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ASPECTS of

SCIENTIFIC EXPLANATION

And Other Essays in the Philosophy of Science

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to Diane
4. EMPIRICIST CRITERIA

OF COGNITIVE SIGNIFICANCE:

PROBLEMS AND CHANGES

1. THE GENERAL EMPIRICIST CONCEPTION OF COGNITIVE AND EMPIRICAL SIGNIFICANCE

It is a basic principle of contemporary empiricism that a sentence makes a cognitively significant assertion, and thus can be said to be either true or false, if and only if either (1) it is analytic or contradictory—in which case it is said to have purely logical meaning or significance—or else (2) it is capable, at least potentially, of test by experiential evidence—in which case it is said to have empirical meaning or significance. The basic tenet of this principle, and especially of its second part, the so-called testability criterion of empirical meaning (or better: meaningfulness), is not peculiar to empiricism alone: it is characteristic also of contemporary operationism, and in a sense of pragmatism as well; for the pragmatist maxim that a difference must make a difference to be a difference may well be construed as insisting that a verbal difference between two sentences must make a difference in experiential implications if it is to reflect a difference in meaning.

How this general conception of cognitively significant discourse led to the rejection, as devoid of logical and empirical meaning, of various formulations in speculative metaphysics, and even of certain hypotheses offered within
Empiricist Criteria of Cognitive Significance

has a particular observable characteristic, i.e., a characteristic whose presence or absence can, under favorable circumstances, be ascertained by direct observation. The task of setting up criteria of empirical significance is thus transformed into the problem of characterizing in a precise manner the relationship which obtains between a hypothesis and one or more observation sentences whenever the phenomena described by the latter either confirm or disconfirm the hypothesis in question. The ability of a given sentence to enter into that relationship to some set of observation sentences would then characterize its testability-in-principle, and thus its empirical significance. Let us now briefly examine the major attempts that have been made to obtain criteria of significance in this manner.

One of the earliest criteria is expressed in the so-called verifiability requirement. According to it, a sentence is empirically significant if and only if it is not analytic and is, at least in principle, complete verification by observational evidence; i.e., if observational evidence can be described which, if actually obtained, would conclusively establish the truth of the sentence. With the

2. THE EARLIER TESTABILITY CRITERIA OF MEANING AND THEIR SHORTCOMINGS

Let us note first that any general criterion of cognitive significance will have to meet certain requirements if it is to be at all acceptable. Of these, we note one, which we shall consider here as expressing a necessary, though by no means sufficient, condition of adequacy for criteria of cognitive significance.

(A) If under a given criterion of cognitive significance, a sentence $N$ is nonsignificant, then so must be all truth-functional compound sentences in which $N$ occurs nonvacuously as a component. For if $N$ cannot be significantly assigned a truth value, then it is impossible to assign truth values to the compound sentences containing $N$; hence, they should be qualified as nonsignificant as well.

We note two corollaries of requirement (A):

(A1) If under a given criterion of cognitive significance, a sentence $S$ is nonsignificant, then so must be its negation, $\neg S$.

(A2) If under a given criterion of cognitive significance, a sentence $N$ is nonsignificant, then so must be any conjunction $N\&S$ and any disjunction $N\mid S$, no matter whether $S$ is significant under the given criterion or not.

We now turn to the initial attempts made in recent empiricism to establish general criteria of cognitive significance. Those attempts were governed by the consideration that a sentence, to make an empirical assertion must be capable of being borne out by, or conflicting with, phenomena which are potentially capable of being directly observed. Sentences describing such potentially observable phenomena—no matter whether the latter do actually occur or not—may be called observation sentences. More specifically, an observation sentence might be construed as a sentence—no matter whether true or false—which ascerts or denies that a specified object, or group of objects, of macroscopic size

