

Artificial Intelligence Methods for Social Good

M2-3 [Game Theory]:

Human Behavior Modeling

08-537 (9-unit) and 08-737 (12-unit)

Instructor: Fei Fang

feifang@cmu.edu

Wean Hall 4126

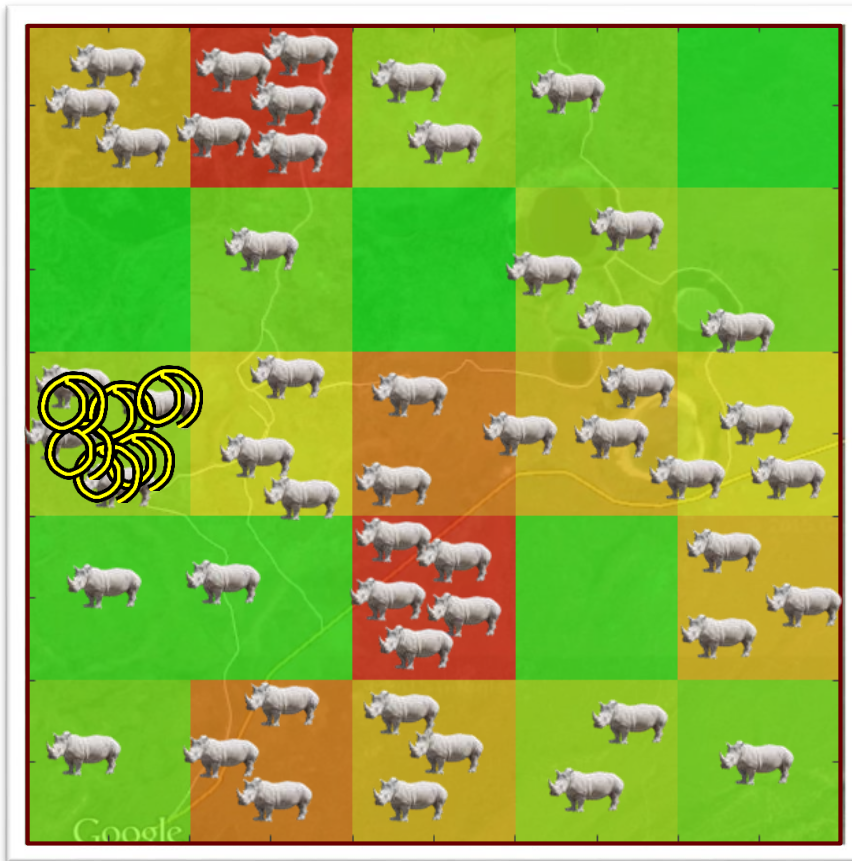
Challenges in Wildlife Conservation

- ▶ Frequent and repeated attacks
 - ▶ Not one-shot
- ▶ Attacker decision making
 - ▶ Limited surveillance / Less effort / Boundedly rational
- ▶ Real-world data
 - ▶ Sparse / Incomplete / Uncertainty / Noise
- ▶ Real-world deployment
 - ▶ Practical constraints
 - ▶ Field test



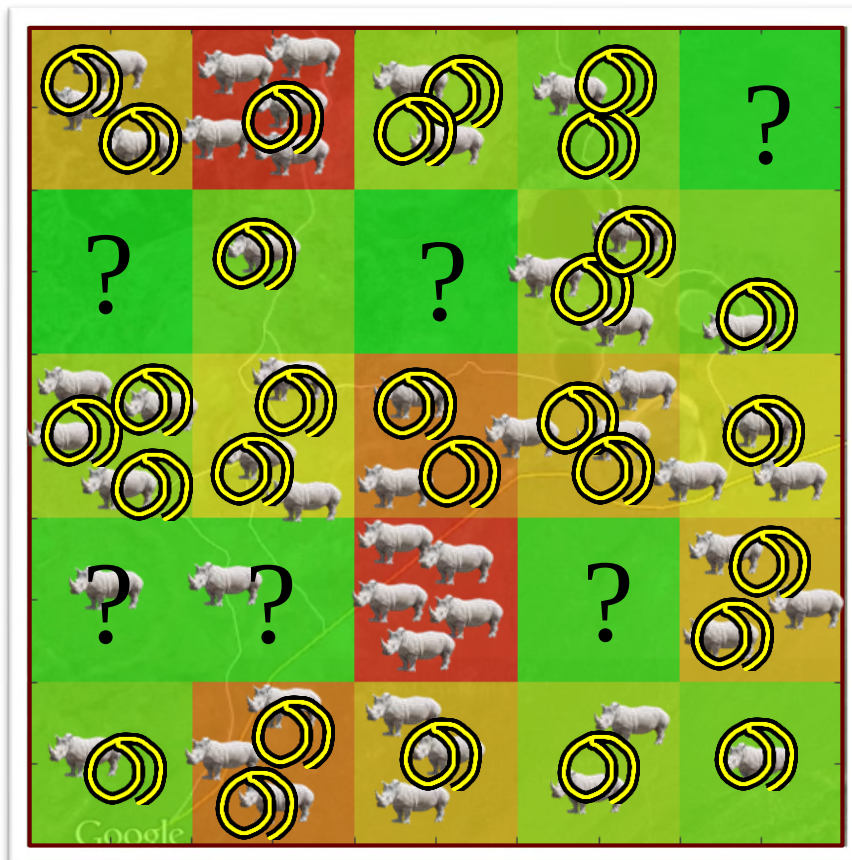
Challenges in Wildlife Conservation

- Perfectly rational (Maximize expected utility)? No!



Challenges in Wildlife Conservation

► Real-world data



Human Behavior Modeling & Learning

- ▶ **Uncertainty and Bias Based Models**
 - ▶ Prospect Theory [Kahneman and Tvesky, 1979]
 - ▶ Anchoring bias and epsilon-bounded rationality [Pita et al, 2010]
 - ▶ Attacker aims to reduce the defender's utility [Pita et al, 2012]
- ▶ **Quantal Response Based Models**
 - ▶ Quantal Response [McKelvey and Palfrey, 1995]
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- ▶ **Latest Models**
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- ▶ **PAWS**

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PT: Prospect Theory

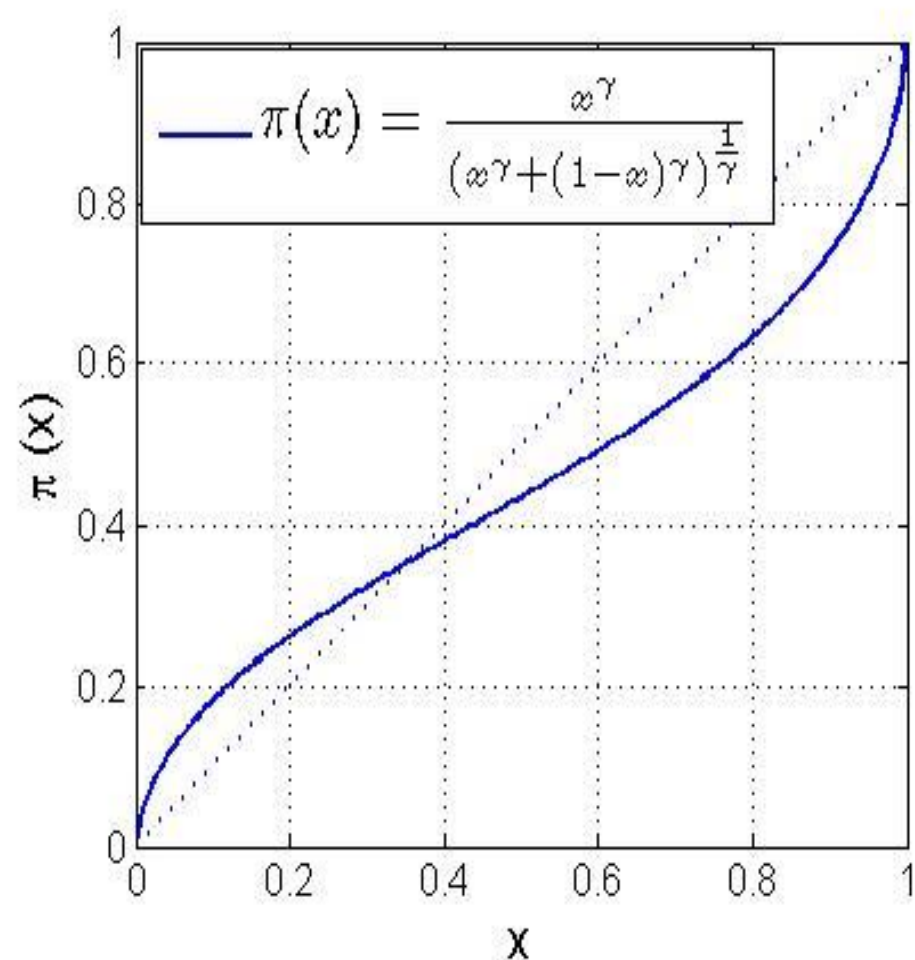
- ▶ Model human decision making under uncertainty
- ▶ Maximize the 'prospect' [Kahneman and Tversky, 1979]

