

# 15-451 Mini 3

Feb 19, 2008

This mini is due via \*email\* to your TA, by midnight Tuesday Feb 19.  
Please use the subject line "15-451 MINI #3" in your email.  
Questions/concerns/comments to Dafna Shahaf <dshahaf+451@cs.cmu.edu>

## 1 Question 1: Treaps

Consider the following (key priority) pairs:

$(a\ 4), (b\ 6), (c\ 1), (d\ 3), (e\ 2), (f\ 5)$

1. Choose any ordering you would like on those elements (such as  $\langle b, d, f, e, c, a \rangle$ ) and illustrate inserting them into a treap, step by step, in that order. An ascii drawing is fine.
2. In what way, if any, does the final treap depend on the chosen ordering of insertions?

## 2 Question 2: Hashes

Consider the following two hash functions  $h_1$  and  $h_2$  from  $\{1, 2, 3\}$  to  $\{0, 1\}$ :

	1	2	3
$h_1$	0	0	1
$h_2$	0	1	0

In other words,  $h_1(1) = 0, h_1(2) = 0, h_1(3) = 1, h_2(1) = 0, h_2(2) = 1, h_2(3) = 0$ . Is the set  $H = \{h_1, h_2\}$  a universal hash family? Why or why not?