(continued next page)
help of the concept of observation sentence, we can restate this requirement as follows: A sentence \( S \) has empirical meaning if and only if it is possible to indicate a finite set of observation sentences, \( O_1, O_2, \ldots, O_n \), such that if these are true, then \( S \) is necessarily true, too. As stated, however, this condition is satisfied also if \( S \) is an analytic sentence or if the given observation sentences are logically incompatible with each other. By the following formulation, we rule these cases out and at the same time express the intended criterion more precisely:

(2.1) **Requirement of Complete Verifiability in Principle.** A sentence has empirical meaning if and only if it is not analytic and follows logically from some finite and logically consistent class of observation sentences. These observation sentences need not be true, for what the criterion is to explicate is testability by "potentially observable phenomena," or testability "in principle."

In accordance with the general conception of cognitive significance outlined earlier, a sentence will now be classified as cognitively significant if either it is analytic or contradictory, or it satisfies the verifiability requirement. This criterion, however, has several serious defects. One of them has been noted by several writers:

- **a.** Let us assume that the properties of being a stock and of being red-legged

3. As has frequently been emphasized in the empiricist literature, the term "verifiability" is to indicate, of course, the conceivability, or better, the logical possibility, of evidence of an observational kind which, if actually encountered, would constitute conclusive evidence for the given sentence; it is not intended to mean the technical possibility of performing the tests needed to obtain such evidence, and even less the possibility of actually finding directly observable phenomena which constitute conclusive evidence for that sentence—which would be tantamount to the actual existence of such evidence and would thus imply the truth of the given sentence. Analogous remarks apply to the terms "falsifiability" and "confirmability." This point has clearly been disregarded in some critical discussions of the verifiability criterion.

Thus, e.g., Russell (1948), p. 468 combines verifiability as the actual existence of a set of conclusively verifying occurrences. This conception, which has never been advocated by any logical empiricist, must naturally turn out to be inadequate since according to it the empirical meaningfulness of a sentence could not be established without gathering empirical evidence, and moreover even of it to permit a conclusive proof of the sentence to questions it. It is not surprising, therefore, that his extraordinary interpretation of verifiability leads Russell to the conclusion: "In fact, that a proposition is verifiable is itself not verifiable" (I.c.). Actually, under the empiricist interpretation of complete verifiability, any statement asserting the verifiability of some sentence \( S \) whose text is quoted, is either analutive or contradictory; for the decision whether there exists a class of observation sentences which entail \( S \), i.e., whether such observation sentences can be formulated, no matter whether they are true or false—that decision is a purely logical matter.

Incidentally, statements of the kind mentioned by Russell, which are not actually verifiable by any human being, were explicitly recognized as cognitively significant already by Schlick (1926), Page 5, who argued that the impossibility of verifying them was "merely empirical." The characterization of verifiability with the help of the concept of observation sentence as suggested here might serve as a more explicit and rigorous statement of that conception.
makes complete falsifiability in principle the defining characteristic of empirical significance. Let us formulate this criterion as follows:

(2.2) REQUIREMENT OF COMPLETE FALSEFIABILITY IN PRINCIPLE. A sentence has empirical meaning if and only if its negation is not analytic and follows logically from some finite logically consistent class of observation sentences.

This criterion qualifies a sentence as empirically meaningful if its negation satisfies the requirement of complete verifiability; as it is to be expected, it is therefore inadequate on similar grounds as the latter:

(a) It denies cognitive significance to purely existential hypotheses, such as 'There exists at least one unicorn', and all sentences whose formulation calls for mixed—i.e., universal and existential—quantification, such as 'For every compound there exists some solvent', for none of these can possibly be conclusively falsified by a finite number of observation sentences.

(b) If 'P' is an observation predicate, then the assertion that all things have the property P is qualified as significant, but its negation, being equivalent to a purely existential hypothesis, is disqualified [cf. (a)]. Hence, criterion (2.2) gives rise to the same dilemma as (2.1).

