# 1. **Problem 1**

Let  $L_1 \subset L_2$ .

(a) If  $L_1$  is a regular language, then is  $L_2$  necessarily a regular language?

Solution:

(b) If  $L_2$  is a regular language, then is  $L_1$  necessarily a regular language?

Solution:

## 2. **Problem 2**

Consider a regular language L that accepts a string if the 6th to last bit is a 1 (over an alphabet of  $\{0, 1\}$ .

(a) Construct an NFA that recognizes L.

#### Solution:

(b) Argue that any DFA which recognizes L must have at least 64 states.

Solution:

## 3. Problem 3

Given a DFA for L, provide a formal construction for a DFA that recognizes L<sup>\*</sup>. In other words, provide the 5-tuple that characterizes  $Kleene(L) = \{w_1...w_k | k \ge 0 \text{ and } each w_i \in L\}$ .

Solution:

### 4. Problem 4

Draw a DFA that accepts the regular language represented by the regular expression  $((01)^*)001$ .

Solution: