

Market-making with Search and Information Frictions

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Liquidity in Financial Markets

OTC markets are changing: reduced trading frictions & increased transparency

- policy: OTC markets → centralized exchanges, required disclosure of trades (TRACE)
- technology: faster/easier for traders to receive quotes & dealers to aggregate information

How will these changes impact liquidity?

A common metric for liquidity: **Bid-ask spreads**

- More generally, non-linear pricing or the price impact of trade

Asymmetric Information + Search

Two prominent theories provide stark predictions:

- ① **Asymmetric information**: investors know more about asset than dealers
 - See, e.g., Glosten-Milgrom
 - Prediction: more transparency \Rightarrow narrower spreads
- ② **Search frictions**: dealers have market power, investors trade infrequently
 - See, e.g., Duffie-Garleanu-Pedersen
 - Prediction: faster trading \Rightarrow narrower spreads

Do changes in trading frictions mitigate or exacerbate informational frictions?

Are these stark predictions true when both frictions are present?

Challenge: existing literature (theory & empirical) studies two frictions **in isolation**

Hard to answer without a **unified framework**

This Paper

Develop a unified framework of a dynamic asset market with:

- ① search frictions and market power
- ② asymmetric information

where dealers *learn over time* from market-wide trading activity

Show that interaction \Rightarrow conventional wisdom does not hold

Focus: reducing search frictions can lead to wider bid-ask spreads

- Static effect: search frictions $\downarrow \Rightarrow$ intertemporal competition $\uparrow \Rightarrow$ spreads \downarrow (DGP)
- Dynamic effect: **search frictions $\downarrow \Rightarrow$ learning slows \Rightarrow spreads eventually \uparrow (GM)**

Additional contributions:

- New tradeoffs shed light on ambiguous empirical findings effects of reduced trading frictions
- Model useful for anticipating impact of regulations that reduce info or trading frictions

Market-making with asymmetric information

- “Small” informed traders, dealers learn from individual trades: Glosten-Milgrom(1985), ...
- “Large” informed trader, dealers learn from aggregate trade: Kyle(1985),...
- This paper: “small” informed traders, dealers learn from aggregate trade, search & market power

Market-making with search frictions

- Full info: Duffie, Garleanu & Pedersen(2005), Lagos & Rocheteau(2009)...
- Private info, private values: Spulber(1996), Lester, Rocheteau & Weill (2015)...
- This paper: private information about common values (adverse selection), learning

Decentralized trading with adverse selection

- Idiosyncratic: Inderst(2005), Guerrieri-Shimer-Wright(2010), Camargo & Lester(2014), Lauer mann & Wolinsky(2016), Kim (2017)...
- Aggregate: Wolinsky(1990), Blouin & Serrano(2001), Duffie, Malamud & Manso(2009), Golosov, Lorenzoni & Tsyvinski(2014)...
- This paper: Learning from market-wide activity, effect of info frictions on bid-ask spread

the economic environment

Agents and Assets

- Discrete time, infinite horizon
- A market for a **single** asset, quality (state of the world) is either l or h
- A continuum of **traders**
 - can hold $q \in \{0, 1\}$ units of the asset
 - measure N_q^e of new traders with q assets enter each period
 - all traders exit market with probability $1 - \delta$ in each period
 - traders have private info about asset quality + their own preferences
- A continuum of **dealers**
 - can hold unrestricted positions (long or short)
 - don't know asset quality, but learn from trading activity

Preferences

Given state of world $j \in \{l, h\}$,

- **trader** i who owns an asset receives:
 - flow payoff $\omega_t + \varepsilon_{i,t}$ per period
 - terminal payoff c_j upon exit, with $c_h > c_l$

with

- $\omega_t \sim F(\omega)$ = market-wide liquidity shock, mean zero, iid over time
- $\varepsilon_{i,t} \sim G(\varepsilon)$ = idiosyncratic liquidity shock, mean zero, iid over time
- For each unit he holds, **dealer** receives:
 - payoff v_j , with $v_h > v_l$
 - no liquidity shocks

