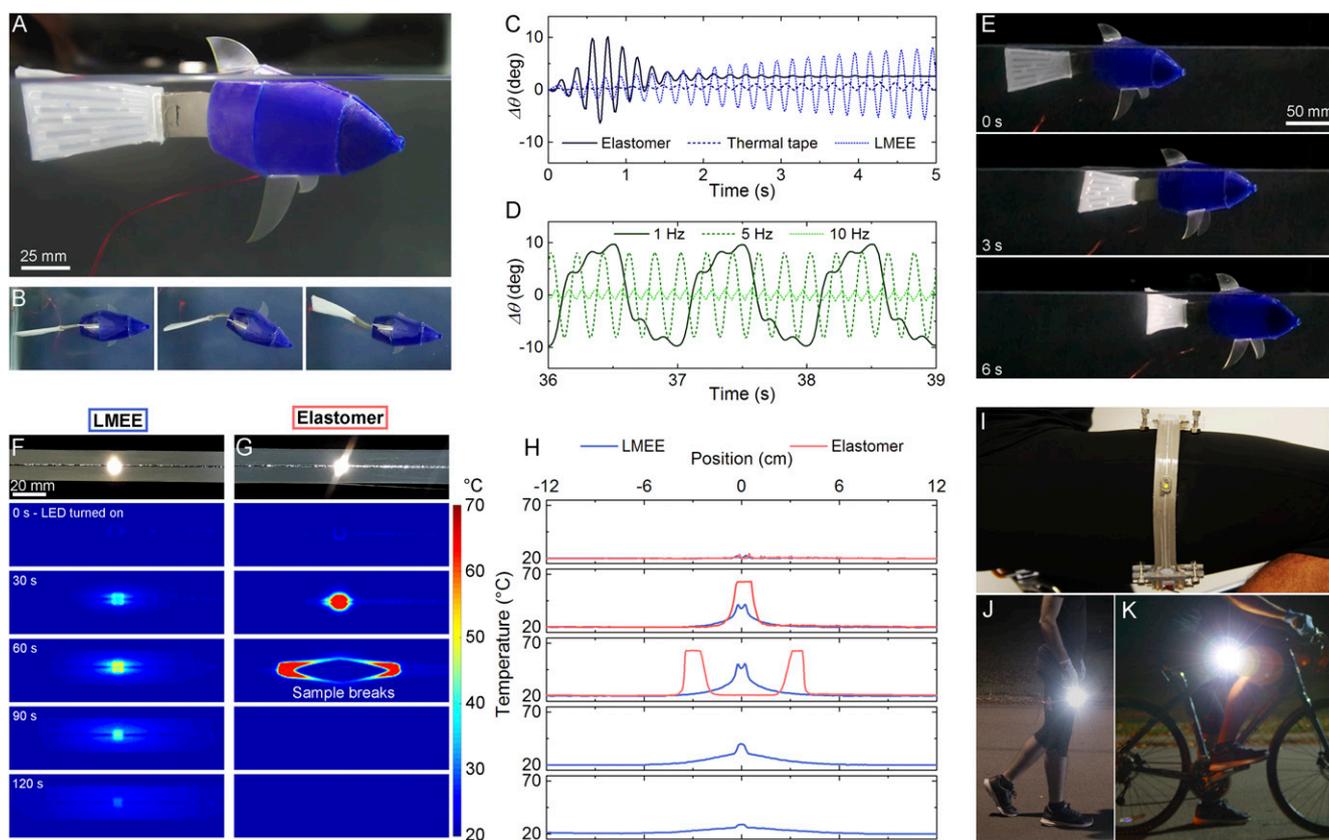
Because the LMEE composites are intrinsically soft and deformable, they can be incorporated as thermal interface materials into wearable computing (30) or thermally activated shape-programmable structures (31) and soft robotic systems (32, 33) without altering the natural mechanics of the host. For such applications, high thermal conductivity is not enough; the material must be sufficiently soft to limit mechanical resistance to deformation. We demonstrate this functionality through a thermally activated soft “artificial muscle” that is actuated with embedded wires of Ni–Ti shape memory alloy (SMA) and used for caudal fin locomotion of a silent, soft swimming robot (Fig. 3 *A* and *B*, Figs. S9 and S10, and Movie S2). Compared with thermally insulating silicone and relatively stiff thermal tapes, sealing the SMA wires in LMEE allows for significant enhancements in actuation frequency, deflection, and duration (Fig. 3 *C* and *D*). Specifically, the LMEE is able to actuate for more than 10,000 cycles at a frequency of 5 Hz (33.3 min) with no observed degradation in amplitude ( $14 \pm 1$  degrees; Fig. S9*D*). In contrast, the unfilled silicone elastomer becomes saturated with heat and ceases to actuate after 2 s. Although the commercial tape can support cyclical loading, its relatively high mechanical stiffness results in a low steady-state amplitude of  $\sim 3$  degrees. When

incorporated into the robotic fish, the LMEE-sealed SMA enables forward swimming at  $\sim 0.15$  body lengths per second (Fig. 3*E*).

