Should Teachers Know, or Know How to Teach?

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April 29, 2006

This is a revised version of a paper presented at the session on teacher quality at the March, 2001 American Educational Finance Association Annual Research Conference. The authors benefited from comments of session participants, Dan Goldhaber, Drew Gitomer and Henry Levin, and the comments of two anonymous referees. Responsibility for the paper rests solely with the authors.
Abstract

While there is growing national concern about inadequate student achievement in the US compared to that of our trading partners and a growing awareness that teacher quality is a primary determinant of student learning, there remain outstanding questions about what characteristics of teachers lead to improved learning outcomes of their students. Sanders (1996) and more recently Rivkin, Hanushek and Kain (2005) document through micro-econometric estimation that some teachers have large, persistent, and statistically significant effects on student learning outcomes. However, what in particular about such successful teachers explains positive student learning outcomes remains essentially unknown.

Similarly, while there is general awareness that what a classroom teacher knows and how they teach it must make a difference in student achievement, there is still little systematic evidence on the relationship between various teacher characteristics and student achievement. This paper reports the results of estimating a multi-equation model of hiring policies, teacher characteristics that distinguish between general knowledge and pedagogical knowledge, and student achievement at the district level in Pennsylvania.

We find that, before correcting for endogeneity of teacher quality \textit{viz a viz} the hiring decision, the \textit{elasticity} of median ETS National Teacher Exam General Knowledge test scores on multidimensional measures of student achievement is about .8. However, \textit{after} correcting for endogeneity of this teacher quality measure \textit{viz a viz} the hiring decision, the elasticity is very large in absolute value (from about 8.0 to 12.0) and statistically significant. We also find that the median Professional Knowledge test score is typically negatively related to student achievement. After correcting for endogeneity, the elasticity remains negative, but becomes much larger in absolute value, although it is typically not statistically significant. Various robustness tests indicate that these findings with respect to General Knowledge and Professional Knowledge are relatively stable.

Although problems with instrument strength preclude reaching definitive conclusions, the very large positive effect of General Knowledge on student achievement, and the very large negative effect of Professional Knowledge on student achievement warrant further investigation by the research community.

These findings also suggest that institutions responsible for preparing classroom teachers likely will do a better job \textit{viz a viz} student achievement if they emphasize General Knowledge rather than Professional Knowledge in these preparation activities.
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1 Introduction

Successful public school reform in the U.S. is increasingly described by educators and commentators on education in terms of increased student learning, both in terms of greater proportions of students testing at grade level, and in terms of generally higher levels of student achievement. School reform increasingly embraces repeated assessment of students and teachers as diagnostic and management devices, adoption of the view that all students can achieve at high levels\textsuperscript{1}, the increased use of technology to complement traditional classroom pedagogy, increased parental involvement in the educational process, and the reduction in class size at least in earlier grades to cement basic learning skills.\textsuperscript{2} Some also suggest improvements in school governance\textsuperscript{3}, and greater attention to academic quality of teachers in the teacher selection process\textsuperscript{4}.

While improving teacher quality is now generally embraced as central to successful educational reform, there remains significant disagreement among those who study teacher preparation about how important content knowledge and general academic preparation are viz. a viz. pedagogical knowledge in the preparation of teachers.\textsuperscript{5}

Our purpose in this paper is several fold:

1. to examine the path through which insularity of school districts affects student learning outcomes through effects on teacher quality of those hired found earlier by Strauss, Bowes, Marks, and Plesko (2000) for Pennsylvania school districts,

2. to examine the importance of teacher quality as measured by various teacher test scores on student learning outcomes and thus investigate whether or not the very large effects of such test scores found earlier by Strauss and Sawyer(1986) in North Carolina school districts are sustained,

3. to distinguish among types of teacher proficiencies (general vs. pedagogical knowledge) while holding constant other factors such as the teacher selection decision, and

4. suggest a methodological innovation in characterizing student learning outcomes by constructing an index of learning through the use of factor analysis.

\textsuperscript{1}Levin(1997)

\textsuperscript{2}Although see Hanushek (1999) for cautionary results.

\textsuperscript{3}Strauss and Severino(2005)

\textsuperscript{4}See Ballou and Podgursky (1997a) who find that districts often do not hire the most academically qualified teachers, and Strauss, Bowes, Marks and Plesko(2000) who report on insularity in the teacher selection process.

\textsuperscript{5}There is an increasingly vigorous debate about the whether or not students learn more from teachers who are traditionally certified by schools of education, as compared to teachers who are not so traditionally certified. For contrasting views, for example, Goldhaber and Brewer(1999) and Darling-Hammond(2000).
The paper is organized as follows: Section 2 reviews earlier findings on the relationship between teacher quality and student achievement; Section 3 specifies the structural model of the teacher selection and student achievement process, reviews the measures of student and teacher achievement and other empirical data, and discusses statistical estimation issues resulting from incomplete data on some variables in the model; Section 4 presents and interprets the statistical estimation results, and Section 5 concludes.

2 Earlier and Related Studies on the Effect of Teacher Quality on Student Achievement

Sanders (1996) and more recently Rivkin, Hanushek and Kain (2005), document through micro-econometric estimation that some teachers have large and statistically significant effects on student learning outcomes; however, what in particular about such successful teachers explains positive student learning outcomes remains unknown. Generally, years of teacher education and teacher experience, themselves, explain relatively little of observed variations on reading and mathematics outcomes.6

There is a small academic literature on the effect of teacher quality, as measured by standardized teacher test scores, and substantive or content preparation on student performance in the US.

In an early study, Lins (1946) found with a sample of teachers in 27 classes that the correlation between average National Teacher Exam (NTE) scores and residual pupil gain scores was .45.

In an examination of the statistical relationship between NTE scores and student competency and student achievement in North Carolina, Strauss and Sawyer (1986) found very strong evidence of a sizable link between core battery NTE test scores and 11th grade reading and math competency and achievement scores.7 In that study, a 1% relative increase in the average of core battery scores at the district level was associated with a 3 to 5% relative decline in the fraction of students who fell below grade level in reading and math; this result was after controlling for ethnicity, student teacher ratio, college going plans, and per capita income of the school district.

Webster (1988) found a significant relationship between teachers’ scores on the Wesman Personnel Classification test, a test of verbal and quantitative ability, and middle school students’ scores on the Iowa Tests of Basic Skills.

Loadman and Deville (1990) demonstrated a stronger relationship between ACT scores and NTE, then between GPA and NTE. One interpretation of this empirical relationship is that teacher preparation institutions may not be adding particular value through approved courses of studies.

Ferguson (1991) found a similar relationship, although not as large, between

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6Rivkin, Hanushek and Kain (2005, p. 417). See also Zumwalt and Craig (2005) for a broad review of the peer reviewed literature on teacher’s characteristics and student learning outcomes.

7See Strauss and Sawyer (1986).
measures of teacher quality and student achievement in Texas, and Ferguson and Ladd (1996) found similar relationships in Alabama.