$$\text{prospect} = \sum_{i \in \text{AllOutcomes}} \pi(x_i) \cdot V(C_i)$$

- ▶ $\pi(\cdot)$: weighting function
- ▶ $V(\cdot)$: value function
- ▶ Defender: choose a strategy that maximizes DefEU when attacker best responds to the expected prospect (instead of AttEU)

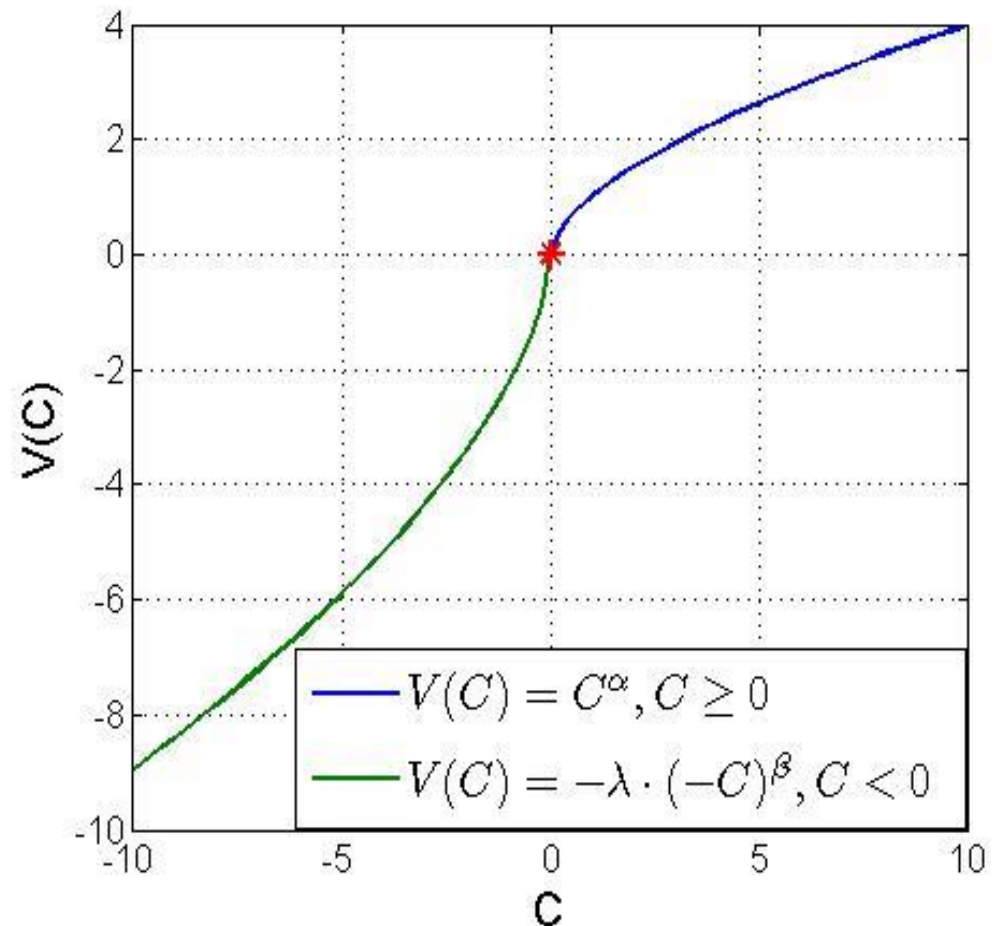
PT: Prospect Theory

- ▶ Empirical Weighting Function
- ▶ Slope gets steeper as x gets closer to 0 and 1
- ▶ Not consistent with probability definition
 - $\pi(x) + \pi(1-x) < 1$
- ▶ Empirical value:
 $\gamma = 0.64$ ($0 < \gamma < 1$)



PT: Prospect Theory

- ▶ Empirical Value Function
- ▶ Risk averse regarding gain
- ▶ Risk seeking regarding loss
- ▶ Empirical value:
 $\alpha=\beta=0.88, \lambda=2.25$



COBRA: Anchoring Bias and Epsilon-Bounded Rationality

- ▶ “epsilon optimality”
- ▶ Anchoring bias: Full observation ($\alpha = 0$) vs no observation ($\alpha = 1$)

$$\max_{x,q,\gamma,a} \gamma$$

$$s.t. x' = (1 - \alpha)x + \frac{\alpha}{N}$$

a is attacker's highest expected utility given x'

$$q_j = 1 \text{ if } \text{AttEU}_j(x') \geq a - \epsilon$$

$$\gamma \leq \text{DefEU}_j(x) \text{ if } q_j = 1$$

- ▶ Experiments: $\alpha = 0.37$ works best

MATCH: Attacker aims to reduce the defender's utility

- ▶ Attacker may deviate from the best response to reduce the defender's expected utility
- ▶ Choose a target to maximize
$$\frac{\text{Defender's utility loss due to deviation}}{\text{Adversary's utility loss due to deviation}}$$
- ▶ Defender: choose a strategy that maximize DefEU while bound the above value by β
- ▶ Experiments: $\beta = 1$

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QR: Quantal Response Model

- ▶ Error in individual's response
 - ▶ Still: more likely to select better choices than worse choices
- ▶ Probability distribution of different responses
- ▶ Quantal best response:

$$q_j = \frac{e^{\lambda * \text{AttEU}_j(x)}}{\sum_i e^{\lambda * \text{AttEU}_i(x)}}$$

- ▶ λ : represents error level (=0 means uniform random)
 - ▶ Maximal likelihood estimation ($\lambda=0.76$)