Search, Prices, and Trade

Each period, trader meets stochastic number $n \in \{0, 1, 2\}$ of dealers

$$\text{Prob}(\text{meet } n \geq 1 \text{ dealer}) = \pi$$

Conditional on meeting at least one dealer,

- $\text{Prob}(\text{meet } n = 1 \text{ dealer}) = \alpha_m$ (“monopolist meeting”)
- $\text{Prob}(\text{meet } n = 2 \text{ dealer}) = \alpha_c$ (“competitive meeting”)

Dealers observe number of competing dealers but not asset quality/trader preferences

- offer to buy at bid price B_t^k , sell at ask price A_t^k for $k \in \{c, m\}$
- trader accepts or rejects.
- if she rejects, no trade occurs in that period.

Information and Learning

After trades occur in each period, dealers observe total trading volume

Two sources of uncertainty for dealers:

- ① asset quality: common value
- ② aggregate liquidity shock: private value

⇒ volume is a noisy signal about asset quality

Dealers are informationally small and all have common beliefs

- Beliefs summarized by $\mu_t \equiv \text{Prob}_t(j = h)$

► Interpretation via Interdealer Market

optimal behavior and equilibrium

Traders' Optimal Behavior

Let

- $W_{j,t}^q \equiv$ value of owning $q \in \{0, 1\}$ units of quality $j \in \{l, h\}$ asset at t
- $R_{j,t} = W_{j,t}^1 - W_{j,t}^0 \equiv$ reservation value at t when quality is $j \in \{l, h\}$

Given bid and ask prices (B_t^k, A_t^k) , $k \in \{m, c\}$, and shocks $(\varepsilon_{i,t}, \omega_t)$,

- Owner should sell if $\varepsilon_{i,t}$ sufficiently small, hold otherwise:

$$B_t^k + W_{j,t}^0 \geq \varepsilon_{i,t} + \omega_t + W_{j,t}^1$$

- Non-owner should buy if $\varepsilon_{i,t}$ sufficiently large, do nothing otherwise:

$$-A_t^k + \varepsilon_{i,t} + \omega_t + W_{j,t}^1 \geq W_{j,t}^0$$

Traders' Optimal Behavior

- Owner i sells in a k meeting iff

$$\epsilon_{i,t} \leq \underline{\epsilon}_{j,t}^k \equiv B_t^k - R_{j,t} - \omega_t$$

- Non-owner i buys in a k meeting iff

$$\epsilon_{i,t} \geq \bar{\epsilon}_{j,t}^k \equiv A_t^k - R_{j,t} - \omega_t$$

- Reservation values satisfy

$$R_{j,t} = (1 - \delta)c_j + \delta \mathbb{E}[R_{j,t+1}] + \delta \pi \mathbb{E} \left[\underbrace{\Omega_{j,t+1}}_{\text{Net option value}} \right]$$

where

$$\Omega_{j,t} = \sum_{k=c,m} \alpha^k \left[\underbrace{\max\{B_t^k - R_{j,t+1} - \omega_t - \epsilon_{i,t}, 0\}}_{\text{option to sell}} - \underbrace{\max\{-A_t^k + R_{j,t+1} + \omega_t + \epsilon_{i,t}, 0\}}_{\text{option to buy}} \right]$$

Aggregate Positions

$N_{j,t}^q$ = measure of traders holding $q \in \{0, 1\}$ units of asset when quality is $j \in \{l, h\}$

$$N_{j,t+1}^1 = \delta \left\{ N_t^1 \left[\underbrace{1 - \pi}_{\text{no meeting}} + \underbrace{\pi \left(1 - \sum_{k=c,m} \alpha^k G(\underline{\varepsilon}_{j,t}^k) \right)}_{\text{meeting, no sell}} \right] + N_t^0 \underbrace{\pi \left(1 - \sum_{k=c,m} \alpha^k G(\bar{\varepsilon}_{j,t}^k) \right)}_{\text{meet \& buy}} \right\} + N_1^e$$

$$N_{j,t+1}^0 = \delta \left\{ N_t^1 \pi \sum_{k=c,m} \alpha^k G(\underline{\varepsilon}_{j,t}^k) + N_t^0 \left[1 - \pi + \pi \sum_{k=c,m} \alpha^k G(\bar{\varepsilon}_{j,t}^k) \right] \right\} + N_0^e.$$

Dealers observe past volume and (know N_q^e)

\Rightarrow they know N_t^q when setting (B_t^k, A_t^k) .

