

Heartbeat Scheduling

Provable Efficiency for Nested Parallelism

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Motivation: make it easier to write high-level and efficient fork-join parallel code

Running example:

(using notation of the Cilk language extensions for C/C++)

Applies
function f to
iterates in the
range $[lo, hi)$

```
void map(lo, hi, f)
  if lo <= hi
    return
  else if lo + 1 == hi
    f(lo)
    return
```

```
int mid = (lo + hi) / 2
```

```
spawn map(lo, mid, f)
```

```
    map(mid, hi, f)
```

```
sync
```

Fork point
enables calls to
go in parallel

Join point blocks
until both calls
return

Fibers and their overheads

- We consider languages with support for fork join, on a multicore system.
- Every fork point potentially creates a *fiber*.
- Each fiber creation imposes a noticeable cost at runtime.
- The total cost can range from a few percent to a large enough to negate parallelism.

fiber =
representation of
a fork point that
can move
between cores by
load balancing

aka: task
descriptor,
lightweight
thread, spark,
etc.

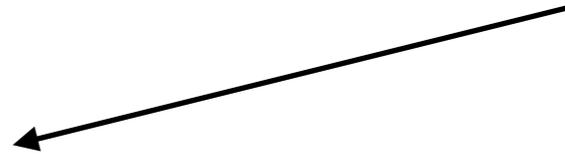
Can we design a runtime technique
that ensures, for any fork-join
program, bounded overheads on the
overall cost of fiber creation?

Related work & contribution

Main approaches to taming fiber-creation overheads

Related work & contribution

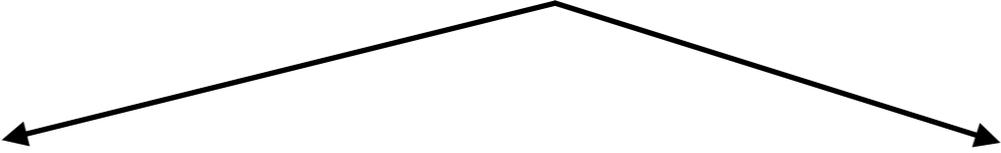
Main approaches to taming fiber-creation overheads



Reduce the cost of each
fiber creation
(useful, but not sufficient)

Related work & contribution

Main approaches to taming fiber-creation overheads



Reduce the cost of each
fiber creation
(useful, but not sufficient)

Reduce the number of fibers created
(i.e., *prune* excess parallelism)

Related work & contribution

Main approaches to taming fiber-creation overheads

```
graph TD; A[Main approaches to taming fiber-creation overheads] --> B[Reduce the cost of each fiber creation  
(useful, but not sufficient)]; A --> C[Reduce the number of fibers created  
(i.e., prune excess parallelism)]; C --> D[Granularity control:  
Prediction of running time  
to throttle fiber creation  
  
(depends on predicting  
execution time, requires  
additional information, not  
always available)];
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Delay creating a fiber until it's  
needed to realize parallelism  
  
(no formal guarantees;  
known adversarial inputs)];
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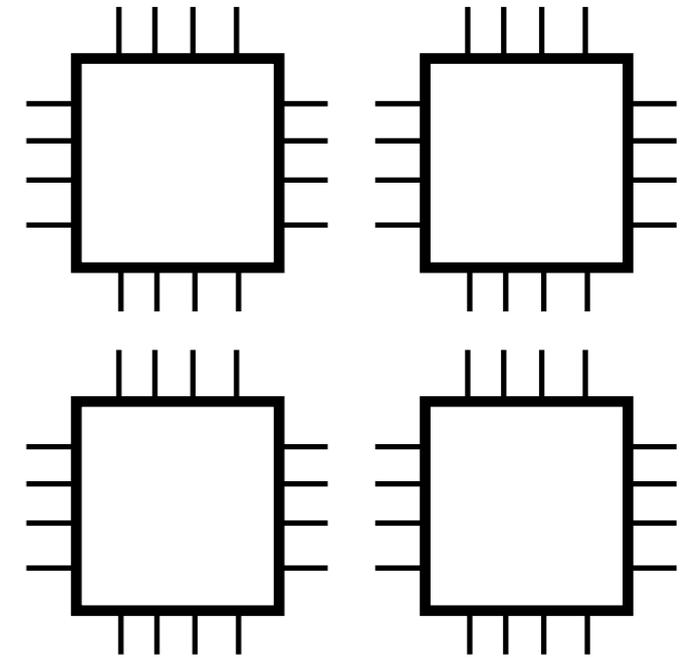
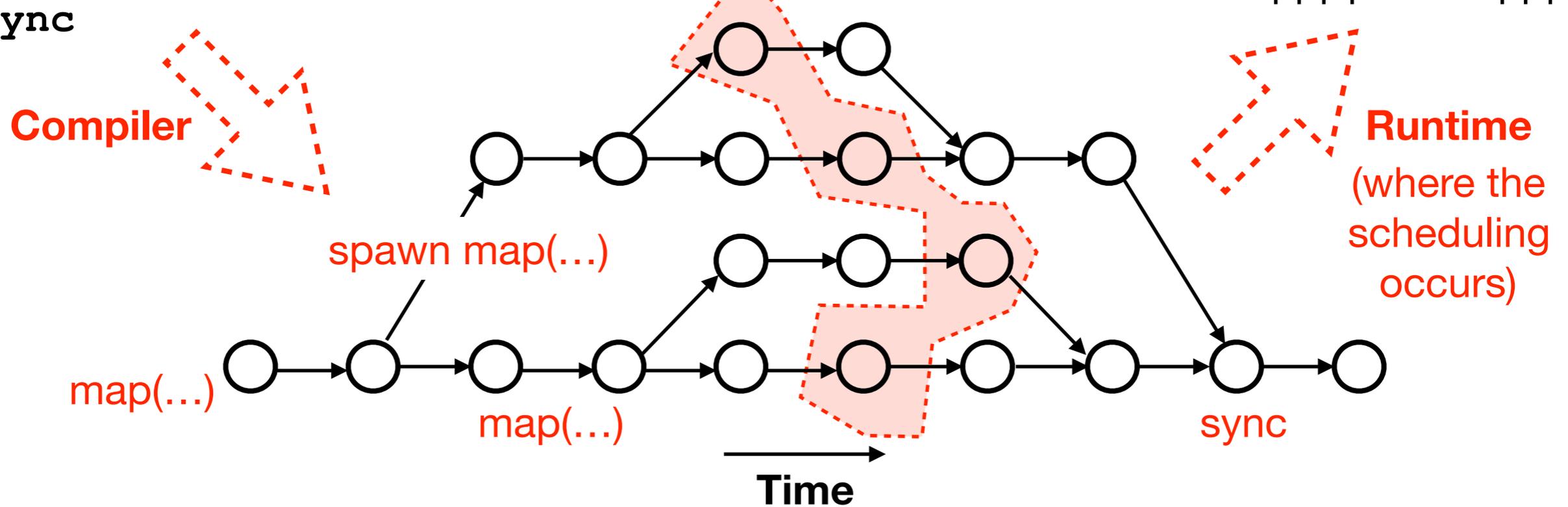
Lazy Scheduling:
Delay creating a fiber until it's needed to realize parallelism

(no formal guarantees; known adversarial inputs)

Heartbeat Scheduling: a runtime technique that, for any fork join program and any input, ensures **provably small overheads** and **good utilization**.

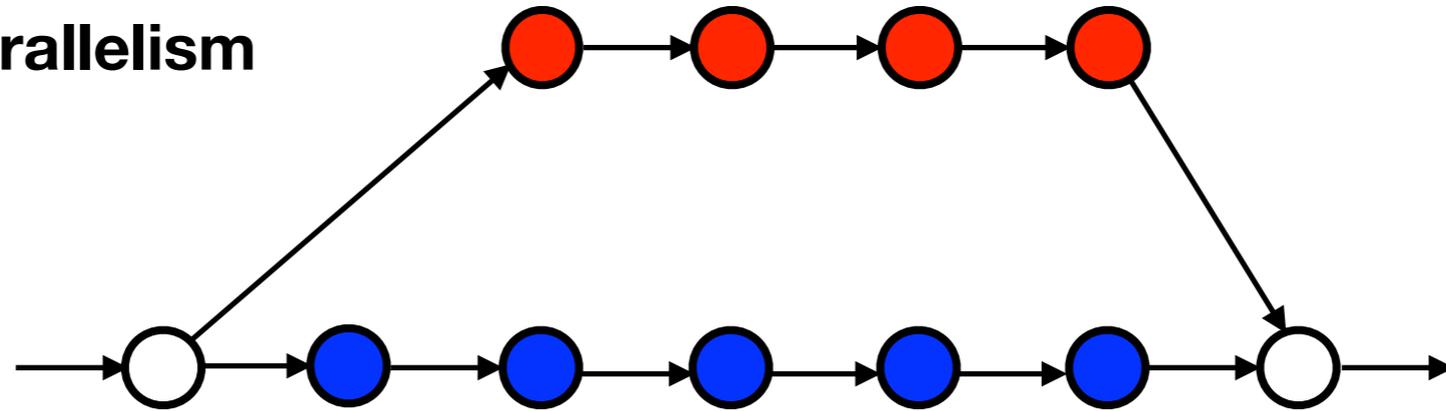
Scheduling fork-join programs