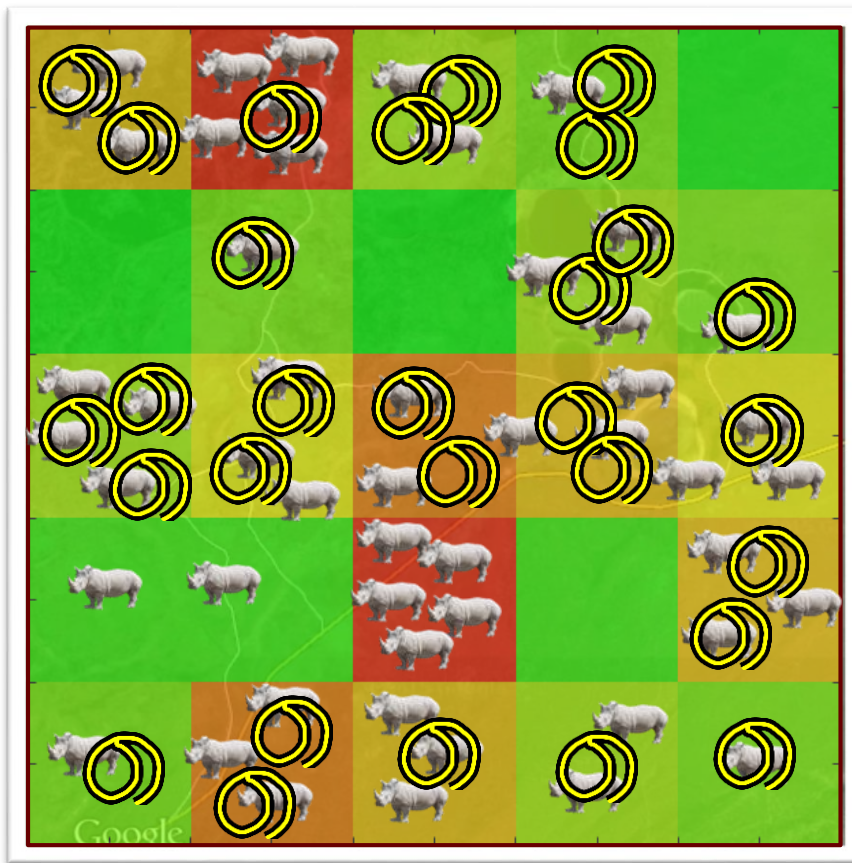
Quiz I: Quantal Response Model

- ▶ If there are two choices (actions), what is the probability of choosing the first action if the player follows quantal response model with $\lambda = 0$?
 - ▶ 1
 - ▶ 0
 - ▶ $\frac{1}{2}$
 - ▶ $\frac{1}{e} \approx 0.368$

$$q_j = \frac{e^{\lambda * \text{AttEU}_j(x)}}{\sum_i e^{\lambda * \text{AttEU}_i(x)}}$$

SUQR: Subjective Utility Quantal Response Model

► $SEU_j = \sum_k w_k * f_j^k, \quad q_j = \frac{e^{\lambda * SEU_j(x)}}{\sum_i e^{\lambda * SEU_i(x)}}$



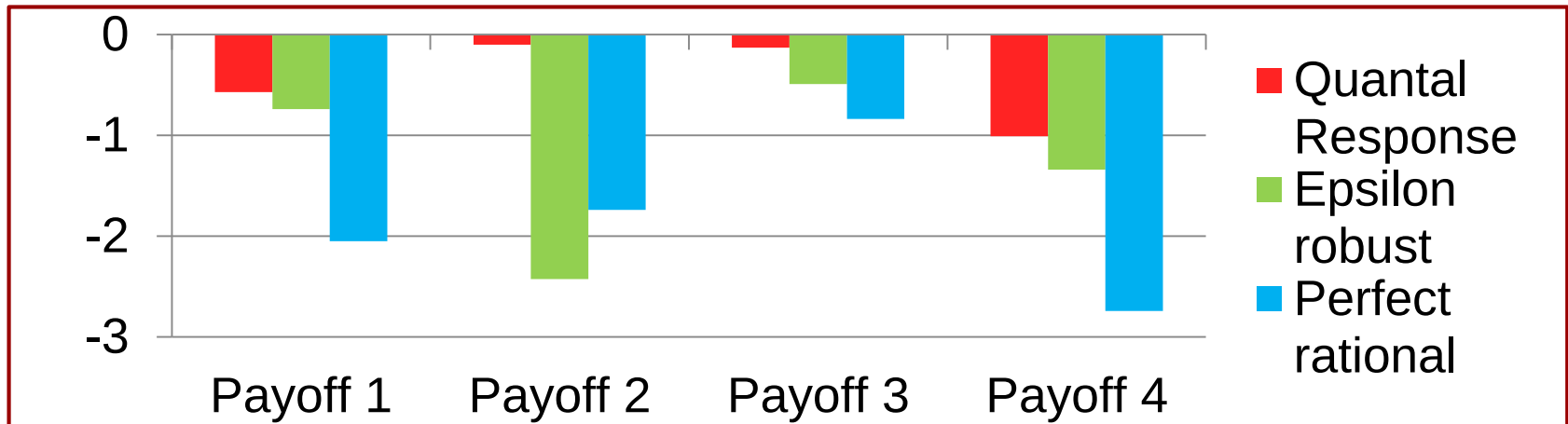
Coverage Probability
+ Reward/Penalty



Attack Probability

Comparison of Model Performance

► Prospect Theory < DOBSS < COBRA < Quantal Response < MATCH < SUQR



MATCH wins	Draw	QR wins
42	52	6

MATCH wins	Draw	SUQR wins
1	8	13

Human Behavior Modeling & Learning

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- ▶ **PAWS Application**

GSG: Incorporating Delayed Observation

Wildlife



Forest



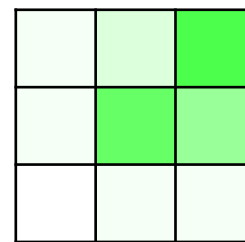
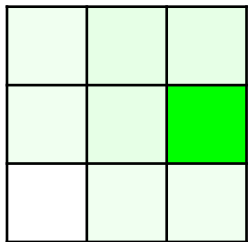
Fishery



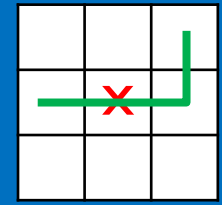
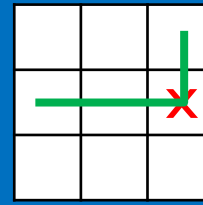
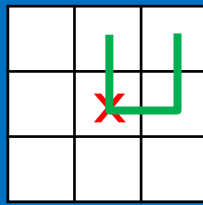
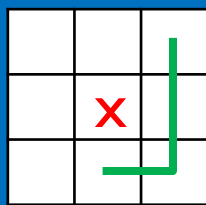
- ▶ Frequent and repeated attacks
 - ▶ Not one-shot / More data
- ▶ Attacker decision making
 - ▶ Limited surveillance / Less effort / Boundedly rational
- ▶ New model: Green Security Games

GSG: Incorporating Delayed Observation

Defender



Time



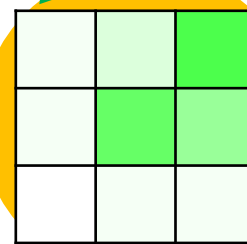
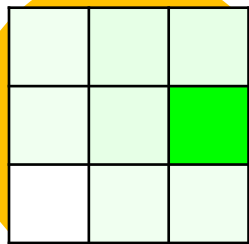
Poacher



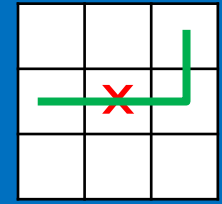
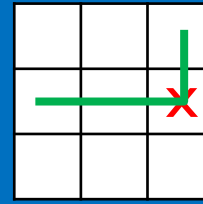
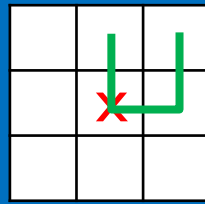
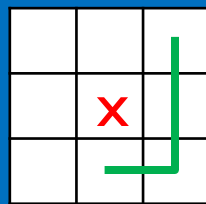
GSG: Incorporating Delayed Observation

Defender

Hidden from poacher



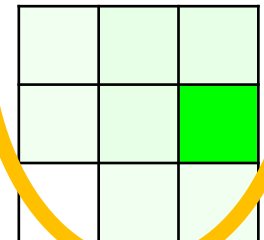
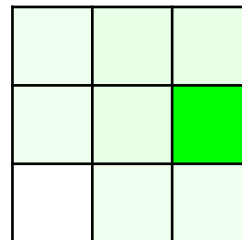
Time