Monopolist Dealer's Prices

Dealer with a captive customer chooses (A_t^m, B_t^m) to maximize

$$\mathbb{E}_{j,\omega} \left[\frac{N_t^0}{N_t^0 + N_t^1} (1 - G(\bar{\varepsilon}_{j,t}^m)) (A_t^m - v_j) + \frac{N_t^1}{N_t^0 + N_t^1} G(\underline{\varepsilon}_{j,t}^m) (v_j - B_t^m) \right]$$

Why? we find conditions s.t. no motive for experimentation, no benefit to waiting

- Pricing decision is static
- Sell (buy) choice unaffected by ask (bid) \Rightarrow separates the bid/ask problems
- Aggregate positions known \Rightarrow irrelevant for pricing, only beliefs μ_t matter

▶ No Experimentation

Key assumptions:

- Both traders and dealers are small, so take future beliefs as given
- Dealers can hold unrestricted positions, have deep pockets
- Support of shocks “large enough”

Under these conditions: market-wide info dominates learning from an individual meeting

Monopolist Dealer's Prices (given beliefs μ_t)

As a result, optimal monopoly prices satisfy:

$$A_t^m = \mathbb{E}_j v_j + \underbrace{\frac{1 - \mathbb{E}_{j,\omega} [G(\bar{\varepsilon}_{j,t}^m)]}{\mathbb{E}_{j,\omega} [g(\bar{\varepsilon}_{j,t}^m)]}}_{\text{market power}} + \underbrace{\mu_t(1 - \mu_t)(v_h - v_l) \frac{\mathbb{E}_\omega [g(\bar{\varepsilon}_{h,t}^m) - g(\bar{\varepsilon}_{l,t}^m)]}{\mathbb{E}_{j,\omega} [g(\bar{\varepsilon}_{j,t}^m)]}}_{\text{asymmetric information}}$$

$$B_t^m = \mathbb{E} v_j - \frac{\mathbb{E}_{j,\omega} [G(\underline{\varepsilon}_{j,t}^m)]}{\mathbb{E}_{j,\omega} [g(\underline{\varepsilon}_{j,t}^m)]} - \mu_t(1 - \mu_t)(v_h - v_l) \frac{\mathbb{E}_\omega [g(\underline{\varepsilon}_{l,t}^m) - g(\underline{\varepsilon}_{h,t}^m)]}{\mathbb{E}_{j,\omega} [g(\underline{\varepsilon}_{j,t}^m)]}.$$

Monopolist Dealer's Prices (given beliefs μ_t)

As a result, optimal monopoly prices satisfy:

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$$B_t^m = \mathbb{E}_j v_j - \frac{\mathbb{E}_{j,\omega} [G(\underline{\varepsilon}_{j,t}^m)]}{\mathbb{E}_{j,\omega} [g(\underline{\varepsilon}_{j,t}^m)]} - \text{Cov} \left(\frac{g(\underline{\varepsilon}_{j,t}^m)}{\mathbb{E}_{j,\omega} [g(\underline{\varepsilon}_{j,t}^m)]}, v_j \right)$$

Competitive Prices

Bertrand competition \Rightarrow zero profits (*a la* Glosten-Milgrom)

$$A_t^c = \frac{\mathbb{E}_{j,\omega} [v_j (1 - G(\bar{\varepsilon}_{j,t}^c))]}{\mathbb{E}_{j,\omega} [(1 - G(\bar{\varepsilon}_{j,t}^c))]}$$

$$B_t^c = \frac{\mathbb{E}_{j,\omega} [v_j G(\underline{\varepsilon}_{j,t}^c)]}{\mathbb{E}_{j,\omega} [G(\underline{\varepsilon}_{j,t}^c)]}$$