```
void map(lo, hi, f)
  if lo <= hi
    return
  else if lo + 1 == hi
    f(lo)
    return
  int mid = (lo + hi) / 2
  spawn map(lo, mid, f)
  map(mid, hi, f)
sync
```

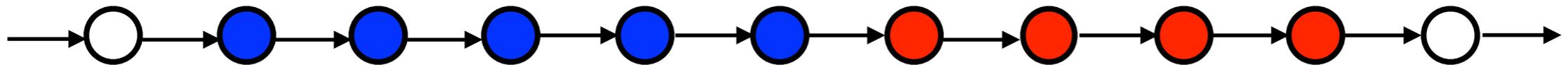


Decision to be made by the runtime for each fork point

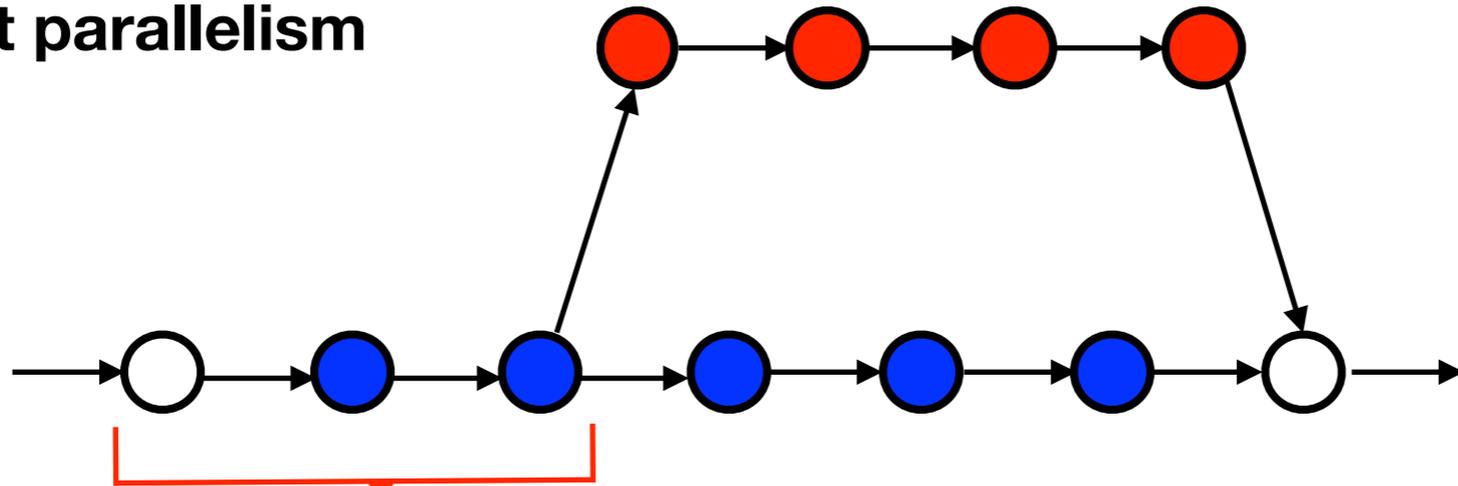
Enable latent parallelism



Sequentialize latent parallelism



Delay latent parallelism



Delay creating a fiber, in case the fork point ends up being excess parallelism

The problem with manual granularity control