Furthermore, we demonstrate the LMEE's potential as an exceptional material for thermal management in stretchable electronics and wearable computing by comparing infrared temperature maps of an extreme high power (XHP) LED lamp on stretched LMEE and unfilled silicone elastomer membranes (*Methods*). The poor thermal conductivity of the unfilled silicone elastomer results in excessive heat accumulation that leads to thermal degradation and dramatic mechanical failure. In contrast, the LMEE effectively dissipates heat and allows continuous operation of the LED (Fig. 3 *F–H* and Movie S3). To demonstrate the potential use of LMEEs as heat spreaders for low-profile wearable applications, an XHP LED lamp is mounted to a strip of LMEE that is wrapped around the thigh. This wearable lamp can operate during running, hiking, and cycling to provide exceptional visibility at night without the need for a socket mount (Fig. 3 *I–K* and Movie S4). It runs at power outputs greater than 1 W and produces substantially more light and heat than standard indicator LEDs, which run on milliwatts of power. The XHP LED is representative of a broader range of heat-generating devices (e.g., processors, transformers, power supplies) that could potentially be used in wearable computing and stretchable electronic circuits.

### Discussion and Conclusions

Electrically insulating solids with high thermal conductivity are typically rigid due to the dynamics of phonon transport within an



**Fig. 3.** Soft robot and stretchable electronics implementation of the LMEE composite. (A) Soft robotic fish composed of a silicone body and caudal fin connected by an LMEE-sealed SMA actuator. (B) Top-down view during forward caudal fin locomotion. (C) LMEE, unfilled silicone elastomer, and commercial thermal tape actuated at a frequency of 5 Hz. (D) LMEE actuated at 1-, 5-, and 10-Hz signal. (E) Time sequence images of the soft robotic fish swimming with a stroke frequency of 0.7 Hz. (F) XHP LED lamp mounted on an LMEE composite stretched to 400% strain with a sequence of IR images during LED operation. (G) The same experiment on an elastomer sample where the sample breaks at 60 s due to significant localized heating. (H) Temperature versus time plots for the IR image sequence, where the temperature is measured across the sample's length. LED is turned on and off at  $t = 0$  s and  $t = 70$  s, respectively. (I) An XHP LED is mounted to a strip of LMEE that is wrapped around the leg and shows high brightness during (J) running and (K) cycling.



**Mechanical Testing.** Mechanical samples are prepared in a dogbone shape, and tests are performed on an Instron 5969 mechanical testing machine using a 10 N load cell. Three samples are tested with LM volume ratio of 30% and 50%, under a strain rate of 10 mm/min. Samples are cyclically loaded three times at each of the following sequence of strains: 20%, 40%, 60%, 80%, 100%, 150%, and 200%. Fig. S8 A and B presents the stress–strain curves for LMEE for the 30% and 50% samples, respectively. The elastic modulus is calculated as the slope of the loading curve at a nominal strain of 10%. The nominal strain is defined with respect to the absolute stress-free strain of the sample, which increases during cyclical loading. In general, strain is calculated as a percentage defined with respect to the original length of the virgin sample (before initial loading). The 10% elastic modulus for the 30% and 50% samples is presented in Fig. S8 C and D, respectively.

**Soft Robotics Implementation.** We perform a series of illustrative artificial muscle implementations with SMA wire that enable the propulsion of a bioinspired, silent, soft swimming robot (Fig. 3 A and B and Movie S2). The actuator is composed of two naturally curved loops of SMA wire (0.012 in diameter; Dynalloy) that have an antagonistic arrangement and induce bidirectional bending when serially activated through direct Joule heating. The material encapsulating the SMA actuator is thus required to have both high thermal conductivity to facilitate heat transfer to the outer media and a low Young's modulus to allow significant deflection (Figs. S8 and S9). This advantage can be seen in Fig. 3C when actuators sealed in either LMEE, unfilled silicon, or commercial thermal tapes are actuated at a frequency of 5 Hz in a water bath. The LMEE-sealed actuator reaches a steady-state amplitude of ~10 degrees, whereas the unfilled silicone elastomer becomes saturated with heat and ceases to actuate, and the commercial tape reaches a much smaller amplitude of ~3 degrees because of its high mechanical stiffness. The LMEE-sealed actuator is also able to operate at a range of frequencies (Fig. 3D), with a maximum of 10 Hz. At frequencies above 5 Hz, the electrical pulse duration becomes shorter than the thermal time constant of the fin, and the amplitude of the periodic temperature oscillation within the SMA wire decreases. Details of the SMA actuator fabrication and testing are reported in *Thermal Actuator*.