Competitive Prices

Bertrand competition \Rightarrow zero profits (*a la* Glosten-Milgrom)

$$A_t^c = \mathbb{E}_t v_j + \underbrace{\text{Cov} \left(\frac{1 - G(\bar{\varepsilon}_{j,t}^c)}{\mathbb{E}_{j,\omega} [1 - G(\bar{\varepsilon}_{j,t}^c)]}, v_j \right)}_{\text{asymmetric information}}$$

$$B_t^c = \mathbb{E}_t v_j - \underbrace{\text{Cov} \left(\frac{G(\underline{\varepsilon}_{j,t}^c)}{\mathbb{E}_{j,\omega} [G(\underline{\varepsilon}_{j,t}^c)]}, v_j \right)}_{\text{asymmetric information}}$$

Monopoly vs. Competitive (Ask) Prices

$$A_t^m = \mathbb{E}_j v_j + \underbrace{\frac{1 - \mathbb{E}_{j,\omega} [G(\bar{\varepsilon}_{j,t}^m)]}{\mathbb{E}_{j,\omega} [g(\bar{\varepsilon}_{j,t}^m)]}}_{\text{market power}} + \underbrace{\text{Cov} \left(\frac{g(\bar{\varepsilon}_{j,t}^m)}{\mathbb{E}_{j,\omega} [g(\bar{\varepsilon}_{j,t}^m)]}, v_j \right)}_{\text{asymmetric information}}$$

$$A_t^c = \mathbb{E}_t v_j + \underbrace{\text{Cov} \left(\frac{1 - G(\bar{\varepsilon}_{j,t}^c)}{\mathbb{E}_{j,\omega} [1 - G(\bar{\varepsilon}_{j,t}^c)]}, v_j \right)}_{\text{asymmetric information}}$$

Two key differences:

- 1 Competitive price has no markup/market power term.
- 2 PDF vs. CDF:
 - Monopolist's optimal price depends on mass of *marginal* investors
 - Competitive price requires equal profits *on average*

Evolution of Beliefs

Information: Dealers see volume at end of t (buys and sells), or equivalently

$$\underline{\epsilon}_t^k = B_t^k - R_t - \omega_t \quad \text{or} \quad \bar{\epsilon}_t^k = A_t^k - R_t - \omega_t$$

where $R_t = R_{j,t}$ if asset is of quality j

Since prices known, as if dealers see a signal $S_t = R_t + \omega_t \Rightarrow$ signal extraction problem

Updating: what would ω_t have to be in state $\iota \in \{l, h\}$ to generate S_t ?

$$\omega_{\iota,t}^* = S_t - R_{\iota,t}$$

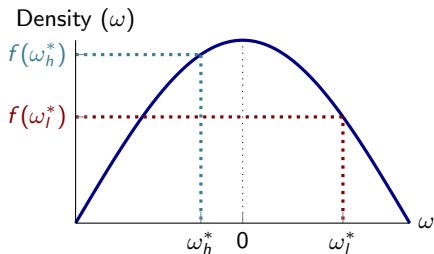
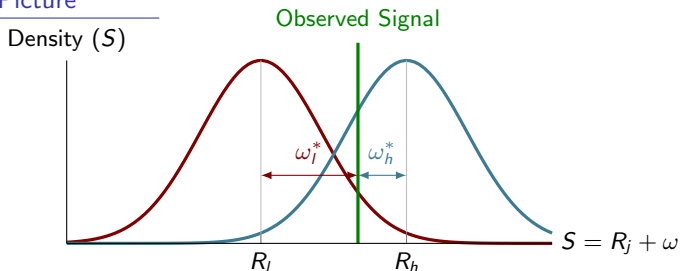
Beliefs then evolve according to

$$\mu' = \frac{\mu_t f(\omega_{h,t}^*)}{\mu_t f(\omega_{h,t}^*) + (1 - \mu_t) f(\omega_{l,t}^*)} = \frac{\mu_t}{\mu_t + (1 - \mu_t) \frac{f(\omega_t + R_{j,t+1}(\mu') - R_{l,t+1}(\mu'))}{f(\omega_t + R_{j,t+1}(\mu') - R_{h,t+1}(\mu'))}}$$