```
void map(lo, hi, f)
  if hi - lo < grain
    foreach i in [lo, hi)
      f(i)
  return
int mid = (lo + hi) / 2
spawn map(lo, mid, f)
      map(mid, hi, f)
sync
```

Manual
serializing for
small calls

Manual granularity control
degrades code quality and is not
performance portable.

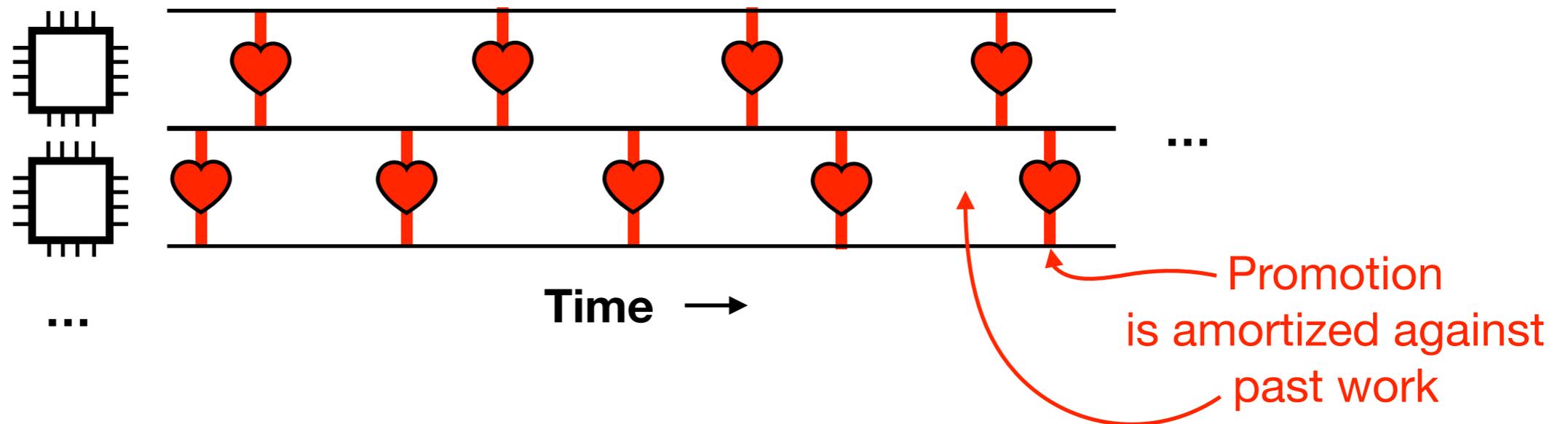
An acceptable setting of `grain`
depends on:

(Tzannes et al 2014)

- The calling context
 - e.g., function f might perform little to a lot of work, might perform a call to `map`
- The execution environment
 - Vagaries of chip architecture
 - Number of cores
 - Operating system / software environment

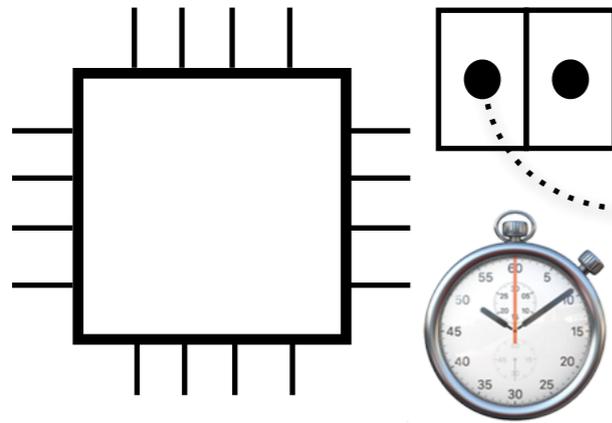
Heartbeat scheduling

Key idea: **amortize** fiber-creation overhead against past work

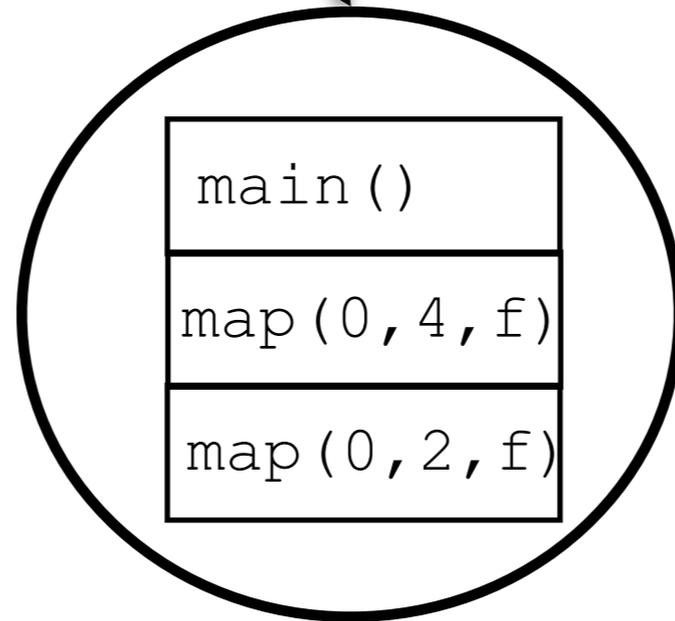


- At runtime, each core keeps track of how long it's been since the previous fiber creation.
- When it's been long enough, the core inspects the call stack of its current running fiber.
- If there's some latent parallel call in the call stack, the core promotes the parallel call into a new fiber.

How heartbeat scheduling works



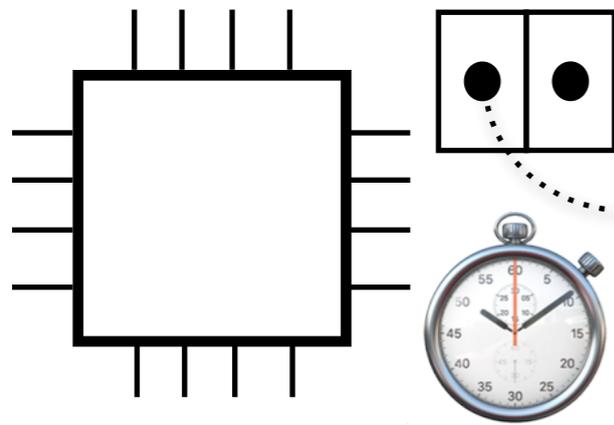
Heartbeat (alarm /
clock fires every
h cycles)