Monk and King (1995) investigated the effects of subject-specific teacher preparation on student performance in secondary math and science. They find that students whose sophomore-year teacher possessed relatively high levels of subject-matter preparation in mathematics (more than 9 mathematics courses) scored significantly higher than corresponding juniors whose sophomore-year teacher possessed relatively low levels of subject-matter preparation. One more semester of a mathematics course translated to a 1.5 percent improvement in performance, independent of the student's initial pretest score.\(^8\)

Sanders (1996) found that students who scored at the same level on mathematics tests in third grade were separated subsequently by differences of as much as 50 percentage points on sixth grade tests depending on the quality of the teachers to whom they were assigned. Rivkin, Hanushek and Kain (2005) found from a very careful analysis of Texas panel data that "...teachers have powerful effects on reading and mathematics achievement, though little of the variation in teacher quality is explained by observable characteristics such as education or experience."\(^9\)

Our model of the relationship between teacher characteristics and student achievement follows the typical cross-sectional production function model at the district level to take advantage of unique information about the teacher selection process in Pennsylvania, and to re-examine earlier results of Strauss and Sawyer (1986) for North Carolina district level student achievement information.

Strauss and Sawyer (1986) specify and estimate a relationship in which student achievement depends on various measures of factor quality and intensity: average National Teacher Exam scores which was the combined score for general and pedagogical knowledge at the district level, student teacher ratio, insured capital per student, percent of the student body non-white, and fraction of the student body with post-secondary educational plans. Spending per capita is not included in such a specification because it is viewed as a monotonic transformation of input quantities already specified. Note that if input prices are uniform across districts, then multi-collinearity will result in the estimation process.

Strauss and Sawyer estimated:

\[
\text{Achievement} = \gamma_1 + \gamma_2 \frac{NTE}{Students} + \gamma_3 \frac{Capital}{Students} + \gamma_4 \frac{Students}{Teachers} + \gamma_5 \%\text{College Going} + \gamma_6 \%\text{Nonwhite} + \nu_1 \quad (1)
\]

Additionally, we shall account for the teacher selection process and resulting insularity (or nepotism) in the hiring process reported in Strauss, Bowes, Marks and Plesko (2000). That 2 equation model specified that the fraction of teachers employed in a district who graduated high school in that district, taken to be a measure of hiring insularity, is a function of the unemployment rate, and the

\(^8\)Monk and King (1995, p. 46)  
level of educational attainment in the district. Student achievement in turn depends on the level of insularity, and measures of student poverty and general educational attainment of population:

\[
\text{Insularity} = \gamma_6 + \gamma_7 \text{Urate} + \gamma_8 \%BA + \nu_2 \tag{2}
\]

\[
\text{Achievement} = \gamma_9 + \gamma_{10} \text{Insularity} + \gamma_{11} \%BA + \gamma_{12} \%AFDC + \nu_3 \tag{3}
\]

3 Model, Empirical Measures, and Estimation Considerations

3.1 A Model of Employment and Teacher and Student Achievement

For this study, we combine the considerations from the modeling of the hiring decision and educational production function literature in a three equation model of the teacher hiring, teacher quality, and student achievement process. The model we develop is at the district level and parallels the data that we have available to test the model.

In our first equation, districts choose how insular a hiring process to pursue. We measure insularity by the percentage of a district’s teachers who received their high school credential from that district. The idea is that district boards and administrators are, in part, pursuing personal and political goals via the hiring process and that their ability to do this is constrained by voter monitoring and by the costs of their actions. Teaching jobs will be a more valuable commodity in poor districts with high unemployment, so that we should see boards more motivated to distribute these jobs on other-than-merit bases in such districts. Districts in which parents are better able or more willing to monitor board actions should have less scope to be insular. Districts which have a broader pool of applicants will find it more costly in terms of “opportunity quality” to pursue insular policies, so that these districts should be less insular. Finally, rural districts may be more insular simply because they find it more difficult to attract candidates (and the candidates they do attract are more likely to be attached to the district already).

Our second equation examines the quality of employed teachers, as measured by median General Knowledge and Professional Knowledge test scores in the district of those who took the National Teacher Examination. Quality is modeled as a function of the number of schools of education in the county as a proxy for the general level of supply, the unemployment rate, and the general educational background of the population. We expect that as the level of insularity and unemployment goes up in the district, the general level of teacher quality will decline as non-academic considerations dominate the hiring decision. We would expect that as the general level of educational attainment rises in the district, the general quality of the teachers hired would rise, and that as the
number of education schools in the area rises, there will be more and higher quality teachers to choose among by hiring districts.

Our third equation models student achievement as a function of teacher quality and other factors. We expect student achievement to rise with the general educational attainment of the population, fall as poverty increases, and rise with various measures of teacher quality e.g. be positively related to higher median General and Professional Knowledge test scores.

The structural model thus is:

\[ \text{Inshr} = X_1 \beta_1 + \epsilon_1 \] (4)
\[ *\text{Kn} = \rho_1 \text{Inshr} + X_2 \beta_2 + \epsilon_2 \] (5)
\[ \text{Achvm} = \rho_2 (*\text{Kn}) + X_3 \beta_3 + \epsilon_3 \] (6)

The presentation above is somewhat unusual in our use of "*Kn" to denote either Professional Knowledge, General Knowledge or both.\(^{10}\) When we estimate our structural model, we estimate it three ways. First, we estimate the system as a three equation model with General Knowledge as our measure of teacher quality: that is we estimate (4)-(6) with GenKn replacing *Kn. Second, we estimate the system as a three equation model with Professional Knowledge as our measure of teacher quality: that is we estimate (4)-(6) with PrfKn replacing *Kn. Third, we estimate the system as a four equation model, with two separate equations similar to equation 5, one each for General and Professional Knowledge and with both quality measures in equation 6.

Note that since the quality of teacher hires is endogenous, we must estimate the model using systems estimation techniques. The estimation problem is complicated by the fact that we do not have data on all 501 school districts in Pennsylvania for equations (4)-(6).

3.2 Empirical Measures

Data to estimate the above structural models by Pennsylvania school district come from a variety of sources in Pennsylvania. Because we seek to link the effects of the teacher selection process to student learning outcomes, as well as to examine the differential impact of general vs. professional knowledge on student learning outcomes, and most of such data are only available once at the district level, we estimate a cross-sectional set of equations for Pennsylvania school districts in the mid 1990's. While there may be risk in our approach of aggregation bias, as discussed in Hanushek, Rivkin and Taylor(1996), by utilizing district

\(^{10}\)The National Teacher Examination, now succeeded by the Praxis test series, was developed by Educational Testing Service of Princeton, New Jersey to measure certain core skills that all teachers were expected to demonstrate, and specialized skills. The General Knowledge component of the core battery sought to measure the general literacy of a prospective teacher, while the Professional Knowledge component sought to measure, on a written basis, what the prospective teacher knew about pedagogical methods and general psychology.
Table 1: Variable Descriptions

