

Definition MunkTop.16.1: If (X, \mathcal{T}) is a topological space and $Y \subseteq X$ then *the subspace topology on Y inherited from (X, \mathcal{T})* is $\{Y \cap U : U \in \mathcal{T}\}$.

Definition MunkTop.16.2: If (X, \mathcal{T}) is a topological space and $Y \subseteq X$ then (Y, \mathcal{T}') is a *subspace* of (X, \mathcal{T}) if and only if \mathcal{T}' equals the subspace topology on Y inherited from (X, \mathcal{T}) .

Definition MunkTop.16.3: If then *the dictionary order on $(R, A) \times (S, B)$* is the unique T such that for every $y, y \in T$ if and only if there exist p, q, r, s such that $y = ((p, q), (r, s))$ and $p, r \in A$ and $q, s \in B$ and pRr or $p = r$ and qSs .

Definition MunkTop.16.4: If $I = [0, 1]$ and R equals the dictionary order on $(\{(x, y) : x < y\}, I) \times (\{(x, y) : x < y\}, I)$ then *the ordered square I_0^2* is $(I \times I, \text{the order topology on } (I \times I, R))$.

Definition MunkTop.16.5: If R is a strict sipmle order on X and $Y \subseteq X$ then Y is a *convex* subset of (X, R) if and only if for every $a, b \in Y$, $(a, b) \subseteq Y$.