```
void main()  
  map(0, 4, f)  
  return
```

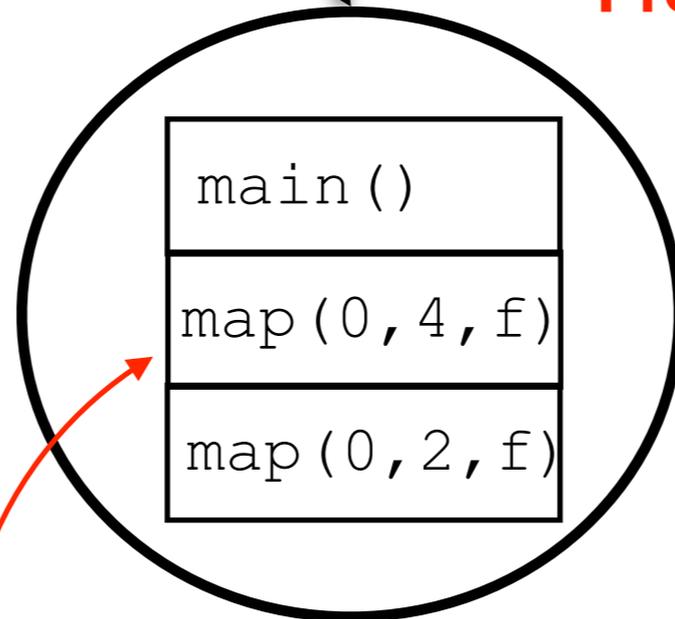
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void map(lo, hi, f)  
  if lo <= hi  
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  else if lo + 1 == hi  
    f(lo)  
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How heartbeat scheduling works



Heartbeat (alarm / clock fires every h cycles)

Promotion



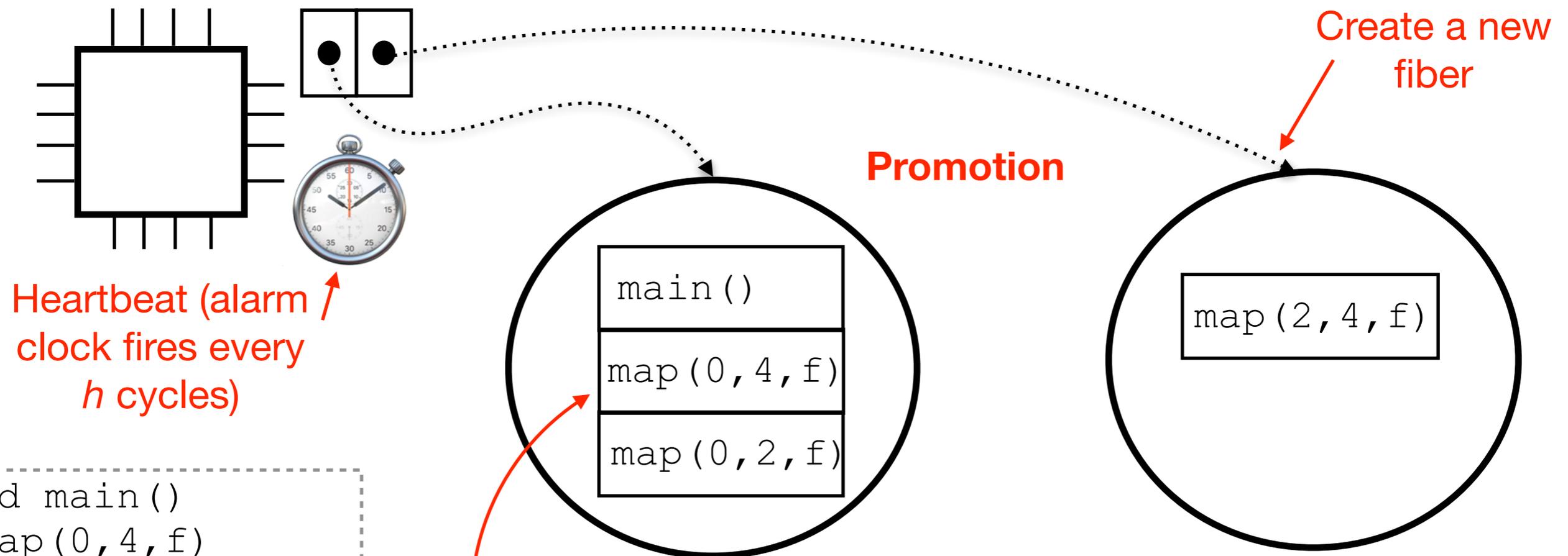
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Snapshot of the call stack, just after second recursive call to map.

The stack grows down.

How heartbeat scheduling works



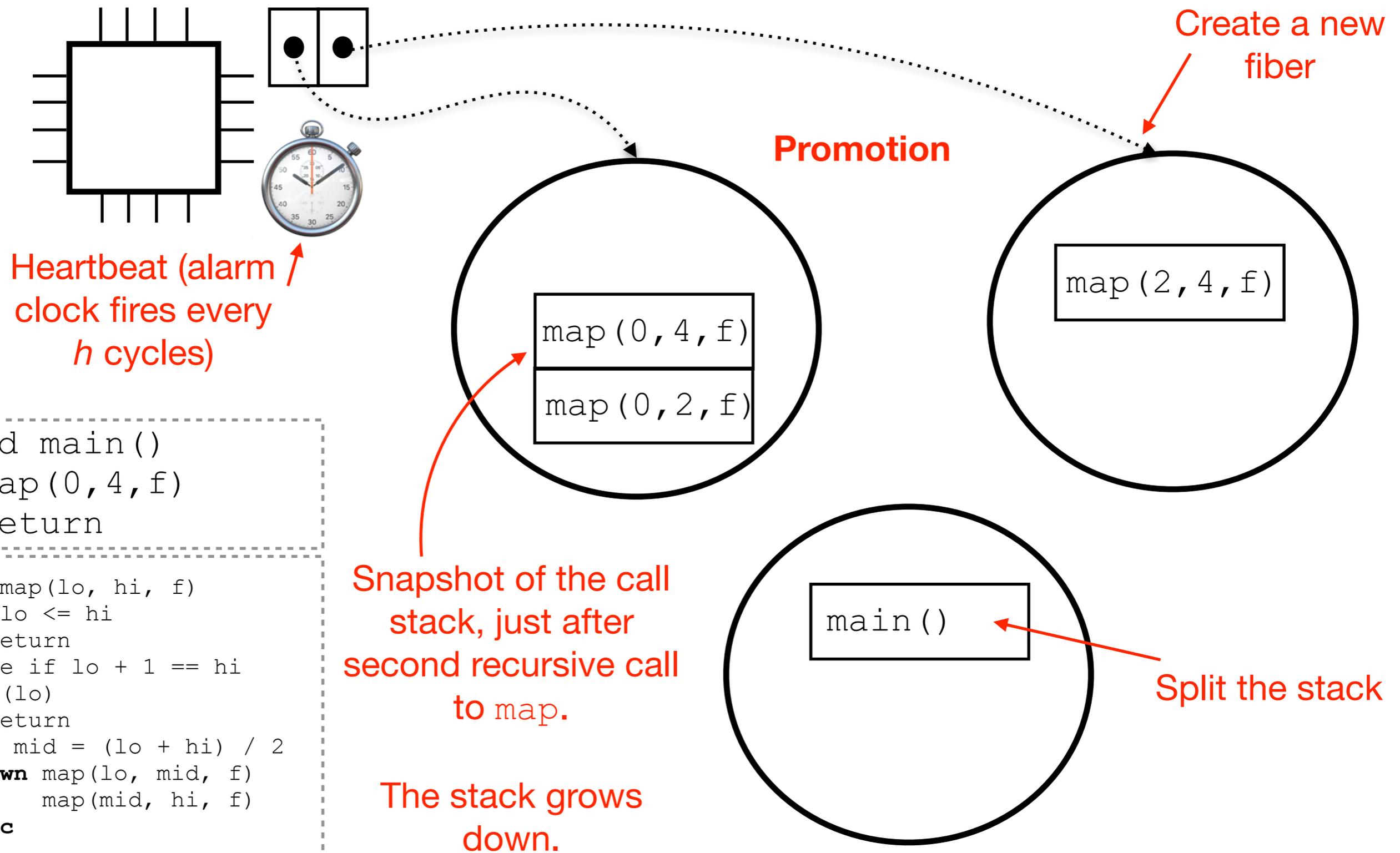
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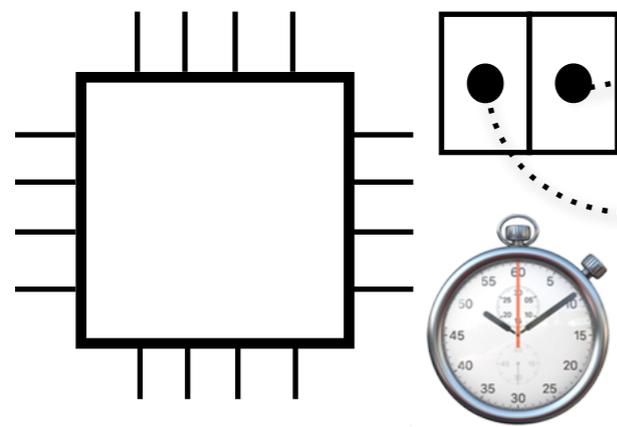
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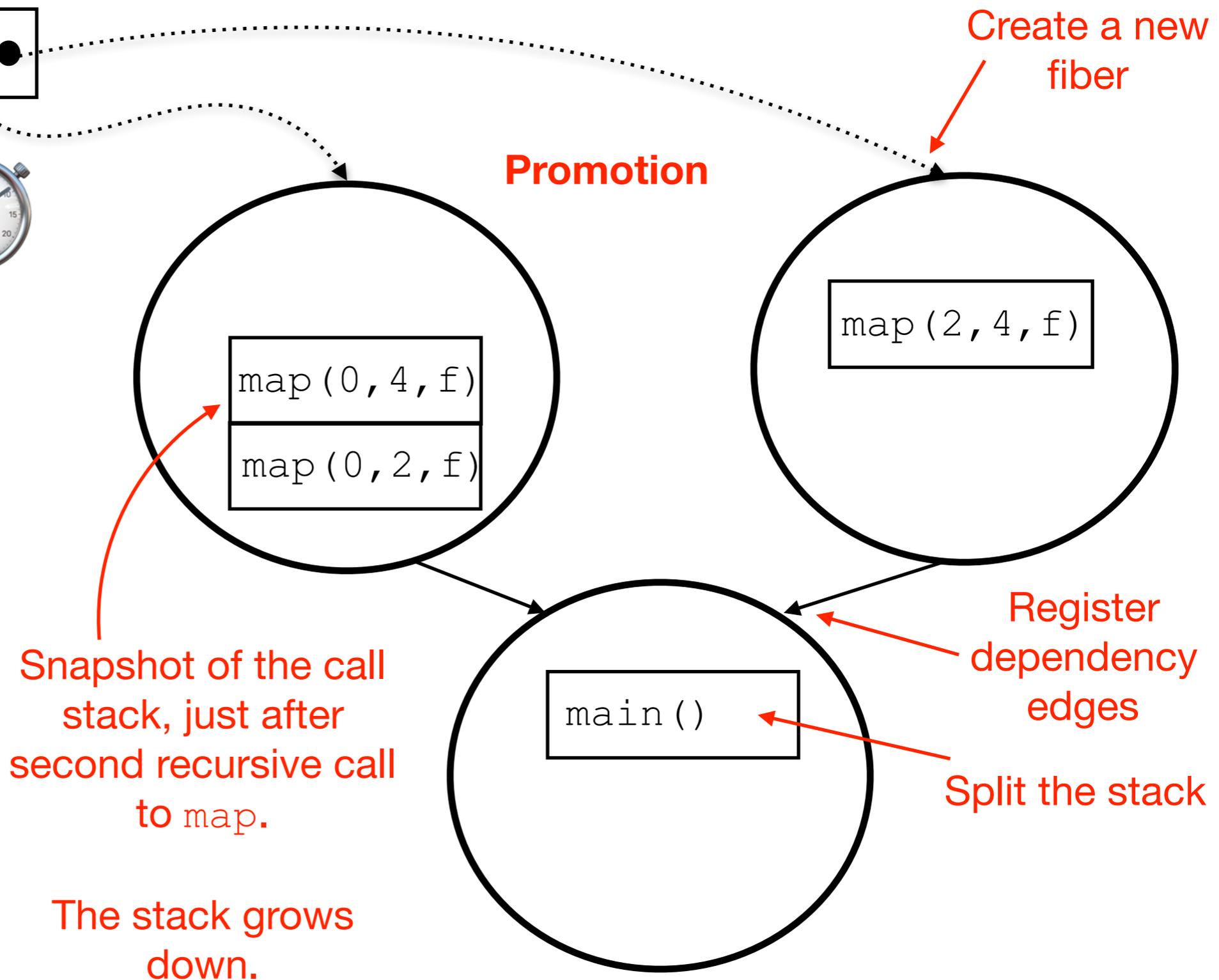


How heartbeat scheduling works



Heartbeat (alarm clock fires every h cycles)