<table>
<thead>
<tr>
<th>Variable</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Inslr</td>
<td>Insularity: the natural log of the % of teachers who graduated from the same district</td>
</tr>
<tr>
<td>GenKn</td>
<td>General Knowledge: the natural log of the mean score of district teachers on General Knowledge portion of National Teacher Examination</td>
</tr>
<tr>
<td>PrfKn</td>
<td>Professional Knowledge: the natural log of the mean score of district teachers on Professional Knowledge portion of National Teacher Examination</td>
</tr>
<tr>
<td>Achvm</td>
<td>Achievement: the natural log of the first principal factor of achievement test scores in the district</td>
</tr>
<tr>
<td>Urate</td>
<td>Unemployment: the natural log of the unemployment rate</td>
</tr>
<tr>
<td>BApct</td>
<td>Parents’ Schooling: the natural log of the percent of school district residents who have at least a bachelor’s degree</td>
</tr>
<tr>
<td>Edsch</td>
<td>Education Schools: the number of schools of education in the same county as the district</td>
</tr>
<tr>
<td>Prprl</td>
<td>Rural: the proportion of the district’s population who live in rural areas.</td>
</tr>
<tr>
<td>Afdc</td>
<td>Parents’ Poverty: the natural log of the percentage of the district’s population which received AFDC.</td>
</tr>
</tbody>
</table>

Table 2: Descriptive Statistics

<table>
<thead>
<tr>
<th>Variable</th>
<th>Mean</th>
<th>Std Dev</th>
<th>25%</th>
<th>75%</th>
<th>N</th>
</tr>
</thead>
<tbody>
<tr>
<td>Inslr</td>
<td>3.34</td>
<td>0.94</td>
<td>2.94</td>
<td>3.91</td>
<td>209</td>
</tr>
<tr>
<td>GenKn</td>
<td>6.50</td>
<td>0.01</td>
<td>6.49</td>
<td>6.50</td>
<td>487</td>
</tr>
<tr>
<td>PrfKn</td>
<td>6.50</td>
<td>0.01</td>
<td>6.50</td>
<td>6.50</td>
<td>487</td>
</tr>
<tr>
<td>Achvm</td>
<td>7.76</td>
<td>0.06</td>
<td>7.73</td>
<td>7.80</td>
<td>487</td>
</tr>
<tr>
<td>Urate</td>
<td>1.68</td>
<td>0.47</td>
<td>1.31</td>
<td>2.03</td>
<td>487</td>
</tr>
<tr>
<td>BApct</td>
<td>2.51</td>
<td>0.53</td>
<td>2.11</td>
<td>2.82</td>
<td>487</td>
</tr>
<tr>
<td>Edsch</td>
<td>2.71</td>
<td>2.91</td>
<td>0.00</td>
<td>4.00</td>
<td>487</td>
</tr>
<tr>
<td>Prprl</td>
<td>0.52</td>
<td>0.39</td>
<td>0.09</td>
<td>1.00</td>
<td>487</td>
</tr>
<tr>
<td>Afdc</td>
<td>1.49</td>
<td>1.08</td>
<td>0.74</td>
<td>2.25</td>
<td>487</td>
</tr>
</tbody>
</table>
level data in one state, and account for endogeneity in our model, especially the hiring decision, and investigate our specification using both OLS and system techniques, and perform extensive tests below of robustness for other variables often used in production studies, it is not obvious that aggregation bias is large nor is the direction of the bias evident in our results below.\textsuperscript{11}

*School District Insularity in hiring process: Instr.* This is measured by percentage of employed teachers in 1996-7 who obtained their high school diploma from that high school as reported to a special survey conducted by the Pennsylvania State Board of Education in July, 1997;

*Teacher Quality by school district of employment: GenK\textsubscript{n}, PrfK\textsubscript{n} The two teacher quality measures are median teacher test scores on Educational Testing Service's National Teacher Exam core battery tests for General Knowledge and Professional Knowledge. The scores ranged from 250 to 990.\textsuperscript{12} Since 1987, the Pennsylvania Department of Education has required anyone aspiring to be certified as a school teacher to pass ETS core and specialized tests. The NTE exams have been used since 1940 to assess the knowledge of prospective teachers in many states. They were first administered by the American Council on Education, and in 1950 became the responsibility of ETS. The NTE contained common or core examinations in professional education and general education.\textsuperscript{13} The General Knowledge examination measures general background knowledge while the Professional Knowledge measures knowledge about pedagogy and general psychology. The median score was calculated from 98,392 unique individual test results\textsuperscript{14} for any teacher who took the examinations between 1990 and 1997, and who was employed by a public school district in Pennsylvania during the period 1990-1999. The median was calculated across 1990-99 for each district, and weighted by the number of years the teacher was in the district. During this period, classroom employment statewide averaged about 105,000, and by 1999, there were NTE scores for 19\% of employed classroom teachers.

*Unemployment Rate: Urate* The unemployment rate by school district as tabulated and reported by the 1995 edition of the Pennsylvania Educational Policy data base, maintained at the University of Pittsburgh.

*Percentage of the Adult Population in 1990 with a bachelor's degree or more as reported in the 1990 Census of Population and tabulated at the school district level: BApct.*

*Number of schools of education in same county as school district: Edsch.* Authors' tabulation by county of 1997 list of approved programs in teacher preparation.

\textsuperscript{11}See Grunfeld and Griliches[1960] further on this.

\textsuperscript{12}Since there is no penalty for guessing in the NTE, the historical passing score of 540, set by the Pennsylvania Department of Education, implied that anyone correctly answering 39\% of the questions of average difficulty passed the test and thus be permitted to be hired by a local school district.

\textsuperscript{13}See Quirk, Witten and Weinberg[1973].

\textsuperscript{14}Some prospective teachers took the NTE General Knowledge and Professional Knowledge examinations more than once, and the highest score was used.
Percent of 1990 Population living in areas of 50,000 or more population in school district: Prk

Percentage of school age children in families receiving cash assistance in each school district: Afic Collected by the Pennsylvania Department of Education in conjunction with administering 1995 student achievement tests.

Composite measure of academic achievement and competency by school district: Achcm This measure is the result of applying factor analysis to a variety of student achievement (1995) and competency test (1990) results by school district in Pennsylvania since 1989. Both the competency and achievement tests are for reading and mathematics for grade school, middle school and high school. Twelve scores per district are summarized in this composite measure. In particular, we utilized achievement test scores in reading and math taken in 1998 at the 5th, 8th, and 11th grade levels (6 measures total). In addition, we utilized competency tests taken in 1991 at the 3rd, 5th, and 8th grade levels also in reading and math (6 measures total). The data we have for the competency tests is the percentage of students who failed. For our student achievement measure, we use the first principal factor of these twelve scores. The factor loadings were quite intuitive. The achievement test scores all received positive loadings and the competency test scores all received negative loadings.\(^\text{15}\)

### 3.3 Statistical Estimation Considerations

Typically, one would estimate (4)-(6) via three-stage least squares. Denoting \(Y\) as the stacked left-hand-side variables, \(X\) as a block diagonal matrix with \(X_1, X_2, X_3\) on the block diagonals, \(\beta\) as the \(\beta_i\) and \(\rho_i\) stacked, \(\Sigma\) is the variance-covariance matrix of the stacked error terms, and \(W\) as the matrix of instruments, the 3SLS estimate is:

\[
\hat{\beta}_{3SLS} = \left(X'\hat{\Sigma}^{-1/2} P_W \hat{\Sigma}^{-1/2} X\right)^{-1} X'\hat{\Sigma}^{-1/2} P_W \hat{\Sigma}^{-1/2} Y
\]

(7)

where \(P_W = \hat{\Sigma}^{-1/2} W \left(W'\hat{\Sigma}^{-1} W\right)^{-1} W'\hat{\Sigma}^{-1/2}\).