Poacher

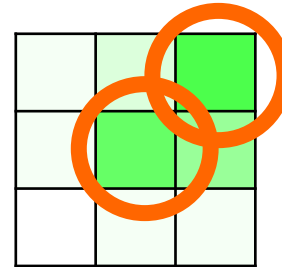
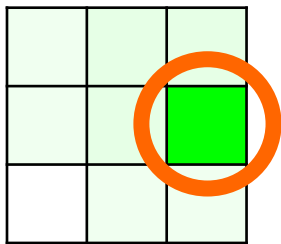


Poachers' understanding

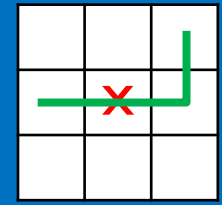
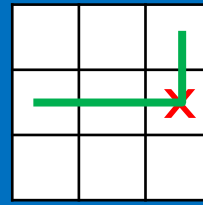
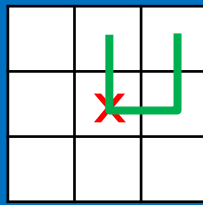
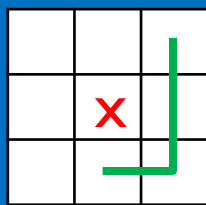


GSG: Incorporating Delayed Observation

Defender



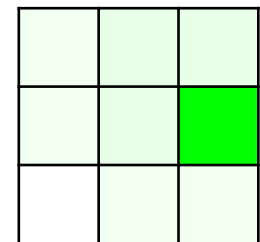
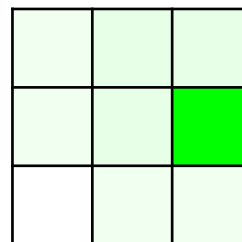
Time



Poacher



Poachers' understanding

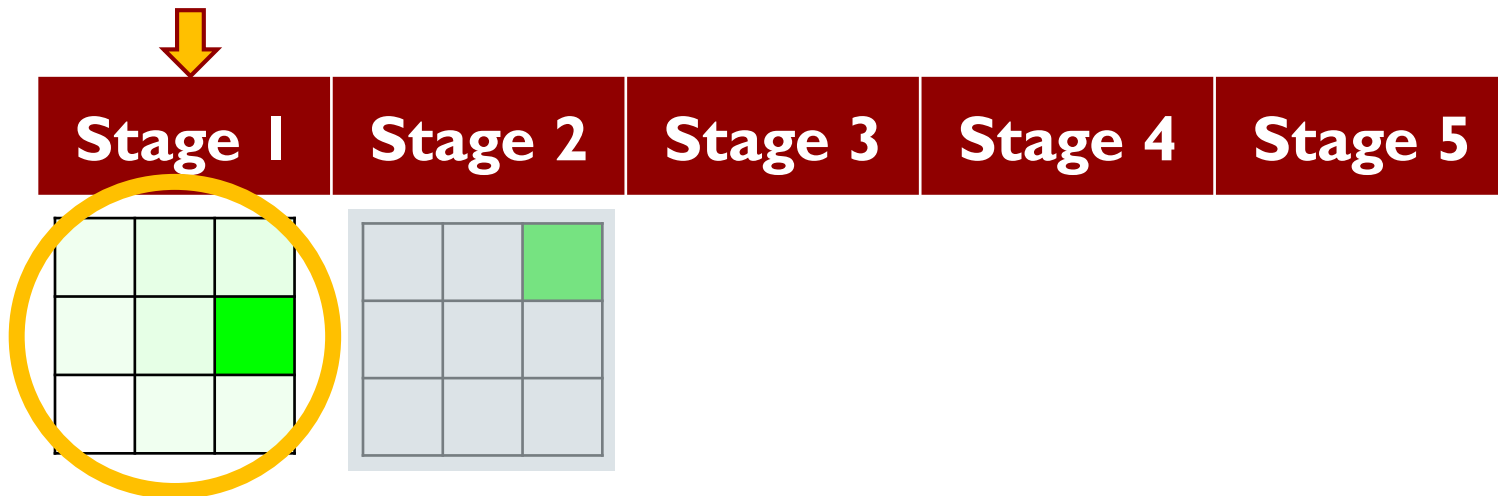


GSG: Incorporating Delayed Observation

- ▶ A Green Security Game (GSG) is a T stage game where the defender protects N targets against L attackers. Defender chooses a mixed strategy c^t in stage t .
- ▶ A GSG attacker is characterized by his memory length Γ , coefficients $\alpha_0, \dots, \alpha_\Gamma$ and SUQR model parameter ω . In stage t , he responds to a convex combination of defender strategy in recent $\Gamma + 1$ rounds: $\eta_t = \sum_{\tau=0}^{\Gamma} \alpha_\tau c^{t-\tau}$