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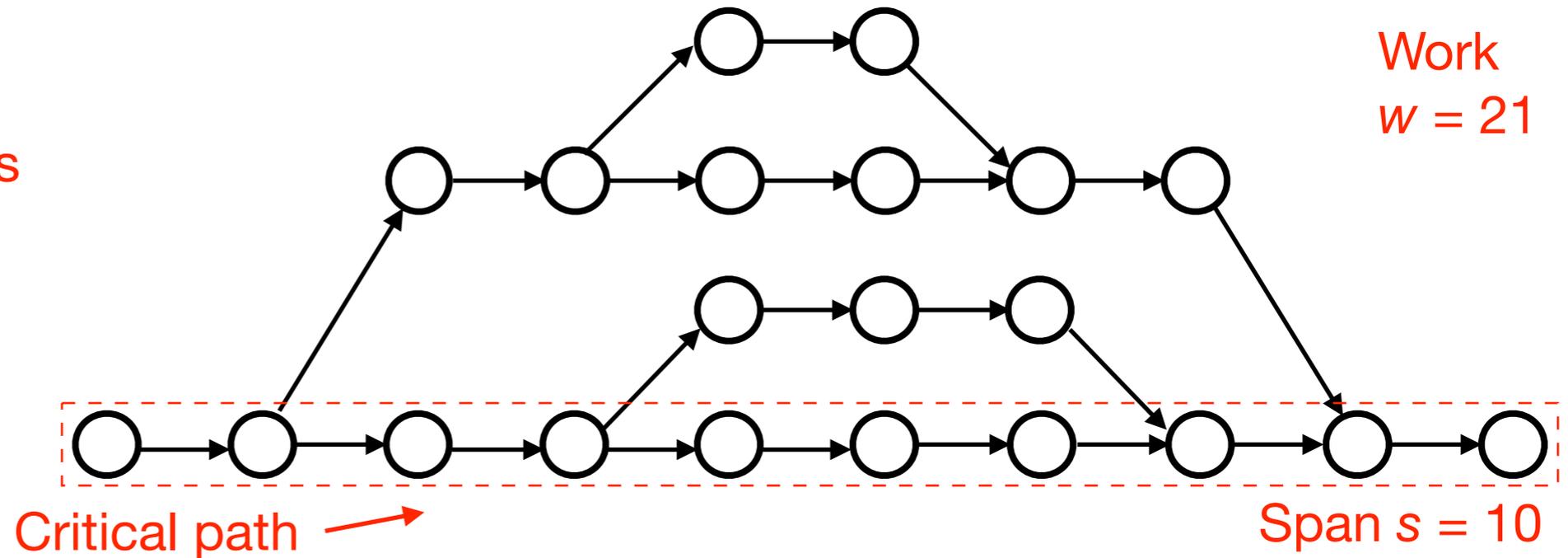
Cost model and time bound

Work

$w = \text{total \# of vertices}$

Span

$s = \text{length of critical path}$



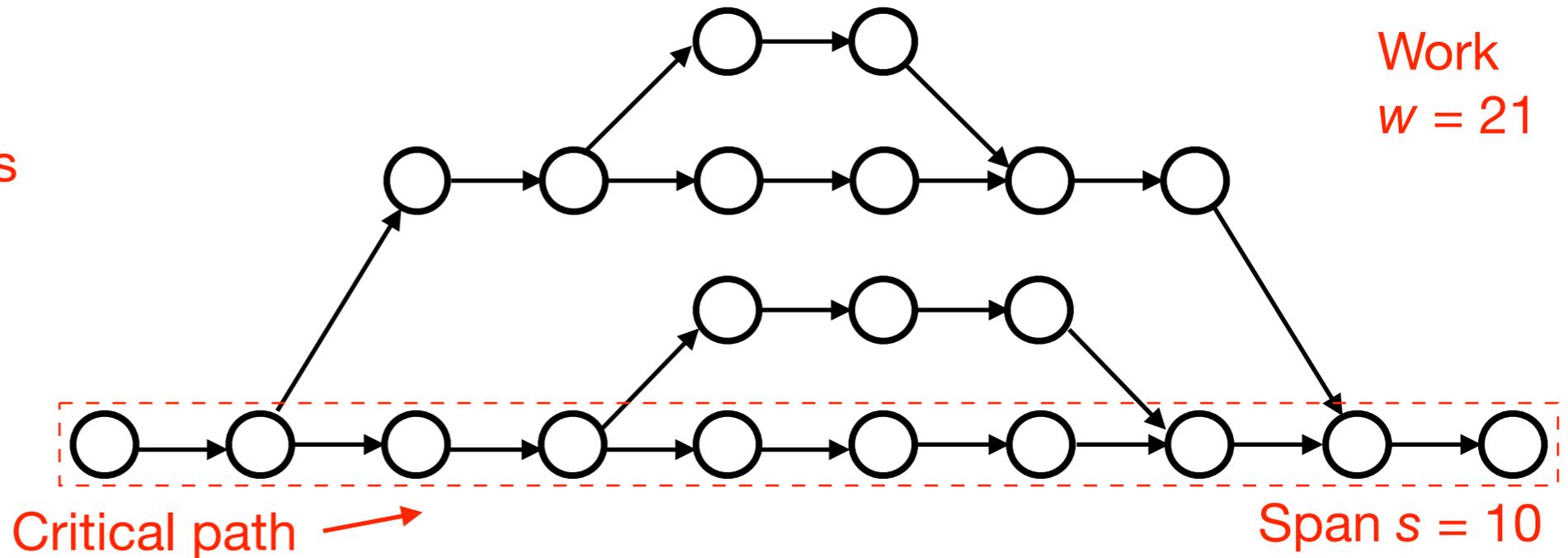
Cost model and time bound

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$w =$ total # of vertices

Span

$s =$ length of critical path



Work-stealing bound:
(Blumofe & Leiserson)

For any fork-join program:

$$E[t_p] \leq w/p + O(s)$$

↑
Expected time to
execute on p cores

← The bound accounts
for the cost of load
balancing fibers, but
assigns to each
scheduling operation
a unit cost.

Time bound for heartbeat scheduling

Definitions:

W Work (total # vertices)

S Span (critical-path length)

t_p Running time of the
program on p cores

Work stealing:

$$E[t_p] \leq w/p +$$

$$O(s)$$

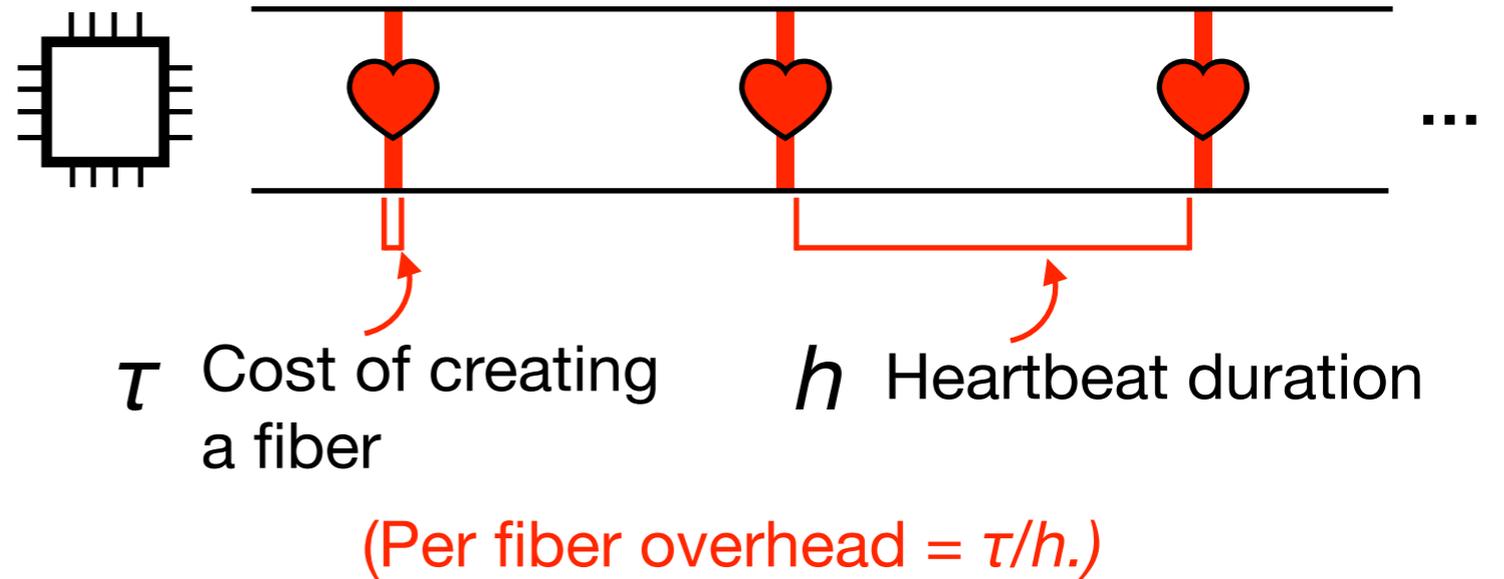
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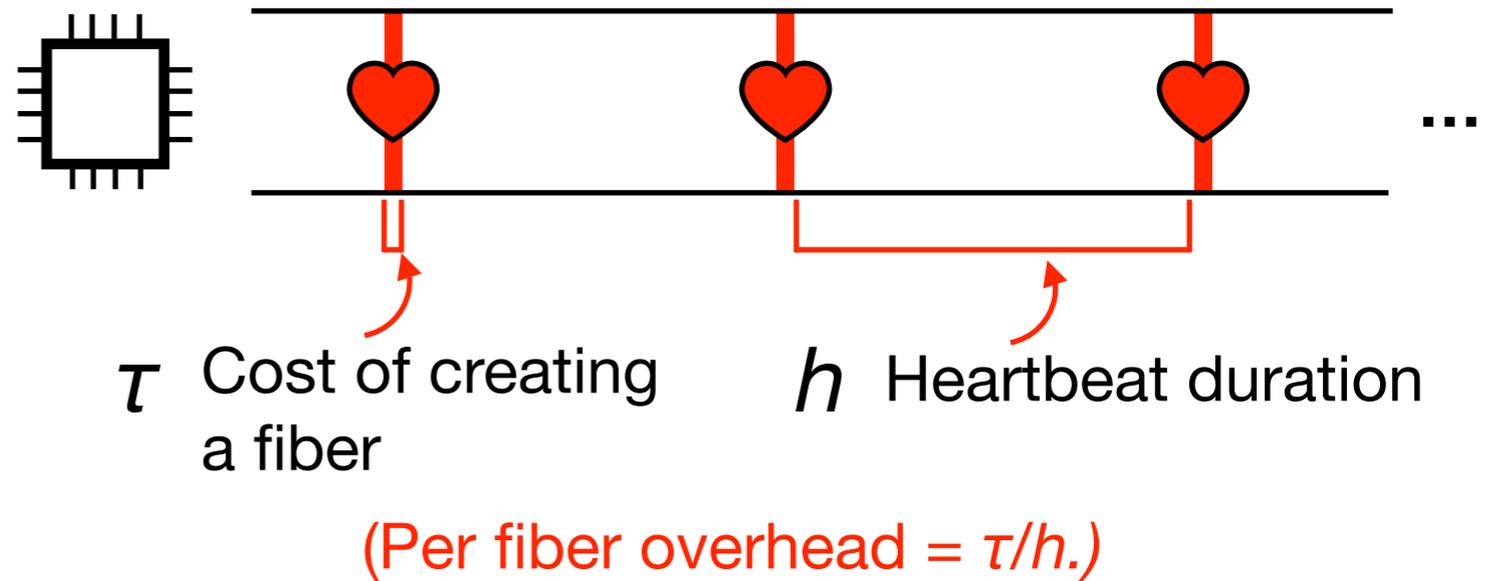
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Definitions:

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Work stealing:

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$O(s)$

$$h = k\tau$$

We can pick h to be a multiple k of τ .

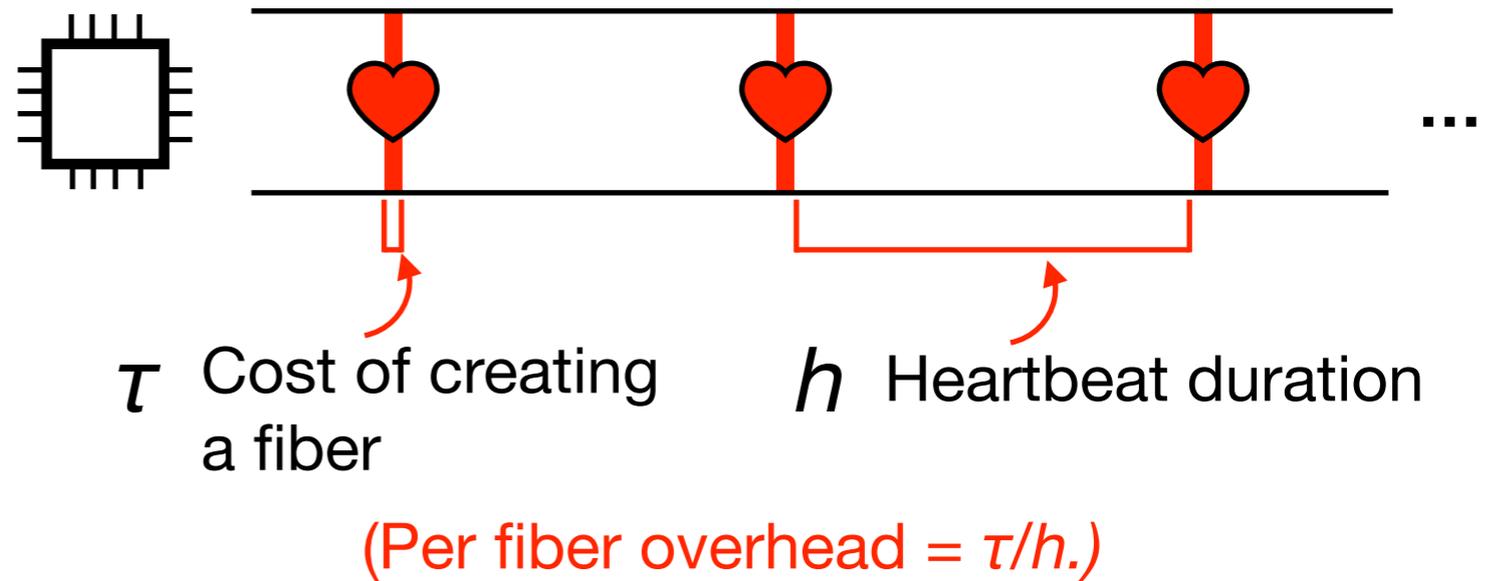
Time bound for heartbeat scheduling

Definitions:

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t_p Running time of the program on p cores



Work stealing:

$$E[t_p] \leq w/p +$$

$$O(s)$$

$$h = k\tau$$

Work stealing with heartbeat, accounting for sched. overheads:

$$E[t_p] \leq w/p + \underbrace{(1/k * w/p)} + \underbrace{O(k * s)}$$

We can pick h to be a multiple k of τ .

1. Bounded increase in overheads

2. Bounded increase in the span

(e.g., 5% of work, if $k = 20$)

Prototype implementation

Heartbeat mechanism

Need to wake up and try to promote \approx 20-50 μ s.



The heartbeat can be realized by software polling or hardware interrupts.

Native support for parallel loops