In the usual 3SLS setup, there are an equal number of observations per equation. This, along with the assumption that the error terms are homoscedastic and uncorrelated across observations but freely heteroscedastic and correlated within observations leads to the error structure \(\Sigma = \Omega \otimes I\). An estimate of \(\Sigma\) is then formed by estimating \(\Omega\) from residuals in the obvious way, after performing 2SLS equation-by-equation.

We cannot simply use equation 7 in the usual way to perform our estimation because our system of equations is “unbalanced.” There are only 209 observations with usable data on all analysis variables. Most of the problems arise due

\(^{15}\)The factor loadings were: 5th grade reading achievement (0.301), 8th grade reading achievement (0.320), 11th grade reading achievement (0.307), 5th grade math achievement (0.315), 8th grade math achievement (0.330), 13th grade math achievement (0.263), 3rd grade reading (in)competency (-0.274), 5th grade reading (in)competency (-0.201), 8th grade reading (in)competency (-0.277), 3rd grade math (in)competency (-0.259), 5th grade math (in)competency (-0.255), and 8th grade math (in)competency (-0.278).
to missing values for Inslr. Many school districts did not report their insularity. Were there not to be missing values for Inslr, there would be 487 useful observations. One tack we could take in our estimation would be to drop the observations with missing Inslr entirely, and use 3SLS in a straightforward manner. We did pursue this strategy for some of our robustness checks in section 4.2, and our baseline estimation of equations 4 through 6 using only the 209 observations does appear there. However, this procedure amounts to throwing away a lot of potentially useful data. We have all the necessary data to estimate equation 6 using 487 observations, and we have 487 observations on every variable save Inslr in equation 5.

We pursue a strategy designed to use this information. First, notice that the utility of the estimator in equation 7 depends in no way upon having an equal number of observations per equation. Only $\Sigma = \Omega \otimes I$ depends on this assumption. With different numbers of observations per equation, the formula for getting $\Sigma$ from $\Omega$ is merely uglier and the calculation more tedious. It is relatively straightforward to use 209 observations on equations 4 and 5 and 487 observations on equation 6. While no “canned” statistical package that we know of can handle the problem, utilizing a matrix programming language the task is not too difficult. Even this strategy throws away some useful observations, however. We would be using only 209 observations on equation 5 when we almost have enough information to use all 487 — only Inslr is missing.

To be able to use all 487 observations on equation 5 we pursue the following strategy. First, observe that we can substitute equation 4 into equation 5 to get:

$$ *\text{Kn} = \rho_1 (X_1 \hat{\beta}_1) + X_2 \beta_2 + \epsilon_2 + \rho_1 \epsilon_1 $$

(8)

If we have consistent estimates of $\beta_1$ in hand, we can construct $X_1 \hat{\beta}_1$ for the observations which have missing Inslr and use equation 8 in place of equation 5 in the estimation. This introduces two distinct additional complexities. First, the $\Sigma$ matrix is rendered even more complex. Now, the covariance between the error in the achievement equation and the error in the $*\text{Kn}$ equation is $\Omega_{23}$ for observations in which Inslr is not missing but $\Omega_{23} + \rho_1 \Omega_{13}$ for observations for which Inslr is missing (since the error term for equation 8 is different from the error term for equation 5. Of course, the variance term for the $*\text{Kn}$ equation is similarly affected. The second issue which arises is that $X_1 \hat{\beta}_1$ is an estimated quantity: it is not equal to the correct right-hand-side variable $X_1 \beta_1$. This means that the standard errors of the estimates must be corrected, as described in Pagan (1984). In our main results reported later, we use this strategy along with the corrections to $\Sigma$ and the standard errors of the $\hat{\beta}_1$. To begin the process, we need consistent estimates of $\beta_1$, and these can be obtained via OLS on equation 4. To summarize our estimation procedure:

1. We estimate equation 4 by OLS, yielding consistent estimates of $\beta_1$.
2. We construct $X_1 \hat{\beta}_1$. 

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3. We run 2SLS on equations 5 (using only 209 obs) and 6 to get consistent estimates of $\beta_2$ and $\beta_3$.

4. We use the residuals from the three above regressions to estimate $\Omega$.

5. We construct the complicated $\Sigma$ taking account of the facts we have 209 observations on the Inslr equation, 487 observations on the $^{*}K_n$ equation, 487 observations on the achvm equation, and that for 276 observations on the $^{*}K_n$ equation we are using equation 8 and for the other 209 we are using equation 5.

6. We apply equation 7 to get the 3SLS estimator.

7. We calculate the variance of our estimator using Pagan’s(1984) methods.

The above procedure produces consistent estimates of parameters and variance matrix as long as the selection of which observations are present for the variable Inslr is random (i.e. independent of the errors in the equations). If the selection is non-random, our estimates will be biased. We explore the possibility of selection in Section 4.3. We find that there is not compelling evidence that there is economically significant selection in our data, so we do not make an effort to address this problem further.

4 Estimation Results

4.1 Basic Results

We estimate the relationship between student achievement and teacher quality in several steps. First, we estimate reduced form equations for the three endogenous variables (Inslr, GenKn and PrfKn), and our index measure of student achievement (Achvm). Second, we estimate our structural equations without taking into account endogeneity through the use of ordinary least squares (OLS). Third, we estimate our system model with General Knowledge as the key explanatory variable, and then, separately, Professional Knowledge as the key explanatory variable. Finally, we estimate our system model with General Knowledge and Professional Knowledge both specified as endogenous and simultaneously estimated. Table 3 - 7 contain this sequence of estimation results.

Table 3 contains the reduced form estimates for the structural system (either the three or four equation variant) formed by (4)-(6). Each of the regressions is highly significant, although multicollinearity renders many of the individual parameter estimates insignificant at conventional levels. At point estimates, all of the exogenous variables in the insularity equation (3.1) have the expected sign except for the proportion rural, and the coefficient estimate for number of schools of education in the county is individually highly significant. In the teacher quality regressions, all of the coefficients have reasonable signs except for the negative coefficient on number of schools of education in the General Knowledge equation. In the quality equations, poverty is significant at conventional levels in both equations as are percent of the population with a bachelor’s
Table 3: Reduced form equations and (standard errors)