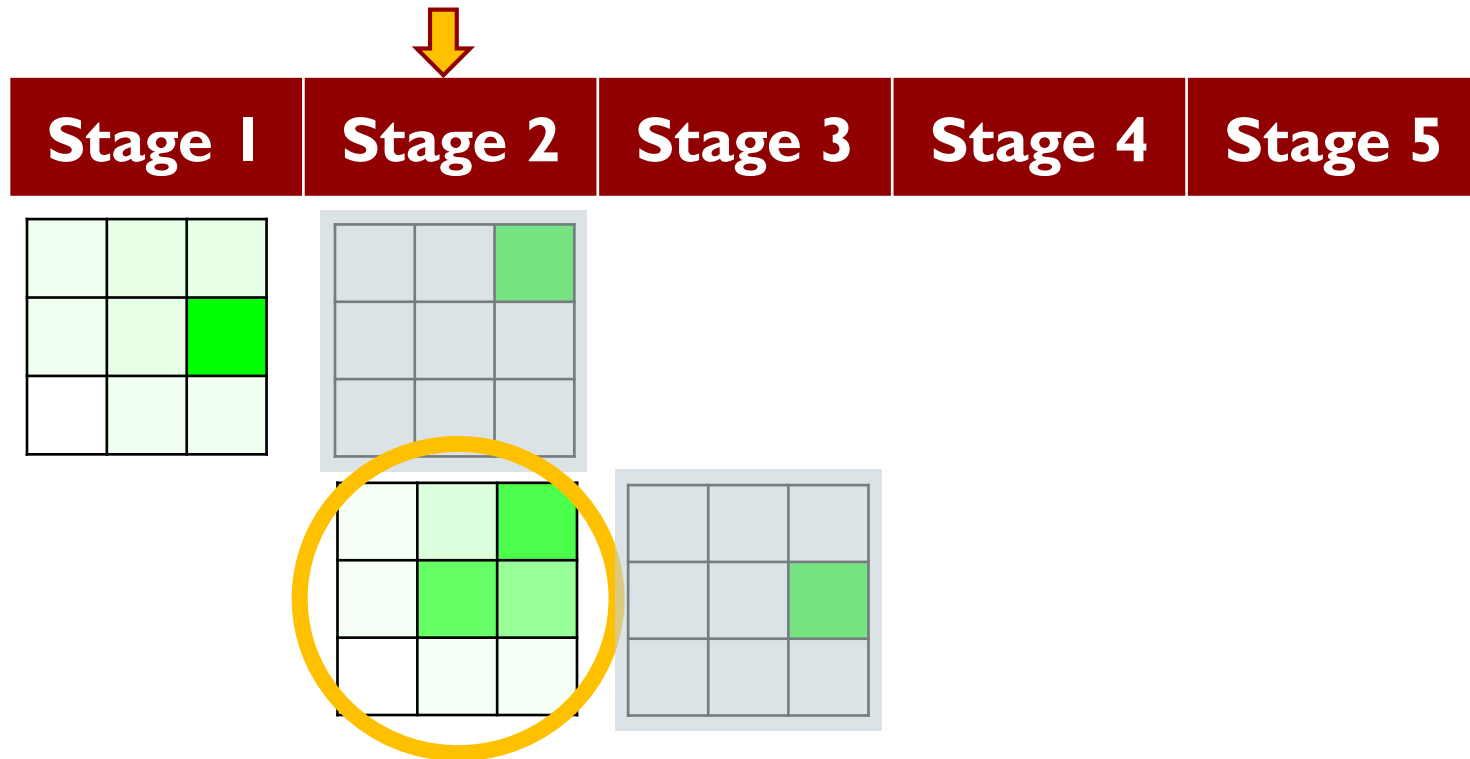
GSG: Incorporating Delayed Observation

- ▶ Plan Ahead – M (PA-M)
- ▶ Plan ahead M stages



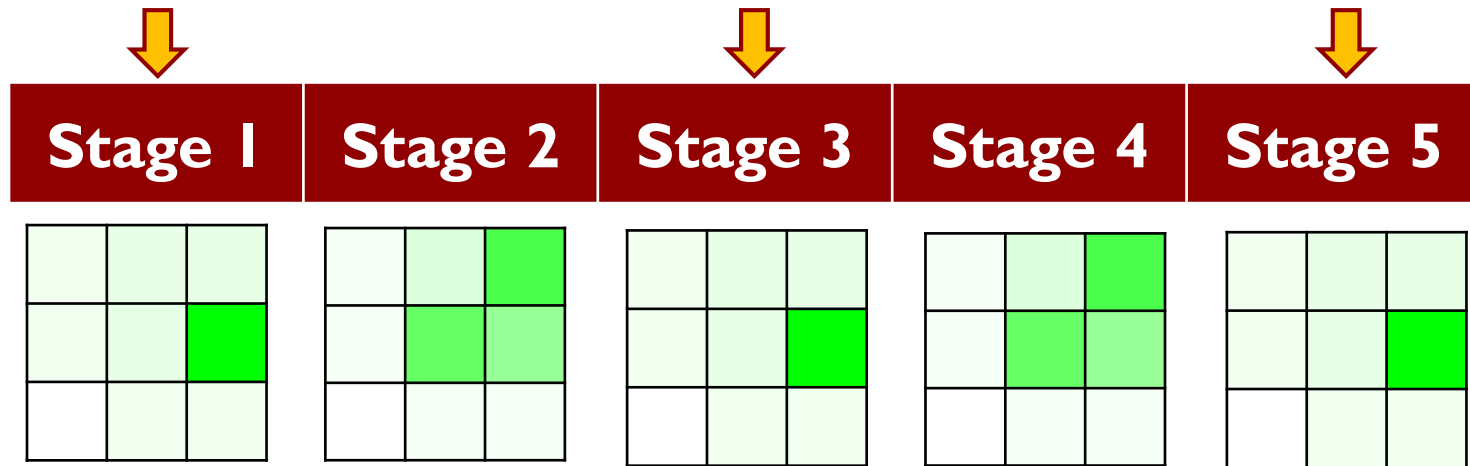
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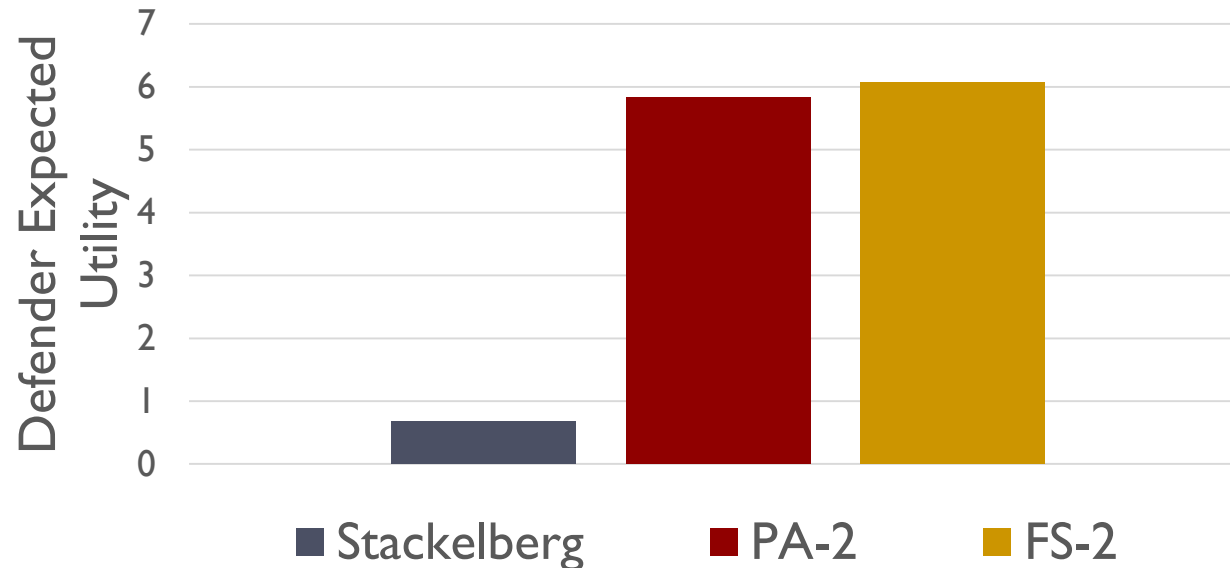


GSG: Incorporating Delayed Observation

- ▶ An alternative: Fixed Sequence – M (FS-M)
- ▶ Use M strategies repeatedly



GSG: Incorporating Delayed Observation



- **Theorem 3:** In a GSG with T rounds, for $\Gamma < M \leq T$, there exists a cyclic defender strategy profile $[s]$ with period M that is a $(1 - \frac{\Gamma}{T}) \frac{Z-1}{Z+1}$ approximation of the optimal strategy profile in terms of the normalized utility, where $Z = \left\lceil \frac{T-\Gamma+1}{M} \right\rceil$

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SHARP: Bounded Rationality in Repeated Games

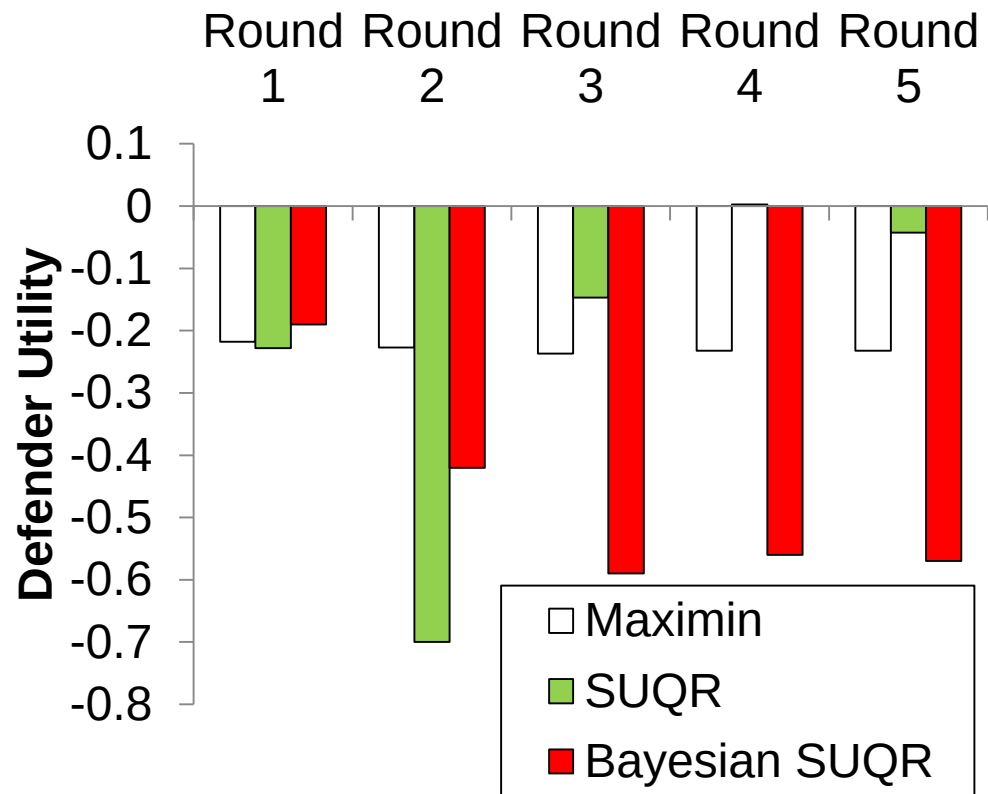
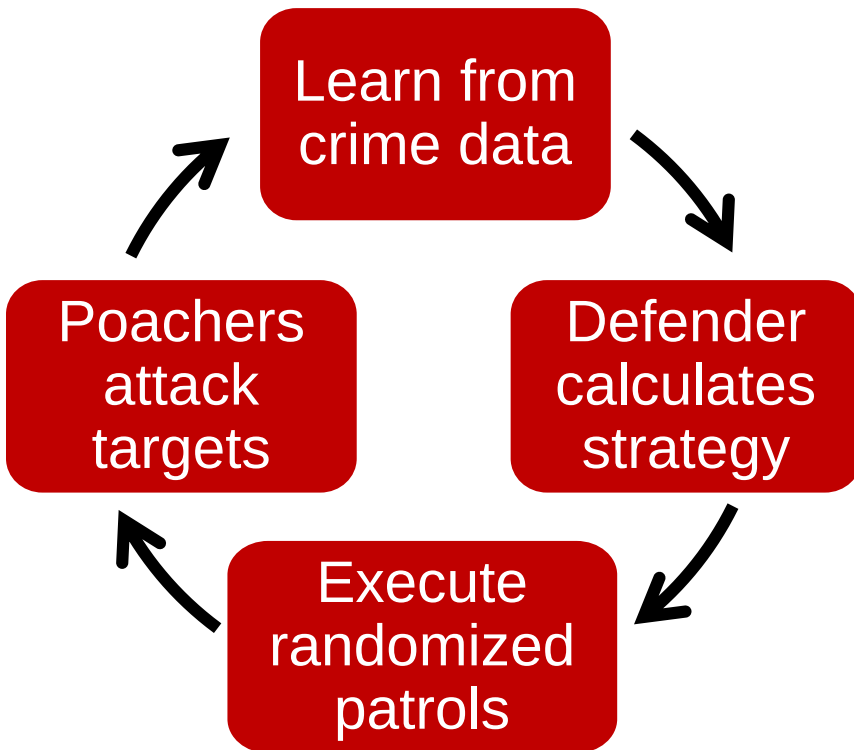


Game 4

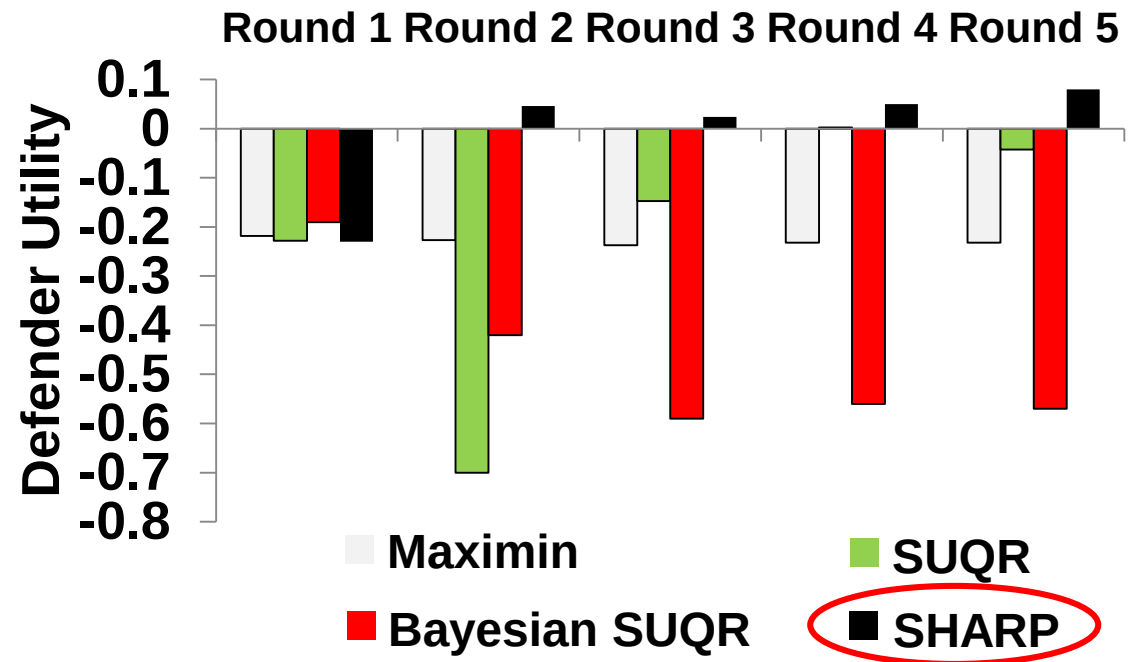
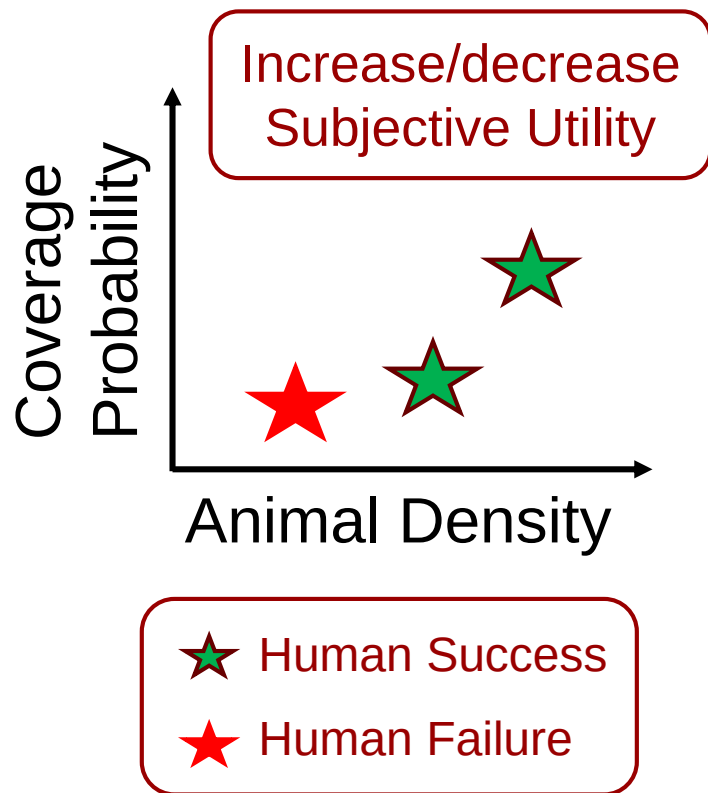
Total: \$1.5

SHARP: Bounded Rationality in Repeated Games

Repeated games on AMT: 35 weeks, 40 human subjects 10,000 emails!