When incorporated into a silicone-based soft robotic fish, the LMEE-sealed SMA enables forward caudal fin locomotion at ~0.15 body lengths per second (0.7 Hz activation). The body of the soft swimming robot is composed

of polydimethylsiloxane (PDMS; 1:10 base to curing agent ratio; Sylgard-184; Dow Corning) mixed with a blue pigment (0.3% by weight; Smooth-On); it is an assembly of three parts that are bonded to form two chambers as shown in Fig. S10, which are filled with EGaln and water, respectively, to balance the weight and buoyancy. Each individual part is produced by casting the dyed PDMS in a 3D-printed mold and then bonded together.

The caudal fin of the robot is composed of Ecoflex 00-30 (Smooth-On). As with the PDMS, the Ecoflex silicone is prepared using a THINKY AR-100 planetary centrifugal mixer. The elastomer is poured into molds for the two halves of the fin. After curing, the two layers of the film are bonded together with an additional layer of Ecoflex. The buoyancy is adjusted by filling the embedded chambers of the caudal fin with water.

**LED Demonstration.** LMEE and elastomer (Ecoflex 00-30; Smooth-On) samples are mounted on a frame and stretched to 400% strain. EGaln traces are applied with a stencil mask and connected to copper leads. XHP LED lamps (Cree XLamp XHP50, 5 mm × 5 mm) are placed onto the EGaln traces on the stretched samples. The LEDs are connected in parallel with a power supply, and 6 V and 500 mA are supplied at time  $t = 0$  s. IR images are captured with a FLIR A645sc Infrared Camera with a 45° lens at a frame rate of 25 frames per second.

For the wearable electronics demonstration, an XHP LED lamp (Cree XLamp XHP50, 5 mm × 5 mm) is placed on an LMEE layer with 3.5-mm thickness, and is sealed by another layer of LMEE. A thin layer of elastomer is used to seal the EGaln traces to stop the LM from spreading. EGaln traces are connected to banana plugs at the terminal end, which are secured in place using silicon adhesive and acrylic clamps. The LED is powered by a 9-V battery.

**ACKNOWLEDGMENTS.** We acknowledge J. Bartels and E. Markvicka for support with infrared imaging. M.D.B., N.K., and C.M. acknowledge support by the Air Force Office of Scientific Research Young Investigator Program (Mechanics of Multifunctional Materials and Microsystems; Dr. Les Lee; Award FA9550-13-1-0123) and NASA Early Career Faculty Award (NNX14AO49G). J.A.M. acknowledges support from the Army Research Office Grant W911NF-14-0350. Materials characterization was performed on equipment supported through an Office of Navy Research (ONR) Defense University Research Instrumentation Program (DURIP) (Bio-inspired Autonomous Systems; Dr. Tom McKenna; Award N00014140778).