<table>
<thead>
<tr>
<th>eq.</th>
<th>(3.1)</th>
<th>(3.2)</th>
<th>(3.3)</th>
<th>(3.4)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Inslr</td>
<td>GenKn</td>
<td>PrfKn</td>
<td>Achvm</td>
</tr>
<tr>
<td>const</td>
<td>3.441</td>
<td>6.49773</td>
<td>6.49679</td>
<td>7.640</td>
</tr>
<tr>
<td></td>
<td>(0.657)</td>
<td>(0.00365)</td>
<td>(0.00289)</td>
<td>(0.017)</td>
</tr>
<tr>
<td>Urate</td>
<td>0.237</td>
<td>-0.00183</td>
<td>-0.00143</td>
<td>-0.003</td>
</tr>
<tr>
<td></td>
<td>(0.233)</td>
<td>(0.00121)</td>
<td>(0.00096)</td>
<td>(0.006)</td>
</tr>
<tr>
<td>BApct</td>
<td>-0.168</td>
<td>0.00156</td>
<td>0.00216</td>
<td>0.0060</td>
</tr>
<tr>
<td></td>
<td>(0.178)</td>
<td>(0.00080)</td>
<td>(0.00079)</td>
<td>(0.005)</td>
</tr>
<tr>
<td>Edsch</td>
<td>-0.738</td>
<td>-0.00019</td>
<td>0.00004</td>
<td>-0.001</td>
</tr>
<tr>
<td></td>
<td>(0.030)</td>
<td>(0.00015)</td>
<td>(0.00012)</td>
<td>(0.001)</td>
</tr>
<tr>
<td>Prprl</td>
<td>-0.169</td>
<td>0.00144</td>
<td>0.00022</td>
<td>0.025</td>
</tr>
<tr>
<td></td>
<td>(0.229)</td>
<td>(0.00115)</td>
<td>(0.00091)</td>
<td>(0.006)</td>
</tr>
<tr>
<td>Afle</td>
<td>0.110</td>
<td>-0.00039</td>
<td>-0.00085</td>
<td>-0.022</td>
</tr>
<tr>
<td></td>
<td>(0.115)</td>
<td>(0.00055)</td>
<td>(0.00013)</td>
<td>(0.003)</td>
</tr>
<tr>
<td>N</td>
<td>209</td>
<td>487</td>
<td>487</td>
<td>487</td>
</tr>
<tr>
<td>(R^2)</td>
<td>0.154</td>
<td>0.089</td>
<td>0.154</td>
<td>0.652</td>
</tr>
</tbody>
</table>
Table 4: Structural Equations and (standard errors), by OLS

<table>
<thead>
<tr>
<th>eq:</th>
<th>(4.1)</th>
<th>(4.2)</th>
<th>(4.3)</th>
<th>(4.4)</th>
<th>(4.5)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>GenKn</td>
<td>PrfKn</td>
<td>Achvm</td>
<td>Achvm</td>
<td>Achvm</td>
</tr>
<tr>
<td>const</td>
<td>6.498</td>
<td>6.495</td>
<td>3.090</td>
<td>7.286</td>
<td>4.928</td>
</tr>
<tr>
<td></td>
<td>(0.005)</td>
<td>(0.001)</td>
<td>(1.432)</td>
<td>(1.830)</td>
<td>(1.929)</td>
</tr>
</tbody>
</table>
| Inshr | $-2.63 \times 10^{-4}$ | $1.98 \times 10^{-4}$ | \[
\begin{array}{c}
6.28 \times 10^{-4} \\
(4.82 \times 10^{-4})
\end{array}
\] | \[
\begin{array}{c}
6.28 \times 10^{-4} \\
(4.82 \times 10^{-4})
\end{array}
\] |
| GenKn | 0.71 | \[
\begin{array}{c}
(0.22) \\
(0.218)
\end{array}
\] |
| PrfKn | 0.063 | \[
\begin{array}{c}
(0.282) \\
(0.314)
\end{array}
\] |
| Urate | $-2.37 \times 10^{-3}$ | $-2.53 \times 10^{-3}$ | \[
\begin{array}{c}
1.39 \times 10^{-3} \\
(1.07 \times 10^{-3})
\end{array}
\] | \[
\begin{array}{c}
1.39 \times 10^{-3} \\
(1.07 \times 10^{-3})
\end{array}
\] |
| BApct | 2.19 $\times 10^{-3}$ | 2.94 $\times 10^{-3}$ | 0.043 | 0.043 | 0.044 |
|       | \[
\begin{array}{c}
1.41 \times 10^{-3} \\
(1.08 \times 10^{-3})
\end{array}
\] | \[
\begin{array}{c}
1.41 \times 10^{-3} \\
(1.08 \times 10^{-3})
\end{array}
\] | \[
\begin{array}{c}
(0.001) \\
(0.001)
\end{array}
\] | \[
\begin{array}{c}
(0.001) \\
(0.001)
\end{array}
\] | \[
\begin{array}{c}
(0.001) \\
(0.001)
\end{array}
\] |
| Edsch | $-4.83 \times 10^{-4}$ | $-1.19 \times 10^{-4}$ | \[
\begin{array}{c}
2.52 \times 10^{-4} \\
(1.93 \times 10^{-4})
\end{array}
\] | \[
\begin{array}{c}
2.52 \times 10^{-4} \\
(1.93 \times 10^{-4})
\end{array}
\] |
| Afdc | $-0.026$ | $-0.027$ | \[
\begin{array}{c}
(0.002) \\
(0.002)
\end{array}
\] | \[
\begin{array}{c}
(0.002) \\
(0.002)
\end{array}
\] | \[
\begin{array}{c}
(0.002) \\
(0.002)
\end{array}
\] |
| N | 209 | 209 | 487 | 487 | 487 |
| $R^2$ | 0.0573 | 0.1285 | 0.6374 | 0.6296 | 0.6389 |
Table 5: Structural Equations: Insularity, General Knowledge and Achievement

<table>
<thead>
<tr>
<th>eq:</th>
<th>5.1 (Insr)</th>
<th>5.2 (GenKn)</th>
<th>5.3 (Achvm)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Insr</td>
<td>GenKn</td>
<td>Achvm</td>
</tr>
<tr>
<td>const</td>
<td>3.882 (0.412)</td>
<td>11.417 (0.004)</td>
<td>-57.755 (0.023)</td>
</tr>
<tr>
<td>Insr</td>
<td>-0.012 (0.005)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>GenKn</td>
<td></td>
<td>10.070 (4.579)</td>
<td></td>
</tr>
<tr>
<td>Urate</td>
<td>0.081 (0.137)</td>
<td>$2.00 \times 10^{-3}$ (2.22 $\times 10^{-3}$)</td>
<td></td>
</tr>
<tr>
<td>BApct</td>
<td>$-0.238$ (0.117)</td>
<td>$-3.06 \times 10^{-4}$ (1.53 $\times 10^{-4}$)</td>
<td>0.039 (0.007)</td>
</tr>
<tr>
<td>Edsch</td>
<td>$-0.071$ (0.015)</td>
<td>$-9.72 \times 10^{-4}$ (3.69 $\times 10^{-4}$)</td>
<td></td>
</tr>
<tr>
<td>Prprl</td>
<td>$-0.242$ (0.188)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Afdc</td>
<td>0.147 (0.081)</td>
<td></td>
<td>-0.008 (0.009)</td>
</tr>
</tbody>
</table>
Table 6: Structural Equations, Professional Knowledge

<table>
<thead>
<tr>
<th>eq:</th>
<th>6.1</th>
<th>6.2</th>
<th>6.3</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Instr</td>
<td>PrfKn</td>
<td>Achvm</td>
</tr>
<tr>
<td>const</td>
<td>3.425 (0.475)</td>
<td>6.510 (0.003)</td>
<td>-0.074 (0.020)</td>
</tr>
<tr>
<td>Instr</td>
<td>$-3.83 \times 10^{-3}$ (2.81 $\times 10^{-3}$)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>PrfKn</td>
<td></td>
<td>-1.184 (3.905)</td>
<td></td>
</tr>
<tr>
<td>Urate</td>
<td>0.027 (0.166)</td>
<td>$-1.25 \times 10^{-3}$ (1.45 $\times 10^{-3}$)</td>
<td></td>
</tr>
<tr>
<td>BApct</td>
<td>$-0.131$ (0.129)</td>
<td>$1.50 \times 10^{-3}$ (0.87 $\times 10^{-3}$)</td>
<td>0.046 (0.010)</td>
</tr>
<tr>
<td>Edsch</td>
<td>$-0.060$ (0.020)</td>
<td>$-1.56 \times 10^{-4}$ (2.03 $\times 10^{-4}$)</td>
<td></td>
</tr>
<tr>
<td>Prprl</td>
<td>$-0.005$ (0.174)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Aflc</td>
<td>0.231 (0.084)</td>
<td></td>
<td>-0.028 (0.005)</td>
</tr>
</tbody>
</table>
Table 7: Structural Equations, Both Knowledge Measures

<table>
<thead>
<tr>
<th>eq.</th>
<th>Instr</th>
<th>GenKn</th>
<th>PrfKn</th>
<th>Achym</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>(0.392)</td>
<td>(0.005)</td>
<td>(0.003)</td>
<td>(0.043)</td>
</tr>
<tr>
<td>Instr</td>
<td></td>
<td>-0.011</td>
<td>-3.95 x 10^{-3}</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>(0.005)</td>
<td>(3.03 x 10^{-4})</td>
<td></td>
</tr>
<tr>
<td>GenKn</td>
<td></td>
<td></td>
<td>12.661</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>(4.638)</td>
<td></td>
</tr>
<tr>
<td>PrfKn</td>
<td></td>
<td></td>
<td>-5.432</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>(6.232)</td>
<td></td>
</tr>
<tr>
<td>Urate</td>
<td>0.036</td>
<td>1.31 x 10^{-3}</td>
<td>-1.34 x 10^{-3}</td>
<td></td>
</tr>
<tr>
<td></td>
<td>(0.132)</td>
<td>(2.50 x 10^{-3})</td>
<td>(2.50 x 10^{-3})</td>
<td></td>
</tr>
<tr>
<td>BApct</td>
<td>-0.211</td>
<td>-6.09 x 10^{-4}</td>
<td>1.65 x 10^{-3}</td>
<td>0.055</td>
</tr>
<tr>
<td></td>
<td>(0.109)</td>
<td>(15.02 x 10^{-4})</td>
<td>(0.91 x 10^{-3})</td>
<td>(0.020)</td>
</tr>
<tr>
<td>Edsch</td>
<td>-0.067</td>
<td>-8.65 x 10^{-4}</td>
<td>-2.44 x 10^{-4}</td>
<td></td>
</tr>
<tr>
<td></td>
<td>(0.016)</td>
<td>(3.78 x 10^{-4})</td>
<td>(2.19 x 10^{-4})</td>
<td></td>
</tr>
<tr>
<td>Prprl</td>
<td>-0.166</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>(0.364)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Afdc</td>
<td>0.184</td>
<td></td>
<td>-0.011</td>
<td></td>
</tr>
<tr>
<td></td>
<td>(0.073)</td>
<td></td>
<td>(0.011)</td>
<td></td>
</tr>
</tbody>
</table>

17
degree and unemployment in the Professional Knowledge equation. The pattern of signs in the achievement equation is also as expected, with the exception of the negative sign on number of schools of education. In this equation, poverty and proportion rural are individually significant at conventional levels.

Table 4 contains estimates of our structural model by ordinary least squares. Obviously, these estimates ignore the endogeneity of insularity and teacher quality. The results are interesting nevertheless. No effect of insularity on teacher quality can be seen here, but the effect of teacher quality on achievement appears. General Knowledge affects achievement positively both when it is entered alone and when it is entered with Professional Knowledge. The elasticity of this effect is 0.71 when entered alone and 0.87 when entered with Professional Knowledge. Professional Knowledge does not have a significant effect either alone or with General Knowledge. At point estimates, Professional Knowledge has a small positive effect when entered alone and a small negative effect when entered with General Knowledge.

Structural models estimated by 3SLS as described above appear in Table 5 and Table 6. The former uses General Knowledge as the (sole) measure of teacher quality, while the latter uses Professional Knowledge. In the case of the General Knowledge specification of Table 5, estimates are quite consistent with our story. Insularity leads to lower teacher quality and lower teacher quality leads to lower student achievement. Both of these effects are significant at conventional levels and the effect sizes are quite large, with the elasticity of student achievement with respect to teacher quality estimated to be 10.

In the case of the Professional Knowledge specification of teacher quality of Table 6, the results are less consistent with expectations. Insularity has little or no estimated effect on teacher quality and teacher quality has no or perhaps a negative effect on student achievement.

Our preferred specification appears in Table 7. This table contains estimates from the four equation model in which we allow for teacher quality to be measured by either Professional or General Knowledge. It is also estimated by the 3SLS technique discussed above. These results largely echo those reported in Table 5 and Table 6. Insularity negatively and significantly affects teacher quality as measured by General or Professional Knowledge. Teacher quality as measured by General Knowledge but not as measured by Professional Knowledge positively and significantly affects student achievement. The estimated elasticity of student achievement with respect to General Knowledge is 12.7 while the estimated elasticity of student achievement with respect to Professional Knowledge is -5.4.

4.2 Robustness

Our specification of the achievement equation, equation 6, is fairly narrow. Other authors have used a number of additional variables to explain achievement. If we have omitted relevant variables and these relevant variables are

\[ \text{The equation for insularity is omitted as it is just the same as equation (3.1).} \]
correlated with our instruments, then our results could be biased as a result. In this section, we check for such biases by running our model with a number of additional variables included.

It is easy to think of reasons why any number of additional variables should be included in our models. In addition, there are no strong theoretical reasons for preferring any particular set of additional control variables. In these circumstances, a reader may be worried that our results are sensitive to our choice of control variables and even that we have engaged in a specific search in order to produce our results. To allay these concerns, we follow a line of recent papers (c.f. Learner, 1983; Sala-I-Martin, 1997) which address this issue by systematically running a great many different regressions including different subsets of the control variables in order to test the robustness of a variable of interest. We use a similar approach.

First, consider our results from running OLS on our structural equations, column 4.5 of Table 4. Consider the equation:

\[ \text{Achvm} = \beta_1 + \beta_2 \text{GenKn} + \beta_3 \text{PrfKn} \]

\[ + \beta_4 \text{BA}pct + \beta_5 \text{Afde} + \text{Controls} \]  

We estimate this equation repeatedly using different variables as controls. We consider all of the following six control variables: ratio of students to teachers, percent black, average enrollment (school size), per capita income, expenditures per student, and percent of teachers with a masters degree or more. We run one OLS regression for each possible combination of these controls, for \(2^6 = 64\) total regressions. In each regression, we keep track of the coefficients on log general knowledge and log professional knowledge.

The results of those 64 regressions are summarized in Table 8 in the final two columns. The column labelled “OLS General Knowledge” contains a summary

<table>
<thead>
<tr>
<th>Table 8: Robustness to Additional Variables, 3SLS and OLS</th>
</tr>
</thead>
<tbody>
<tr>
<td>Base Model Coefficient</td>
</tr>
<tr>
<td>------------------------</td>
</tr>
<tr>
<td>Number of Estimates</td>
</tr>
<tr>
<td>Mean Coefficient</td>
</tr>
<tr>
<td>Standard Deviation of Mean</td>
</tr>
<tr>
<td>% of Coefficients &gt; 0</td>
</tr>
<tr>
<td>% of Coefficients &lt; 0</td>
</tr>
<tr>
<td>% of t-statistics &gt; 2</td>
</tr>
<tr>
<td>% of t-statistics &lt; -2</td>
</tr>
</tbody>
</table>
of the results for the coefficient on general knowledge in equation 10. In the base model, the model with no extra control variables, the coefficient on general knowledge is equal to 0.87, and this matches the results in Table 4. Continuing down that column, over the 64 regressions run with the various combinations of additional control variables, the average value of the coefficient on general knowledge is 0.68 and the standard deviation of this coefficient over the various specifications is 0.17. All of general knowledge coefficients were positively significant.

The last column of Table 8 reports a summary of the estimated coefficients from the professional knowledge coefficient from equation 10. These coefficients average -0.32 (as opposed to -0.45 in the base model) and all are negatively significant.

For the full structural model, we repeatedly re-estimate the four equation system given at equation 6, including extra controls on each equation. Again, we keep track of the values of the coefficients on professional knowledge and general knowledge in the achievement equation. Our specification here is parallel to column 7.4 of Table 7, differing from that specification in that we include extra control variables on each equation. We use the same six control variables in the 3SLS case which we used in the OLS case, yielding 64 different possible combinations. However, since there are four equations in the system, there are $64^4$ or about 16.8 million estimations. This number was infeasible for us, so instead we always entered the same combination of covariates on each of the two equations in the system with profession or general knowledge on the left hand side. This reduces the number of possible combinations of control variables on each equation to $64^3 = 262,144$ estimations.

In the base 3SLS model, the elasticity of achievement with respect to general knowledge is 12.66. Over the 262,144 robustness estimations, the average general knowledge elasticity of achievement is 8.35. 89.3% of the estimations demonstrated a positive effect of general knowledge on achievement. About 53% of the estimations demonstrated a positive, significant effect and none of the estimations demonstrated a negative, significant effect.

By contrast, professional knowledge showed, on average, a -4.01 achievement elasticity (as opposed to -5.43 in the base model). Only about 32% of estimations showed a positive effect of professional knowledge on achievement, none of them significant, while about 68% of estimations showed a negative effect, with only a few of those significant.

These results show a fairly robust positive effect of general knowledge on achievement and no particularly robust effect of professional knowledge on achievement, although the point estimates were more often negative than positive. In all cases, the average effect of knowledge on achievement was, on average, of somewhat smaller magnitude in the regressions with extra controls than it was in our base models.
Table 9: Selection Effects: Sample Means

<table>
<thead>
<tr>
<th>Variable</th>
<th>reporters</th>
<th>non-reporters</th>
<th>difference</th>
<th>t statistic</th>
<th>P value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Urate</td>
<td>1.720</td>
<td>1.657</td>
<td>0.063</td>
<td>1.45</td>
<td>0.147</td>
</tr>
<tr>
<td></td>
<td>(0.487)</td>
<td>(0.461)</td>
<td>(0.472)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>BApct</td>
<td>2.449</td>
<td>2.549</td>
<td>-0.101</td>
<td>-2.09</td>
<td>0.037</td>
</tr>
<tr>
<td></td>
<td>(0.524)</td>
<td>(0.534)</td>
<td>(0.529)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Prprl</td>
<td>0.599</td>
<td>0.470</td>
<td>0.120</td>
<td>3.41</td>
<td>0.001</td>
</tr>
<tr>
<td></td>
<td>(0.372)</td>
<td>(0.397)</td>
<td>(0.386)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Afic</td>
<td>1.508</td>
<td>1.478</td>
<td>0.030</td>
<td>0.30</td>
<td>0.761</td>
</tr>
<tr>
<td></td>
<td>(1.050)</td>
<td>(1.102)</td>
<td>(1.080)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>GenKn</td>
<td>6.497</td>
<td>6.498</td>
<td>0.001</td>
<td>-0.77</td>
<td>0.440</td>
</tr>
<tr>
<td></td>
<td>(0.008)</td>
<td>(0.007)</td>
<td>(0.008)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>PrfKn</td>
<td>6.498</td>
<td>6.499</td>
<td>0.001</td>
<td>-1.32</td>
<td>0.189</td>
</tr>
<tr>
<td></td>
<td>(0.006)</td>
<td>(0.006)</td>
<td>(0.006)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Achvm</td>
<td>7.759</td>
<td>7.764</td>
<td>0.006</td>
<td>-0.83</td>
<td>0.405</td>
</tr>
<tr>
<td></td>
<td>(0.068)</td>
<td>(0.068)</td>
<td>(0.068)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>N</td>
<td>209</td>
<td>278</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

4.3 Selection

Nonrandom selection has long been understood to bias the coefficient estimates in linear models such as ours. Since we are using 209 out of an otherwise usable sample of 487 in equation 4 due to selective reporting of insularity, it is reasonable to be quite concerned about selectivity here. We address the problem in two ways. First, we look for non-random selection directly, by examining the differences in observable characteristics between reporters and non-reporters of insularity.

Table 9 presents a table of means of observables broken out by reporters of insularity and non-reporters. The differences between reporters and non-reporters are, for the most part, small. Non-reporting districts have about a 10% greater proportion of college graduate residents than do non-reporters. Also, non-reporters are considerably more likely to be rural. Interestingly, none of the more performance-oriented measures show a significant difference, either in the economic or statistical sense. Although there is some evidence here of non-random selection, it does not look very large.

We also estimated a logit model in which the left-hand-side variable was a dummy equal to one if the district was a non-reporter. In this regression, the only statistically significant variable (of Urate, BApct, Prprl, and Afic)
Table 10: Selection-Free 2 Equation Model

<table>
<thead>
<tr>
<th>Variable</th>
<th>GenKn</th>
<th>PrfKn</th>
<th>Achvm</th>
</tr>
</thead>
<tbody>
<tr>
<td>const</td>
<td>6.4962</td>
<td>6.4972</td>
<td>-1.912</td>
</tr>
<tr>
<td></td>
<td>(0.0035)</td>
<td>(0.0029)</td>
<td>(50.482)</td>
</tr>
<tr>
<td>GenKn</td>
<td></td>
<td></td>
<td>9.932</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>(4.120)</td>
</tr>
<tr>
<td>PrfKn</td>
<td></td>
<td></td>
<td>-8.460</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>(8.158)</td>
</tr>
<tr>
<td>Urate</td>
<td>-0.0016</td>
<td>-0.0015</td>
<td></td>
</tr>
<tr>
<td></td>
<td>(0.0012)</td>
<td>(0.0010)</td>
<td></td>
</tr>
<tr>
<td>BApct</td>
<td>0.0018</td>
<td>0.0021</td>
<td>0.059</td>
</tr>
<tr>
<td></td>
<td>(0.0010)</td>
<td>(0.0008)</td>
<td>(0.021)</td>
</tr>
<tr>
<td>Edsch</td>
<td>-0.0001</td>
<td>0.0000</td>
<td></td>
</tr>
<tr>
<td></td>
<td>(0.0001)</td>
<td>(0.0001)</td>
<td></td>
</tr>
<tr>
<td>Prprl</td>
<td>0.0022</td>
<td>0.0000</td>
<td></td>
</tr>
<tr>
<td></td>
<td>(0.0010)</td>
<td>(0.0009)</td>
<td></td>
</tr>
<tr>
<td>Afde</td>
<td>-0.0009</td>
<td>-0.0009</td>
<td>-0.020</td>
</tr>
<tr>
<td></td>
<td>(0.0005)</td>
<td>(0.0004)</td>
<td>(0.011)</td>
</tr>
</tbody>
</table>

was Prprl. It had a probability derivative (at sample means) of 0.002. So, a
one percentage point increase in the percent of a district’s population which
is located in a rural area raises the probability of reporting by 0.2 percentage
points. The logistic regression overall was significant at the 2% level. However,
the logistic regression did not do well at predicting whether a district reported.
The regression predicted correctly 58.9% of the time. Since 57.1% of the districts
did not report, one could achieve 57.1% correct predictions by simply predicting
non-reportage always.