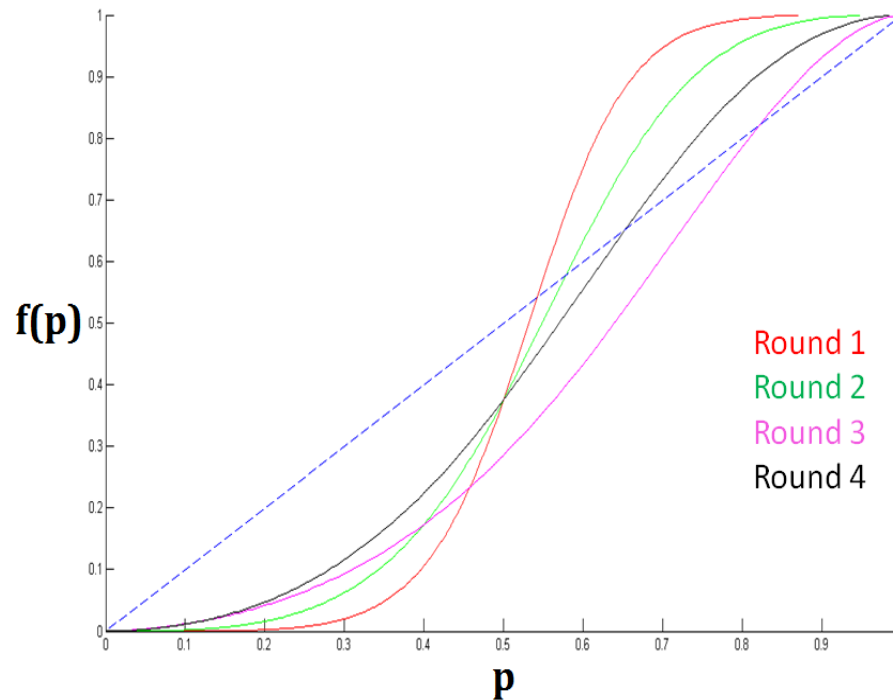


SHARP: Bounded Rationality in Repeated Games



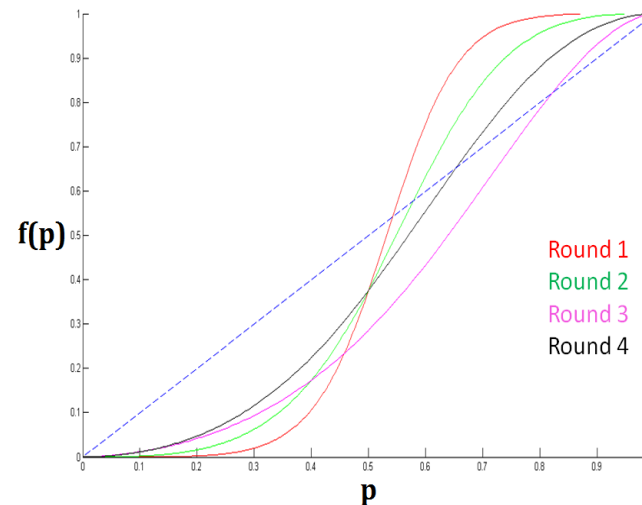
SHARP: Bounded Rationality in Repeated Games

- ▶ Adversary's probability weighting function is S-shaped.
 - ▶ Contrary to Prospect Theory

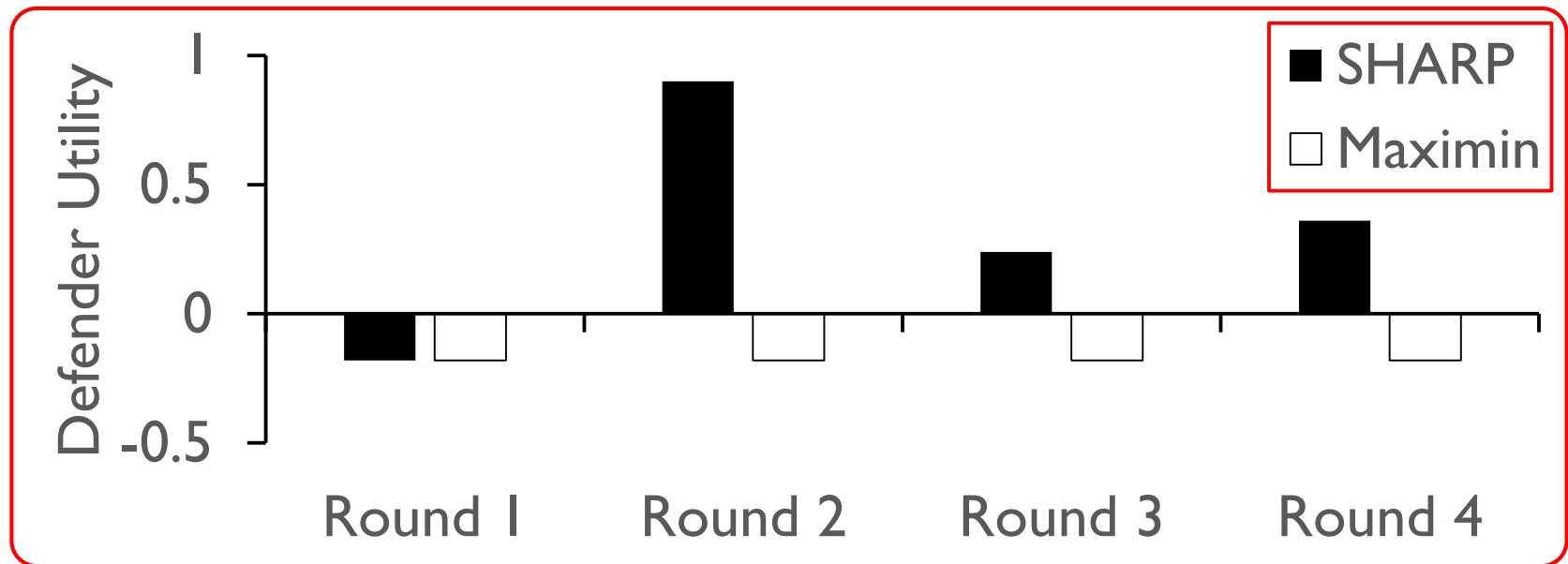


Quiz 2: SHARP

- ▶ According to the learned weighting function, which is S-shaped, the human players are _____ the probability of getting caught when the probability is low
 - ▶ Over-estimating
 - ▶ Under-estimating



SHARP: Bounded Rationality in Repeated Games

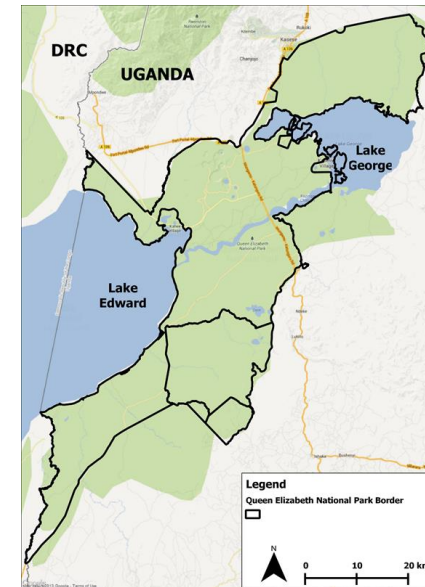


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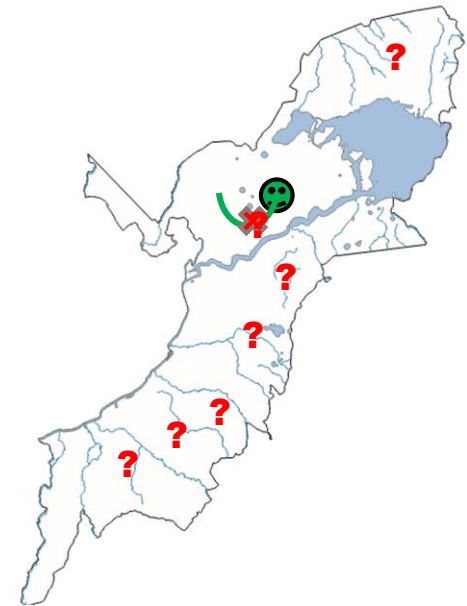
Real-World Data