(c) If a sentence S is completely falsifiable whereas N is a sentence which is not, then their conjunction, S-N (i.e., the expression obtained by connecting the two sentences by the word 'and') is completely falsifiable; for if the negation of S is entailed by a class of observation sentences, then the negation of S-N is, a fortiori, entailed by the same class. Thus, the criterion allows empirical significance to many sentences which an adequate empiricist criterion should rule out, such as 'All swans are white and the absolute is perfect.'

In sum, then, interpretations of the testability criterion in terms of complete verifiability or of complete falsifiability are inadequate because they are overly restrictive in one direction and overly inclusive in another, and because both of them violate the fundamental requirement A.

Several attempts have been made to avoid these difficulties by constraining the testability criterion as demanding merely a partial and possibly indirect confirmability of empirical hypotheses by observational evidence.

A formulation suggested by Ayer is characteristic of these attempts to set up a clear and sufficiently comprehensive criterion of confirmability. It states, in effect, that a sentence S has empirical import if from S in conjunction with suitable subsidiary hypotheses it is possible to derive observation sentences which are not derivable from the subsidiary hypotheses alone.

This condition is suggested by a closer consideration of the logical structure of

3. CHARACTERIZATION OF SIGNIFICANT SENTENCES BY CRITERIA FOR THEIR CONSTITUENT TERMS

An alternative procedure suggests itself which again seems to reflect well
the general viewpoint of empiricism: It might be possible to characterize cognitively significant sentences by certain conditions which their constituent terms have to satisfy. Specifically, it would seem reasonable to say that all extralogical terms in a significant sentence must have empirical reference, and that therefore their meanings must be capable of specification by reference to observables exclusively. In order to exhibit certain analogies between this approach and the previous one, we adopt the following terminological conventions:

Any term that may occur in a cognitively significant sentence will be called a cognitively significant term. Furthermore, we shall understand by an observation term any term which either (a) is an observation predicate, i.e., signifies some observable characteristic (as do the terms ‘blue’, ‘warm’, ‘soft’, ‘coincide with’, ‘of greater apparent brightness than’) or (b) names some physical object of macroscopic size (as do the terms ‘the needle of this instrument’, ‘the Moon’, ‘Krakatoa Volcano’, ‘Greenwich, England’, ‘Julius Caesar’).

Now while the testability criteria of meaning aimed at characterizing the cognitively significant sentences by means of certain inferential connections in which they must stand to some observation sentences, the alternative approach under consideration would instead try to specify the vocabulary that may be used in forming significant sentences. This vocabulary, the class of significant terms, would be characterized by the condition that each of its elements is either a logical term or else a term with empirical significance; in the latter case, it has to stand in certain definitional or explicative connections to some observation terms. This approach certainly avoids any violations of our earlier conditions of adequacy. Thus, e.g., if S is a significant sentence, i.e., contains cognitively significant terms only, then so is its denial, since the denial sign, and its verbal equivalents, belong to the vocabulary of logic and are thus significant. Again, if N is a sentence containing a non-significant term, then so is any compound sentence which contains N.

But this is not sufficient, of course. Rather, we shall now have to consider a crucial question analogous to that raised by the previous approach: Precisely how are the logical connections between empirically significant terms and observation terms to be construed if an adequate criterion of cognitive significance is to result? Let us consider some possibilities.

9. An extralogical term is one that does not belong to the specific vocabulary of logic. The following phrases, and those definable by means of them, are typical examples of logical terms: ‘not’, ‘or’, ‘if . . . then’, ‘all’, ‘some’, ‘. . . is an element of class . . .’. Whether it is possible to make a sharp theoretical distinction between logical and extra-logical terms is a controversial issue related to the problem of discriminating between analytic and synthetic sentences. For the purpose at hand, we may simply assume that the logical vocabulary is given by enumeration.

10. For a detailed exposition and critical discussion of this idea, see H. Feigl’s stimulating and enlightening article (1956).

3.1 The simplest criterion that suggests itself might be called the requirement of definability. It would demand that any term with empirical significance must be explicitly definable by means of observation terms.

This criterion would seem to accord well with the maxim of operationism that all significant terms of empirical science must be introduced by operational definitions. However, the requirement of definability is vastly too restrictive, for many important terms of scientific and even pre-scientific discourse cannot be explicitly defined by means of observation terms.

In fact, as Carnap11 has pointed out, an attempt to provide explicit definitions in terms of observables encounters serious difficulties as soon as dispositional terms, such as ‘soluble’, ‘malleable’, ‘electric conductor’, etc., have to be accounted for; and many of these occur even on the pre-scientific level of discourse.

Consider, for example, the word ‘fragile’. One might try to define it by saying that an object x is fragile if and only if it satisfies the following condition: If at any time t the object is sharply struck, then it breaks at that time. But if the statement connectives in this phrasing are construed truth-functionally, so that the definition can be symbolized by

\[
(D) \quad Fx \equiv (\exists t) (Sxt \supset Bxt)
\]

then the predicate ‘F’ thus defined does not have the intended meaning. For let a be any object which is not fragile (e.g., a raindrop or a rubber band), but which happens not to be sharply struck at any time throughout its existence. Then ‘Sx’ is true and hence ‘Sxt \supset Bxt’ is true for all values of t; consequently, ‘Fx’ is true though a is not fragile.

To remedy this defect, one might construe the phrase ‘if . . . then . . .’ in the original definitions as having a more restrictive meaning than the truth-functional conditional. This meaning might be suggested by the subjunctive phrasing ‘If x were to be sharply struck at any time t, then x would break at t’. But a satisfactory elaboration of this construal would require a clarification of the meaning and the logic of counterfactual and subjunctive conditionals, which is a thorny problem.12

An alternative procedure was suggested by Carnap in his theory of reduction sentences.13 These are sentences which, unlike definitions, specify the meaning of a term only conditionally or partially. The term ‘fragile’, for example, might be introduced by the following reduction sentence:

\[
(R) \quad (\exists t) (Sxt \supset (Fx \equiv Bxt))
\]


12. On this subject, see for example Langford (1941); Lewis (1946), pp. 210-30; Chisholm (1946); Goodman (1947); Tolkienbach (1947), Chapter VIII; Hempel and Oppenheim (1948), Part III; Popper (1949): and especially Goodman’s further analysis (1958).

13. Cf. Carnap, loc. cit. note 11. For a brief elementary presentation of the main ideas, see Carnap (1938), Part III. The sentence R here formulated for the predicate ‘F’ illustrates only the simplest type of reduction sentence, the so-called bilateral reduction sentence.
which specifies that if \( x \) is sharply struck at any time \( t \), then \( x \) is fragile if and only if \( x \) breaks at \( t \).

Our earlier difficulty is now avoided, for if \( x \) is a nonfragile object that is never sharply struck, then that expression in \( R \) which follows the quantifiers is true of \( x \); but this does not imply that ‘\( F x \)’ is true. But the reduction sentence \( R \) specifies the meaning of ‘\( F \)’ only for application to those objects which meet the “test condition” of being sharply struck at some time; for these it states that fragility then amounts to breaking. For objects that fail to meet the test condition, the meaning of ‘\( F \)’ is left undetermined. In this sense, reduction sentences have the character of partial or conditional definitions.

Reduction sentences provide a satisfactory interpretation of the experiential import of a large class of disposition terms and permit a more adequate formulation of so-called operational definitions, which, in general, are not complete definitions at all. These considerations suggest a greatly liberalized alternative to the requirement of definability:

(3.2) The requirement of reducibility. Every term with empirical significance must be capable of introduction, on the basis of observation terms, through chains of reduction sentences.

This requirement is characteristic of the liberalized versions of positivism and physicalism which, since about 1936, have superseded the older, overly narrow conception of a full definability of all terms of empirical science by means of observables, and it avoids many of the shortcomings of the latter. Yet, reduction sentences do not seem to offer an adequate means for the introduction of the central terms of advanced scientific theories, often referred to as theoretical constructs. This is indicated by the following considerations: A chain of reduction sentences provides a necessary and a sufficient condition for the applicability of the term it introduces. (When the two conditions coincide, the chain is tantamount to an explicit definition.) But now take, for example, the concept of length as used in classical physical theory. Here, the length in centimeters of the distance between two points may assume any positive real number as its value; yet it is clearly impossible to formulate, by means of observation terms, a sufficient condition for the applicability of such expressions as ‘having a length of \( \sqrt{2} \) cm’ and ‘having a length of \( \sqrt{2} + 10^{-100} \) cm’; for such conditions would provide a possibility for discrimination, in observational terms, between two lengths which differ by only \( 10^{-100} \) cm.  

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14. Cf. the analysis in Carnap (1936-37), especially section 15; also see the brief presentations of the liberalized point of view in Carnap (1938).

15. (Added in 1946) This is not strictly correct. For a more circumspect statement, see note 13 in "A Logical Appraisal of Operationalism" and the fuller discussion in section 7 of the essay "The Theorician's Dilemma." Both of these pieces are reprinted in the present volume.

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It would be ill-advised to argue that for this reason, we ought to permit only such values of the magnitude, length, as permit the statement of sufficient conditions in terms of observables. For this would rule out, among others, irrational numbers and would prevent us from assigning, to the diagonal of a square with sides of length 1, the length \( \sqrt{2} \), which is required by Euclidean geometry. Hence, the principles of Euclidean geometry would not be universally applicable in physics. Similarly, the principles of the calculus would become inapplicable, and the system of scientific theory as we know it today would be reduced to a clumsy, unmanageable torso. This, then, is no way of meeting the difficulty. Rather, we shall have to analyze more closely the function of constructs in scientific theories, with a view to obtaining through such an analysis a more adequate characterization of cognitively significant terms.

Theoretical constructs occur in the formulation of scientific theories. These may be conceived of, in their advanced stages, as being stated in the form of deductively developed axiomatized systems. Classical mechanics, or Euclidean or some Non-Euclidean form of geometry in physical interpretation, present examples of such systems. The extralogical terms used in a theory of this kind may be divided, in familiar manner, into primitive or basic terms, which are not defined within the theory, and defined terms, which are explicitly defined by means of the primitives. Thus, e.g., in Hilbert's axiomatization of Euclidean geometry, the terms 'point', 'straight line', 'between' are among the primitives, while 'line segment', 'angle', 'triangle', 'length' are among the defined terms. The basic and the defined terms together with the terms of logic constitute the vocabulary out of which all the sentences of the theory are constructed. The latter are divided, in an axiomatic presentation, into primitive statements (also called postulates or basic statements) which, in the theory, are not derived from any other statements, and derived ones, which are obtained by logical deduction from the primitive statements.

From its primitive terms and sentences, an axiomatized theory can be developed by means of purely formal principles of definition and deduction, without any consideration of the empirical significance of its extralogical terms. Indeed, this is the standard procedure employed in the axiomatic development of interpreted mathematical theories such as those of abstract groups or rings or lattices, or any form of pure (i.e., noninterpreted) geometry.

However, a deductively developed system of this sort can constitute a scientific theory only if it has received an empirical interpretation which...
renders it relevant to the phenomena of our experience. Such interpretation is
given by assigning a meaning, in terms of observables, to certain terms or sentences
of the formalized theory. Frequently, an interpretation is given not for the
primitive terms or statements but rather for some of the terms definable by means
of the primitives, or for some of the sentences deducible from the postulates.17
Furthermore, interpretation may amount to only a partial assignment of meaning.
Thus, e.g., the rules for the measurement of length by means of a standard rod
may be considered as providing a partial empirical interpretation for the term
'the length, in centimeters, of interval i', or alternatively, for some sentences of
the form 'the length of interval i is r centimeters'. For the method is applicable
only to intervals of a certain medium size, and even for the latter it does not
constitute a full interpretation since the use of a standard rod does not constitute
the only way of determining length: various alternative procedures are available
involving the measurement of other magnitudes which are connected, by
general laws, with the length that is to be determined.

This last observation, concerning the possibility of an indirect measurement
of length by virtue of certain laws, suggests an important reminder. It is not
correct to speak, as is often done, of 'the experiential meaning' of a term or a
sentence in isolation. In the language of science, and for similar reasons even in
pre-scientific discourse, a single statement usually has no experiential impli-
cations. A single sentence in a scientific theory does not, as a rule, entail any
observation sentences; consequences asserting the occurrence of certain ob-
servable phenomena can be derived from it only by conjoining it with a set of
other, subsidiary, hypotheses. Of the latter, some will usually be observation
sentences, others will be previously accepted theoretical statements. Thus, e.g.,
the relativistic theory of the deflection of light rays in the gravitational field
of the sun entails assertions about observable phenomena only if it is conjoined
with a considerable body of astronomical and optical theory as well as a large
number of specific statements about the instruments used in those observations
of solar eclipses which serve to test the hypothesis in question.

Hence, the phrase, 'the experiential meaning of expression E', is elliptical: What

17. A somewhat fuller account of this type of interpretation may be found in Carnap (1939),
§24. The articles by Spence (1944) and by MacCormack and Meichi (1948) provide enlightening
illustrations of the use of theoretical constructs in a field outside that of the physical sciences,
and of the difficulties encountered in an attempt to analyze in detail their function and inter-
pretation.

Northrop (cf., 1956), Chap. VII, and also the detailed study of the use of deductively formul-
ated theories in science, ibid., Chaps. IV, V, VI and H. Margolis (cf., for example, (1955))
have discussed certain aspects of this process under the title of 'epistemic correlation.'

a given expression "means" in regard to potential empirical data is relative to
two factors, namely:
I. the linguistic framework L to which the expression belongs. Its rules
determine, in particular, what sentences—observational or other-
wise—may be inferred from a given statement or class of statements;
II. the theoretical context in which the expression occurs, i.e., the class
of those statements in L which are available as subsidiary hypotheses.

Thus, the sentence formulating Newton's law of gravitation has no ex-
periential meaning by itself; but when used in a language whose logical apparatus
permits the development of the calculus, and when combined with a suitable
system of other hypotheses—including sentences which connect some of the
theoretical terms with observation terms and thus establish a partial inter-
pretation—then it has a bearing on observable phenomena in a large variety of
fields. Analogous considerations are applicable to the term 'gravitational field',
for example. It can be considered as having experiential meaning only within
the context of a theory, which must be at least partially interpreted; and the
experiential meaning of the term—as expressed, say, in the form of operational
criteria for its application—will depend again on the theoretical system at hand,
and on the logical characteristics of the language within which it is formulated.

4. COGNITIVE SIGNIFICANCE AS A CHARACTERISTIC OF INTER-
PRETED SYSTEMS

The preceding considerations point to the conclusion that a satisfactory
criterion of cognitive significance cannot be reached through the second avenue
of approach here considered, namely by means of specific requirements for the
terms which make up significant sentences. This result accords with a general
characteristic of scientific (and, in principle, even pre-scientific) theorizing:
Theory formation and concept formation go hand in hand; neither can be
 carried on successfully in isolation from the other.

If, therefore, cognitive significance can be attributed to anything, then only
to entire theoretical systems formulated in a language with a well-determined
structure. And the decisive mark of cognitive significance in such a system appears
to be the existence of an interpretation for it in terms of observables. Such an
interpretation might be formulated, for example, by means of conditional or
biconditional sentences connecting nonobservational terms of the system with
observation terms in the given language; the latter as well as the connecting
sentences may or may not belong to the theoretical system.

But the requirement of partial interpretation is extremely liberal; it is satisfied,
for example, by the system consisting of contemporary physical theory com-
bined with some set of principles of speculative metaphysics, even if the latter
have no empirical interpretation at all. Within the total system, these metaphysical principles play the role of what K. Reach and also O. Neurath liked to call isolated sentences: They are neither purely formal truths or falsehoods, demonstrable or refutable by means of the logical rules of the given language system; nor do they have any experiential bearing; i.e., their omission from the theoretical system would have no effect on its explanatory and predictive power in regard to potentially observable phenomena (i.e., the kind of phenomena described by observation sentences). Should we not, therefore, require that a cognitively significant system contain no isolated sentences? The following criterion suggests itself:

(4.1) A theoretical system is cognitively significant if and only if it is partially interpreted to at least such an extent that none of its primitive sentences is isolated.

But this requirement may bar from a theoretical system certain sentences which might well be viewed as permissible and indeed desirable. By way of a simple illustration, let us assume that our theoretical system $T$ contains the primitive sentence

$$\text{(SI)} \quad (s)[P_x \rightarrow (Q_x \equiv P_y)]$$

where $P_x$ and $P_y$ are observation predicates in the given language $L$, while $Q$ functions in $T$ somewhat in the manner of a theoretical construct and occurs in only one primitive sentence of $T$, namely SI. Now SI is not a truth or falsehood of formal logic; and furthermore, if SI is omitted from the set of primitive sentences of $T$, then the resulting system $T'$, possesses exactly the same systematic, i.e., explanatory and predictive, power as $T$. Our contemplated criterion would therefore require SI as an isolated sentence which has to be eliminated—excised by means of Occam’s razor, as it were—if the theoretical system at hand is to be cognitively significant.

But it is possible to take a much more liberal view of SI by treating it as a partial definition for the theoretical term ‘$Q$’. Thus conceived, SI specifies that in all cases where the observable characteristic $P_1$ is present, ‘$Q$’ is applicable if and only if the observable characteristic $P_2$ is present as well. In fact, SI is an instance of those partial, or conditional, definitions which Carnap calls bilateral reduction sentences. These sentences are explicitly qualified by Carnap as analytic (though not, of course, as truths of formal logic), essentially on the ground that all their consequences which are expressible by means of observation predicates (and logical terms) alone are truths of formal logic.

Let us pursue this line of thought a little further. This will lead us to some observations on analytic sentences and then back to the question of the adequacy of (4.1).

20. The sentence $O$ is what Carnap calls the representative sentence of the couple consisting of the sentences $S_1$ and $S_2$; see (1936-37), pp. 451-53.
an isolated sentence among its primitives. For assume that a certain theoretical system T1 contains among its primitive sentences S', S'', ... exactly one, S', which is isolated. Then T1 is not significant under (4.1). But now consider the theoretical system T2 obtained from T1 by replacing the two first primitive sentences, S', S'', by one, namely their conjunction. Then, under our assumptions, none of the primitive sentences of T2 is isolated, and T2, though equivalent to T1, is qualified as significant by (4.1). In order to do justice to the intent of (4.1), we would therefore have to lay down the following stricter requirement:

(4.2) A theoretical system is cognitively significant if and only if it is partially interpreted to such an extent that in no system equivalent to it at least one primitive sentence is isolated.