Should avoid introducing a new stack frame for each parallel loop invocation.

Our solution: extend frame representation to expose *loop descriptor*.

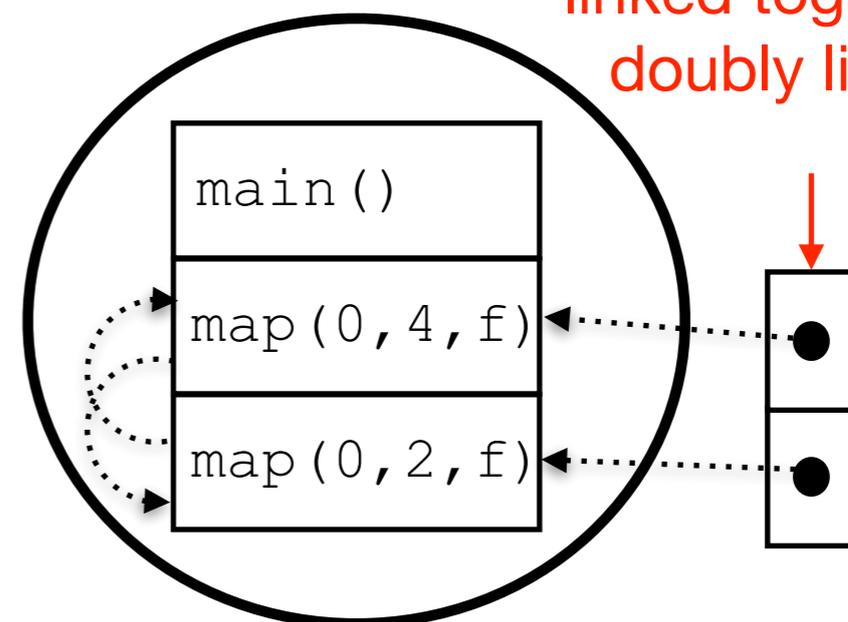
Cactus stack

(+ heartbeat acceleration structure)

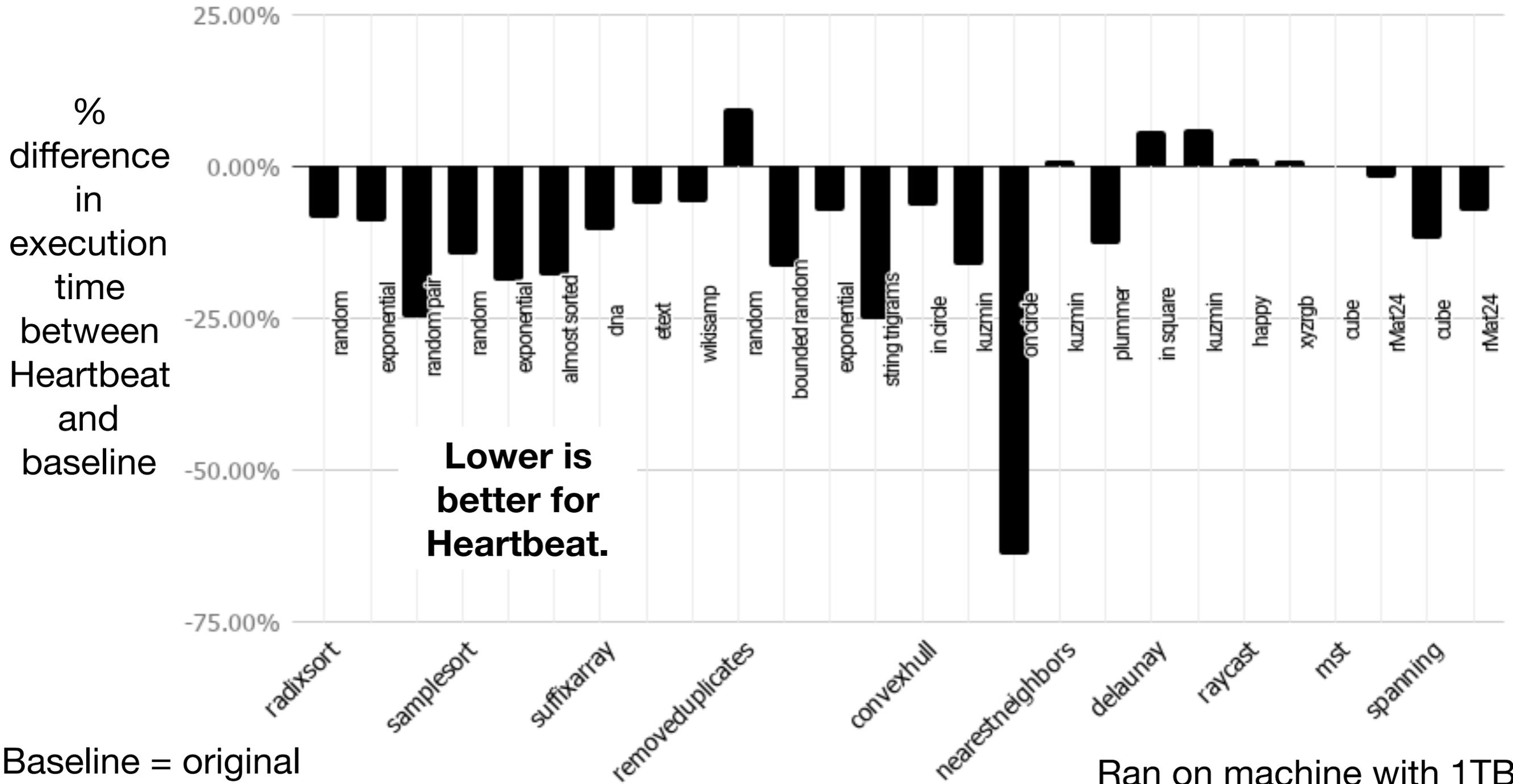
For calling convention: we use the classic cactus-stack representation.

Bookkeeping needed because we need O(1) access to top-most promotable frame.

Promotable frames are linked together by a doubly linked list



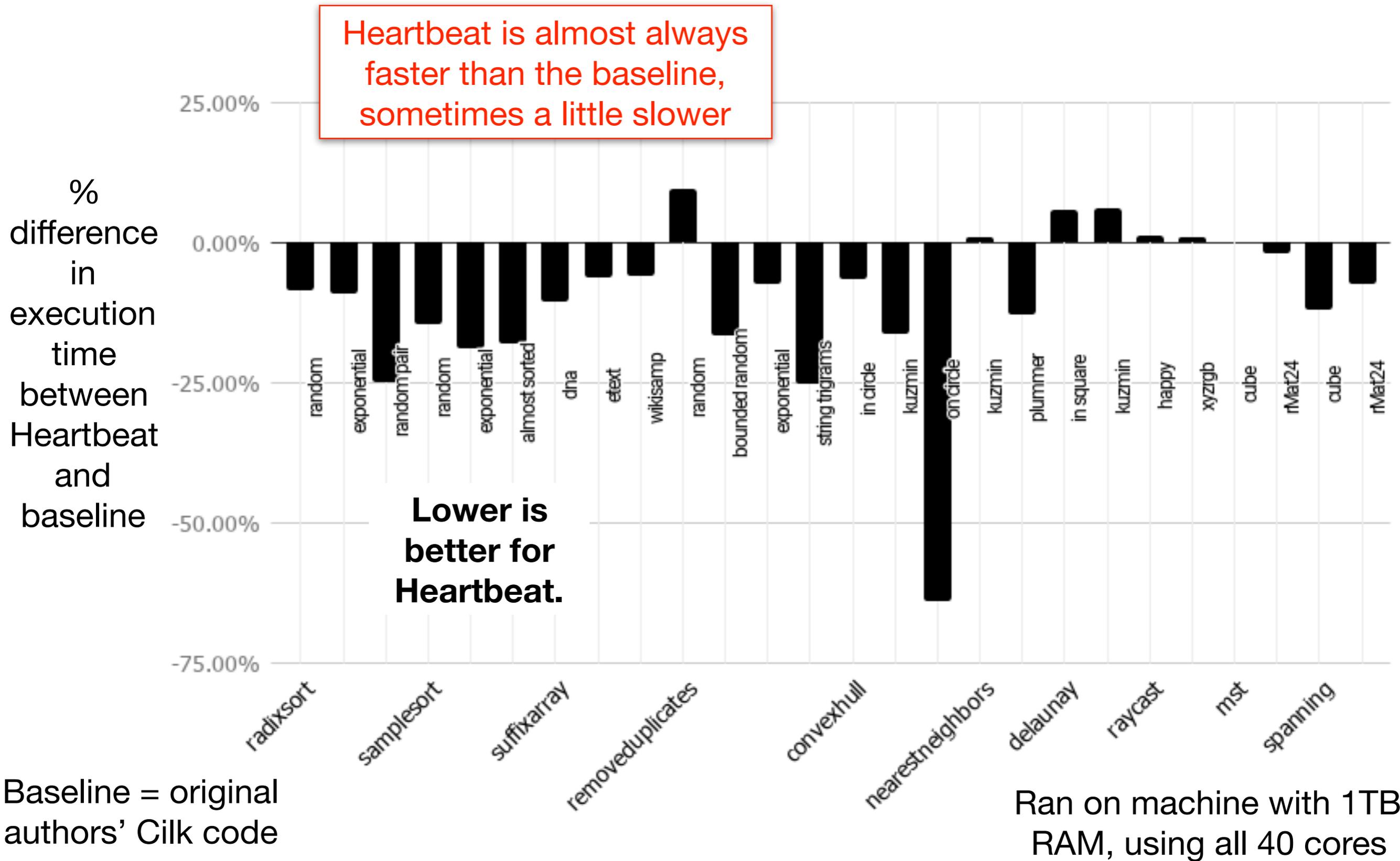
Experimental results



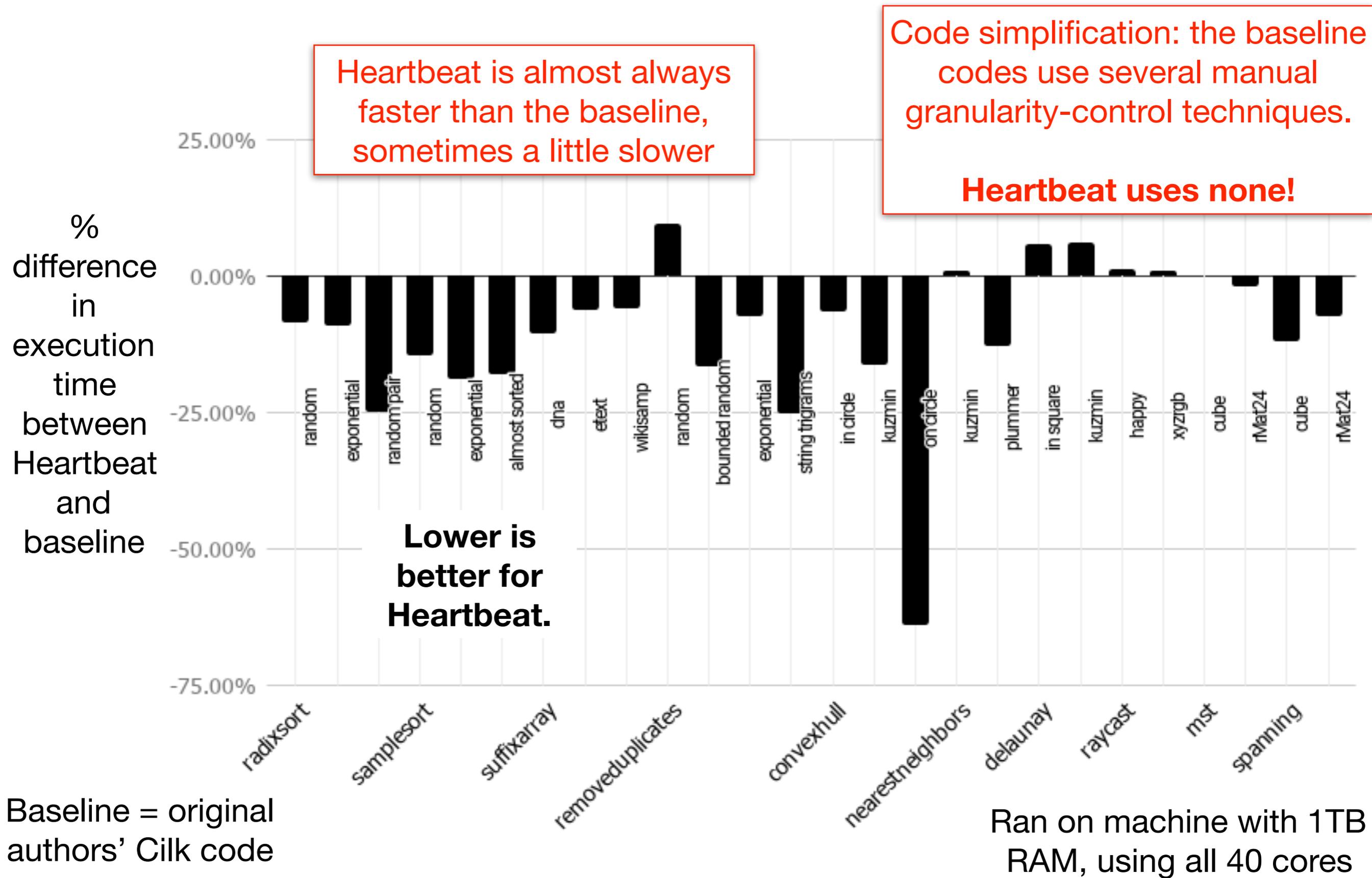
Baseline = original authors' Cilk code

Ran on machine with 1TB RAM, using all 40 cores

Experimental results



Experimental results



Related work

Formal bounds for scheduling fork join

Brent '74, Arora et al '98, Blumofe & Leiserson '99, Agarwal et al '07, Acar et al '11

Lazy-scheduling methods

Mohr et al '91, Feeley '93, Goldstein et al '96, Frigo et al '98, Imam et al '14, Tzannes et al '14

Prediction-based methods

Weening '89, Pehoushek et al '90, Lopez et al '96, Duran et al '08, Acar et al '16, Iwasaki et al '16, Shintaro et al '16



Heartbeat is the first to show analytical bounds on scheduling overheads for all fork join programs.



Heartbeat is the first in this class of approaches to have a state-of-the-art implementation and be backed by end-to-end bounds.



Heartbeat offers similar but stronger guarantees than Oracle-Guided Granularity Control, and delivers state-of-the-art in performance.

Conclusion

- Heartbeat scheduling supports really lightweight nested parallelism:
 - It simplifies code: no need for manual granularity control.
 - It is protected by formal bounds from adversary programs.
 - It can, on ten benchmarks, achieve comparable or better performance to Cilk, a carefully engineered implementation.
- Future work:
 - Optimized compiler implementation
 - Generalizing beyond fork join (e.g., futures)
- **Thanks for you attention!**