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Numerical Analysis Homework 2b

Kincaid 3.3 #8) Program the Newton algorithm in complex arithmetic, and test it on these functions with the given starting points.

```
NewtonIteration[F_, a_] := a -  $\frac{F[a]}{F'[a]}$  ;  
RunProgram[F_, a_, iter_] :=  
  Block[{x = a, i = 0},  
    For[i = 0, i <= iter, i++,  
      Print[StringExpression["Iteration "], i,  
        StringExpression[": "], N[x]];  
      x = NewtonIteration[F, x]]];
```

(a)

```
f[z_] := z2 - 1;  
RunProgram[f, 3 + i, 5]  
  
Iteration 0: 3. + 1. i  
Iteration 1: 1.65 + 0.45 i  
Iteration 2: 1.10705 + 0.148077 i  
Iteration 3: 0.997237 + 0.0146885 i  
Iteration 4: 0.999895 - 0.0000391458 i  
Iteration 5: 1. + 4.10798 × 10-9 i
```

(b)

```
In[95]:= f[z_] := z + Sin[z] - 3;  
RunProgram[f, 2 - i, 5]  
  
Iteration 0: 2. - 1. i  
Iteration 1: 2.31634 - 0.516828 i  
Iteration 2: 2.43554 - 0.0665797 i  
Iteration 3: 2.09744 + 0.0618869 i  
Iteration 4: 2.17654 + 0.00845053 i  
Iteration 5: 2.17981 + 0.0000525506 i
```

(c)

```

In[97]:= f[z_] := z^4 + z^2 + 2 + 3 i;
RunProgram[f, 1, 5]

Iteration 0: 1.
Iteration 1: 0.333333 - 0.5 i
Iteration 2: 2.87509 - 1.61308 i
Iteration 3: 2.14273 - 1.24178 i
Iteration 4: 1.60889 - 0.987186 i
Iteration 5: 1.25204 - 0.83956 i

```

Kincaid 3.3 #6) A succession of 60 monthly payments is made into an annuity. In the first to fifth years, the payments are, respectively, \$200, \$275, \$312, \$380, and \$400. Just after the last payment has been made, the accumulated value of the annuity is \$24,738. What was the monthly rate of interest? Use the secant method to find the zero of the polynomial that arises.

The polynomial for the value of the annuity is

$$V = \sum_{i=1}^{12} 200x^{60-i} + \sum_{i=1}^{12} 275x^{48-i} + \sum_{i=1}^{12} 312x^{36-i} + \sum_{i=1}^{12} 380x^{24-i} + \sum_{i=1}^{12} 400x^{12-i} - 24738.$$

```

In[43]:= SecantIteration[F_, x1_, x11_] :=
  x1 - F[x1] ( (x1 - x11) / (F[x1] - F[x11]) );
RunProgram[F_, a_, b_, iter_] :=
  Block[{x1 = a, x11 = b, temp = 0, i = 0},
  For[i = 0, i <= iter, i++,
  Print[StringExpression["Iteration "], i,
  StringExpression[": "], N[x1],
  StringExpression[" "], F[x1]];
  temp = SecantIteration[F, x11, x1];
  x11 = x1; x1 = temp]];

```

$$\text{In[46]:= } f[x_] := \sum_{i=1}^{12} 200 x^{60-i} + \sum_{i=1}^{12} 275 x^{48-i} + \sum_{i=1}^{12} 312 x^{36-i} +$$

$$\sum_{i=1}^{12} 380 x^{24-i} + \sum_{i=1}^{12} 400 x^{12-i} - 24738;$$

RunProgram[f, 1.3, 1.00, 10]

Iteration 0: 1.3 4.65157 × 10⁹
 Iteration 1: 1. -5933.82
 Iteration 2: 1. -5933.63
 Iteration 3: 1.01231 1541.82
 Iteration 4: 1.00977 -288.021
 Iteration 5: 1.01017 -11.3501
 Iteration 6: 1.01019 0.0879096
 Iteration 7: 1.01019 -0.0000265726
 Iteration 8: 1.01019 -1.30967 × 10⁻¹⁰
 Iteration 9: 1.01019 2.18279 × 10⁻¹¹
 Iteration 10: 1.01019 2.18279 × 10⁻¹¹