Let us apply this requirement to some theoretical system whose postulates include the two sentences S1 and S2 considered before, and whose other postulates do not contain 'Q' at all. Since the sentences S1 and S2 together entail the sentence O, the set consisting of S1 and S2 is logically equivalent to the set consisting of S1, S2 and O. Hence, if we replace the former set by the latter, we obtain a theoretical system equivalent to the given one. In this new system, both S1 and S2 are isolated since, as can be shown, their removal does not affect the explanatory and predictive power of the system in reference to observable phenomena. To put it intuitively, the systematic power of S1 and S2 is the same as that of O. Hence, the original system is disqualified by (4.2). From the viewpoint of a strictly sensationalist positivism as perhaps envisaged by Mach, this result might be hailed as a sound repudiation of theories making reference to fictitious entities, and as a strict insistence on theories couched exclusively in terms of observables. But from a contemporary vantage point, we shall have to say that such a procedure overlooks or misjudges the important function of constructs in scientific theory: The history of scientific endeavor shows that if we wish to arrive at precise, comprehensive, and well-confirmed general laws, we have to rise above the level of direct observation. The phenomena directly accessible to our experience are not connected by general laws of great scope and rigor. Theoretical constructs are needed for the formulation of such higher-level laws. One of the most important functions of a well-chosen construct is its potential ability to serve as a constituent in ever new general connections that may be discovered; and to such connections we would blind ourselves if we insisted on bannning from scientific theories all those terms and sentences which could be "dispensed with" in the sense indicated in (4.2). In following such a narrowly phenomenalistic or positivistic course, we would deprive ourselves of the tremendous fertility of theoretical constructs, and we would often render the formal structure of the expurgated theory clumsy and inefficient.

Criterion (4.2), then, must be abandoned, and considerations such as those outlined in this paper seem to lend strong support to the conjecture that no adequate alternative to it can be found; i.e., that it is not possible to formulate general and precise criteria which would separate those partially interpreted systems whose isolated sentences might be said to have a significant function from those in which the isolated sentences are, so to speak, mere useless appendages.

We concluded earlier that cognitive significance in the sense intended by recent empiricism and operationism can at best be attributed to sentences forming a theoretical system, and perhaps rather to such systems as wholes. Now, rather than try to replace (4.2) by some alternative, we will have to recognize further that cognitive significance in a system is a matter of degree: Significant systems range from those whose entire extralogical vocabulary consists of observation terms, through theories whose formulation relies heavily on theoretical constructs, on to systems with hardly any bearing on potential empirical findings. Instead of dichotomizing this array into significant and non-significant systems it would seem less arbitrary and more promising to appraise or compare different theoretical systems in regard to such characteristics as these:

a. the clarity and precision with which the theories are formulated, and with which the logical relationships of their elements to each other and to expressions couched in observational terms have been made explicit;

b. the systematic, i.e., explanatory and predictive, power of the systems in regard to observable phenomena;

c. the formal simplicity of the theoretical system with which a certain systematic power is attained;

d. the extent to which the theories have been confirmed by experiential evidence.

Many of the speculative philosophical approaches to cosmology, biology, or history, for example, would make a poor showing on practically all of these counts and would thus prove no matches to available rival theories, or would be recognized as so unpromising as not to warrant further study or development. If the procedure here suggested is to be carried out in detail, so as to become applicable also in less obvious cases, then it will be necessary, of course, to develop general standards, and theories pertaining to them, for the appraisal and comparison of theoretical systems in the various respects just mentioned. To what extent this can be done with rigor and precision cannot well be judged in advance. In recent years, a considerable amount of work has been done towards a definition and theory of the concept of degree of confirmation, or logical probability, of a theoretical system, and several contributions have been made towards the

21 Cf., for example, Carnap (1945:1 and 1948:2), and especially (1950). Also see Hefner and Oppenheim (1945).
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clarification of some of the other ideas referred to above. The continuation of this research represents a challenge for further constructive work in the logical and methodological analysis of scientific knowledge.

22. On simplicity, cf. especially Popper (1936), Chap. V; Reichenbach (1938), §42; Goodman (1949), (1950), (1950); on explanatory and predictive power, cf. Hempel and Oppenheim (1948), Part IV.

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