For our second check of the importance of selection bias, we are able to
estimate a smaller model on the full sample even in the absence of observations
on insularity. Observe that we can substitute equation 4 into equation 5 to get
the two-equation (three-equation when we are including both types of knowledge
in equation 6) system:

\[ *Kn = X_4 \beta_4 + \epsilon_2 + \rho_1 \epsilon_1 \]  
\[ \text{Achvm} = \rho_2 (*Kn) + X_3 \beta_3 + \epsilon_3 \]
The matrix $X_4$ contains the "union" of elements from $X_1$ and $X_2$. The elements of $\beta_4$ are equal to the corresponding elements of $\rho_1 \beta_1$ for variables appearing only in equation 4. They are equal to the corresponding elements of $\beta_2$ for variables appearing only in equation 5. They are equal to $\rho_1 \beta_1 + \beta_2$ for variables appearing in both equations. Obviously, we will no longer be able separately to identify many of the $\beta_i$ and we will not be able separately to identify $\rho_1$. However, equations 11 and 12 can be estimated using all 487 observations, obviating selection issues. Furthermore, the most interesting parameters, $\rho_2$ are still identified and can be reported.

Results from this estimation appear in Table 10. The results in that table agree qualitatively with the results reported above. The elasticity of median score on the General Knowledge portion of the NTE has an achievement elasticity of about 10 and is significant. The elasticity of median score on the Professional Knowledge portion of the NTE has a negative but insignificant coefficient.

We have examined the effect of selection in another way as well. Recall that the selection occurs because Insr is missing. In our reduced form regressions reported earlier in Table 3, we used all 487 observations in the equations for GenKn, PrfKn, and Acad. These equations were re-run using only the 209 observations for which Insr is available. The results were qualitatively similar.

It is our conclusion from the results presented in this section that non-random selection probably does not play a large role in biasing our results.

### 4.4 Effect Sizes and Policy Experiments

Simply reading off the results in Table 7 or Table 5, we find that the elasticity of achievement with respect to General Knowledge is in the neighborhood of ten. On the surface, this would appear to be a very large, even implausibly large, result. Of course, given the standard errors, this elasticity could be in the neighborhood of 3 and still be in the 95\% confidence interval. However, the results are not so large when put into the context of the data used to estimate them. The General Knowledge measure has a very small percentage variation in the data. Looking at Table 2, the standard deviation of GenKn (logged General Knowledge) is only 0.01. Furthermore, the interquartile range is only 0.01. Not reported in the table is the range between the 95th percentile of (not-logged) General Knowledge (671) and the 5th percentile (655), at 16. The range between the 95th and 5th percentiles is less than 3\%! So, in these data, a change of 1\% in the median General Knowledge score is a very large change indeed. By contrast the interquartile range in the logged achievement index is 0.07 and the spread between the 95th and 5th percentiles amounts to slightly more than 19\%.

One policy question we might ask ourselves is: what would happen, ceteris paribus, if a school district at the 25th percentile, in terms of General Knowledge NTE, were to adjust its hiring practices in order to rise to the 75th percentile. This would amount to changing hiring practices to raise its median General
Knowledge NTE score upwards by about 1%. This change, by our estimates, would cause our achievement index to rise by about 10% — by slightly more than its interquartile range. Even this effect is quite large, but if teacher quality is important and if it is well measured by General Knowledge NTE, it is not as implausibly large as the shocking elasticity might lead one to believe.

If we were to look at an elasticity value of 3, still in the 95% confidence interval of the estimator, we still get a pretty large effect. Increasing GenKn across its interquartile range (increasing it by 1%) increases achievement by 3% which is substantially less than its interquartile range.

5 Conclusions

Our objective in this paper has been to examine whether or not various measures of teacher quality affect student achievement once the nature of the hiring process has been accounted for. We find that the more highly educated the residents of a school district are, the less likely the district will hire its former graduates as teachers in the classroom. Also, the greater the number of schools of education nearby, the less likely it is that a district will hire its former graduates. On the other hand, the greater the fraction of children in poor families, the more likely it is that a district will hire its former graduates.

With regard to the determinants of the level of Professional and General Knowledge an employed teacher has, we find that districts with more schools of education nearby paradoxically hire teachers with lower General Knowledge.

Perhaps our most interesting finding is that hiring teachers with greater General Knowledge has a very large positive effect on our composite measure of student achievement; the estimated elasticity is 12.66. On the other hand hiring teachers with greater Professional Knowledge has a negative, but statistically insignificant effect on student achievement.

These findings for Pennsylvania in the mid-1990’s are consistent with the earlier findings of Strauss and Sawyer(1986) for North Carolina in 1979, although they are more focused in differentiating between General Knowledge vs. Professional Knowledge. The empirical results do not answer the question of whether or not emphasizing content knowledge, per se, as contrasted with educational school course work in pedagogy, will directly improve student learning outcomes. If the NTE General Knowledge scores are highly correlated with such college entrance screening devices as SAT or ACT scores, then there may be an immediate, policy-operational interpretation of our results.

As has been discussed elsewhere, various commercial SAT preparation services only hire SAT high scoring teachers to prepare students for such tests. This market validated practice in conjunction with the empirical results above may suggest that states and districts, trying to sort through mounds of teacher applications to find the most productive teachers for their students, would do well

\footnote{It is worth noticing that hiring policy affects flows while the policy goal reflects a stock, so that it would doubtless take some time for a changed hiring policy to affect the overall level of the NTE scores.}

\footnote{See Strauss( 1999).}
to make a primary distinction at a fairly high cutoff level based on such test scores before moving on to other intangible factors such as personality.\textsuperscript{19}

\textsuperscript{19}For example, Stanley Kaplan Educational Services will not hire anyone below the 90th percentile in the SAT distribution—about 1400 combined math and verbal—to teach in their SAT preparation courses. In October, 2000, after better than two years of protracted discussions and negotiations within the Pennsylvania State Board of Education, Pennsylvania General Assembly, and among teacher preparation programs, Pennsylvania adopted new teacher testing guidelines which raised the necessary passing scores from 39% correct to 70% correct for various core battery tests. Teacher preparation programs will now also be required to use specific admissions standards based on standardized tests and grade point averages, and require that prospective teachers take identical coursework as regular college majors in a subject specialty.
6 Bibliography