- Kim G-H, et al. (2015) High thermal conductivity in amorphous polymer blends by engineered interchain interactions. *Nat Mater* 14(3):295–300.
- Singh V, et al. (2014) High thermal conductivity of chain-oriented amorphous polythiophene. *Nat Nanotechnol* 9(5):384–390.
- Wang XS, Tang HP, Li XD, Hua X (2009) Investigations on the mechanical properties of conducting polymer coating-substrate structures and their influencing factors. *Int J Mol Sci* 10(12):5257–5284.
- Miranzo P, et al. (2012) Anisotropic thermal conductivity of silicon nitride ceramics containing carbon nanostructures. *J Eur Ceram Soc* 32(8):1847–1854.
- Wong CP, Bollampally RS (1999) Thermal conductivity, elastic modulus, and coefficient of thermal expansion of polymer composites filled with ceramic particles for electronic packaging. *J Appl Polym Sci* 74(14):3396–3403.
- Mamunya YP, Davydenko VV, Pissis P, Lebedev EV (2002) Electrical and thermal conductivity of polymers filled with metal powders. *Eur Polym J* 38(9):1887–1897.
- Zeller RC, Pohl RO (1971) Thermal conductivity and specific heat of noncrystalline solids. *Phys Rev B* 4(6):2029–2041.
- Plawsky JL (2014) Transport Phenomena Fundamentals (CRC Press, Boca Raton, FL), 3rd Ed.
- Shen S, Henry A, Tong J, Zheng R, Chen G (2010) Polyethylene nanofibres with very high thermal conductivities. *Nat Nanotechnol* 5(4):251–255.
- Bigg DM (1986) Thermally conductive polymer compositions. *Polym Compos* 7(3):125–140.
- Cong H, Pan T (2008) Photopatternable conductive PDMS materials for micro-fabrication. *Adv Funct Mater* 18(13):1912–1921.
- Jeong SH, et al. (2015) Mechanically stretchable and electrically insulating thermal elastomer composite by liquid alloy droplet embedment. *Sci Rep* 5:18257.
- Hill RF, Supancic PH (2002) Thermal conductivity of platelet-filled polymer composites. *J Am Ceram Soc* 85(4):851–857.
- Chen Y-M, Ting J-M (2002) Ultra high thermal conductivity polymer composites. *Carbon* 40(3):359–362.
- Biercuk MJ, et al. (2002) Carbon nanotube composites for thermal management. *Appl Phys Lett* 80(15):2767–2769.
- Shahil KMF, Balandin AA (2012) Graphene-multilayer graphene nanocomposites as highly efficient thermal interface materials. *Nano Lett* 12(2):861–867.
- Kurabayashi K (2001) Anisotropic thermal properties of solid polymers. *Int J Thermophys* 22(1):277–288.
- Stankovich S, et al. (2006) Graphene-based composite materials. *Nature* 442(7100):282–286.
- Bartlett MD, et al. (2016) Stretchable, high-k dielectric elastomers through liquid-metal inclusions. *Adv Mater* 28(19):3726–3731.
- Fassler A, Majidi C (2015) Liquid-phase metal inclusions for a conductive polymer composite. *Adv Mater* 27(11):1928–1932.
- Lu Y, et al. (2015) Transformable liquid-metal nanomedicine. *Nat Commun* 6:10066.
- Dickey MD, et al. (2008) Eutectic gallium-indium (EGaln): A liquid metal alloy for the formation of stable structures in microchannels at room temperature. *Adv Funct Mater* 18(7):1097–1104.
- Yu S, Kaviany M (2014) Electrical, thermal, and species transport properties of liquid eutectic Ga-In and Ga-In-Sn from first principles. *J Chem Phys* 140(6):064303.
- Dickey MD (2014) Emerging applications of liquid metals featuring surface oxides. *ACS Appl Mater Interfaces* 6(21):18369–18379.
- Bruggeman DAG (1935) Berechnung verschiedener physikalischer Konstanten von heterogenen Substanzen. I. Dielektrizitätskonstanten und Leitfähigkeiten der Mischkörper aus isotropen Substanzen. *Ann Phys* 416(7):636–664. German.
- Ohmura T, Tsuboi M, Tomimura T (2002) Estimation of the mean thermal conductivity of anisotropic materials. *Int J* 23(3):843–853.
- Borca-Tasciuc T, Kumar AR, Chen G (2001) Data reduction in  $\omega$  method for thin-film thermal conductivity determination. *Rev Sci Instrum* 72(4):2139–2147.
- Han Z, Fina A (2011) Thermal conductivity of carbon nanotubes and their polymer nanocomposites: A review. *Prog Polym Sci* 36(7):914–944.
- Style RW, et al. (2015) Stiffening solids with liquid inclusions. *Nat Phys* 11:82–87.
- Rogers JA, Someya T, Huang Y (2010) Materials and mechanics for stretchable electronics. *Science* 327(5973):1603–1607.
- Haines CS, et al. (2014) Artificial muscles from fishing line and sewing thread. *Science* 343(6173):868–872.
- Morin SA, et al. (2012) Camouflage and display for soft machines. *Science* 337(6096):828–832.
- Larson C, et al. (2016) Highly stretchable electroluminescent skin for optical signaling and tactile sensing. *Science* 351(6277):1071–1074.
- Nagasaka Y, Nagashima A (1981) Absolute measurement of the thermal conductivity of electrically conducting liquids by the transient hot-wire method. *J Phys Educ* 14(12):1435–1440.
- Sen PA, Scala C, Cohen MH (1981) A self-similar model for sedimentary rocks with application to the dielectric constant of fused glass bead. *Geophysics* 46(5):781–795.
- Mishra V, Hardin CL, Garay JE, Dames C (2015) A 3 omega method to measure an arbitrary anisotropic thermal conductivity tensor. *Rev Sci Instrum* 86(5):054902.
- Reinecke BN, Shan JW, Suabedissen KK, Cherkasova AS (2008) On the anisotropic thermal conductivity of magnetorheological suspensions. *J Appl Phys* 104(2):023507.