- ▶ Queen Elizabeth National Park
 - ▶ 1,978 sq. km
 - ▶ 2003-2015
- ▶ Geospatial Features
 - ▶ Terrain (e.g., forest, slope)
 - ▶ Distance to {Town, Water, Outpost}
- ▶ Ranger Coverage
- ▶ Crime Observations

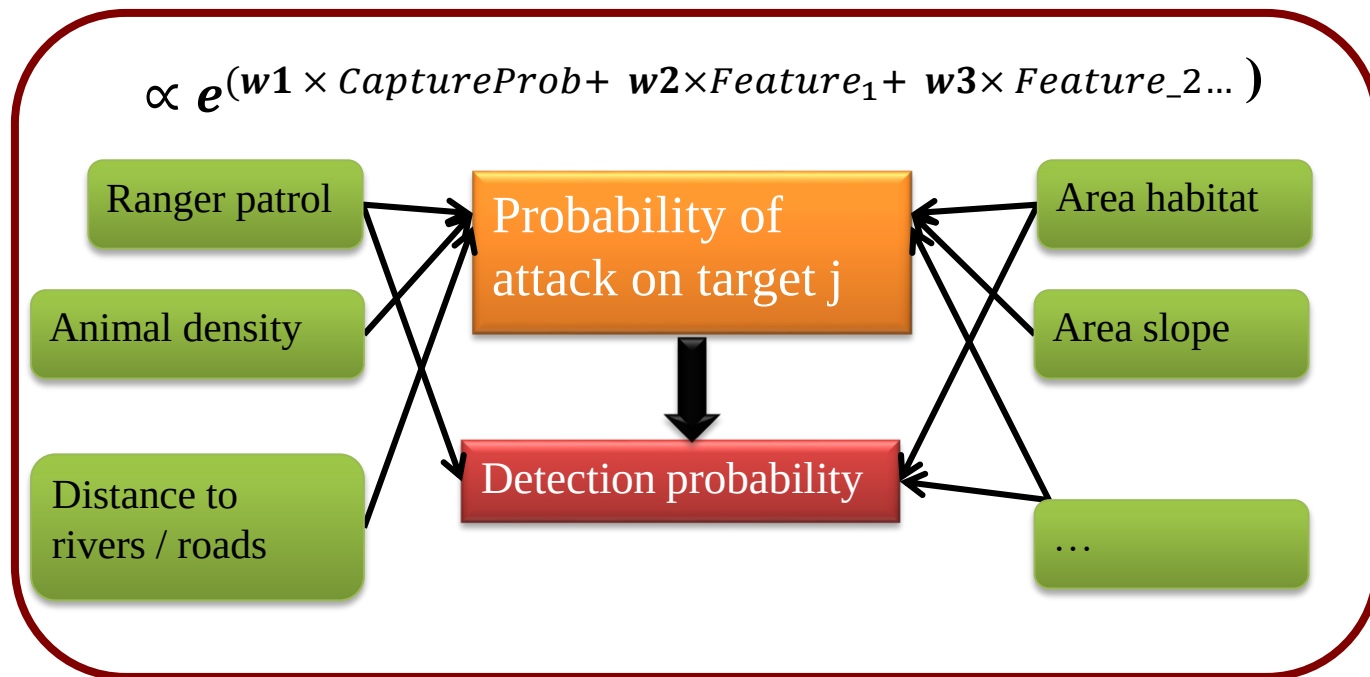


Real-World Data: Challenges

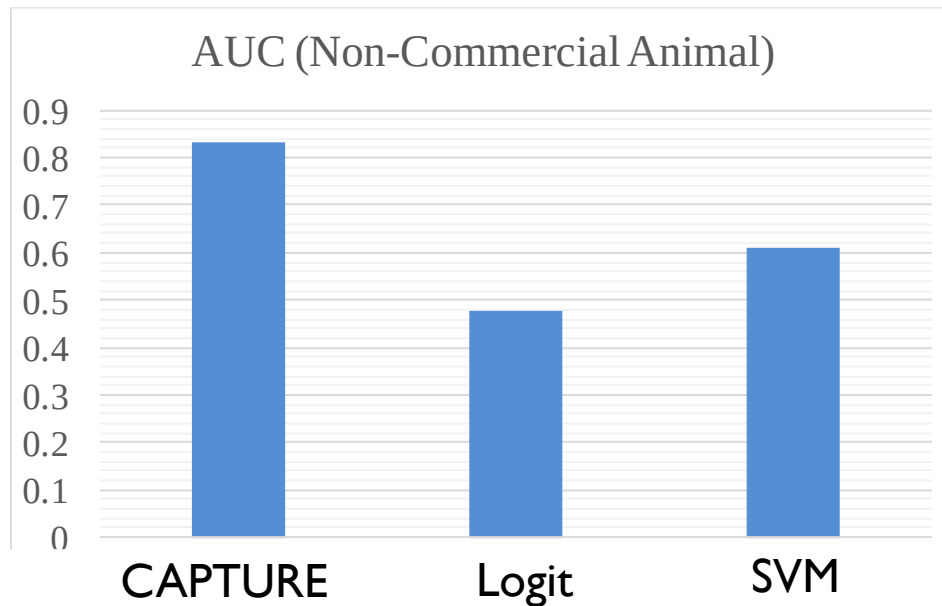
- ▶ “Missing” poaching data
 - ▶ Limited patrol resources (silent victims)
 - ▶ Imperfect observations (e.g., hidden snares)
- ▶ Consequences
 - ▶ Uncertainty in negative labels
 - ▶ Class imbalance



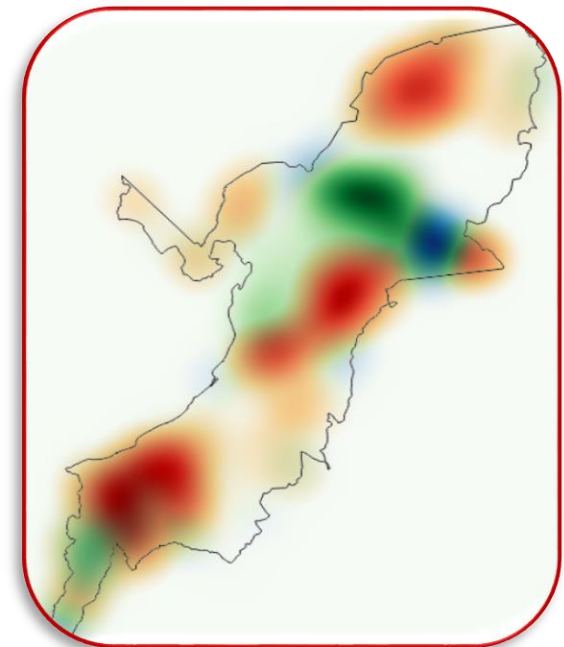
CAPTURE: Two-Layered Model



CAPTURE: Two-Layered Model



Dry Season (June-August 2008)



Green – Animal Density;

Blue – Defender Strategy;

Red – Observed Attack Probability

Quiz 3: Real-World Data Challenge

- ▶ Which of the following are challenges in the real-world data collected through anti-poaching patrols?
 - ▶ Limited amount of data
 - ▶ Uncertainty in negative labels
 - ▶ Class imbalance
 - ▶ Uncertainty in positive labels