Learning process depends on $R_{h,t} - R_{l,t}$

- Trading typically more informative when the reservation values are very different

Learning: Picture



- Belief evolution depends on basic signal extraction
- Easy to see signal extraction problem more difficult if reservation values close together

Equilibrium

A recursive equilibrium is a collection of functions for

- 1 Reservation values: $R_j(\mu)$ $j \in \{h, l\}$
- 2 Thresholds: $\underline{\varepsilon}_j^k(\mu, \omega)$, $\bar{\varepsilon}_j^k(\mu, \omega)$ $k \in \{c, m\}$
- 3 Prices: $A^k(\mu)$, $B^k(\mu)$
- 4 Beliefs: $\mu'(\mu, \omega)$
- 5 Demographics: $N_j^0(\mu, \omega)$, $N_j^1(\mu, \omega)$

such that

- 1 Reservation values are consistent with future beliefs and prices
- 2 Given beliefs and prices, thresholds are optimal for traders
- 3 Given beliefs and thresholds, prices are optimal for dealers
- 4 Beliefs evolve according to Bayes' rule
- 5 Demographics evolve consistent with prices, thresholds

a tractable case

The Uniform-Uniform Model

Assumptions:

- ① $v_j = c_j$ for $j \in \{l, h\}$
- ② $\varepsilon_{i,t} \sim U(-e, e)$ and $\omega_t \sim U(-m, m)$
- ③ e and m are sufficiently large s.t. thresholds are always interior

Together, these assumptions simplify both learning and pricing.

Given beliefs and prices, can characterize (unique) equilibrium

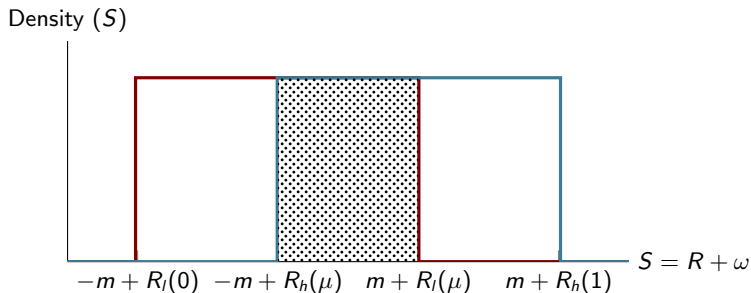
- Study relationship between search frictions, learning, and spreads...

Learning in the Uniform-Uniform Model

Recall: updating equation depends on

$$\frac{f(\omega_l^*)}{f(\omega_h^*)} = \frac{f(S - R_l)}{f(S - R_h)}$$

With bounded and uniform liquidity shocks, either j is revealed, or nothing is learned:



Learning in the Uniform-Uniform Model

Recall: updating equation depends on

$$\frac{f(\omega_l^*)}{f(\omega_h^*)} = \frac{f(S - R_l)}{f(S - R_h)}$$

Under uniform shocks, $f(\omega) = \frac{1}{2m}$ if $\omega \in [-m, m]$, zero otherwise

$$\mu'(\mu, S) = \begin{cases} 0 & \text{if } S \in \Sigma_l(\mu) \equiv [-m + R_l(0), -m + R_h(\mu)] \\ \mu & \text{if } S \in \Sigma_b(\mu) \equiv [-m + R_h(\mu), m + R_l(\mu)] \\ 1 & \text{if } S \in \Sigma_h(\mu) \equiv (m + R_l(\mu), m + R_h(1)]. \end{cases}$$

Then learning process summarized by $\mathbb{P}(\text{quality revealed})$:

$$p(\mu) = \frac{R_h(\mu) - R_l(\mu)}{2m}.$$

Result

Time to learn, $\frac{1}{p(\mu)}$ decreases as $(R_h - R_l) \uparrow$.

Pricing & Equilibrium in the Uniform-Uniform Model

Given simple learning process and linear demand/supply, prices easy to characterize.

Implied bid-ask spread σ given current beliefs $\mu \in (0, 1)$:

$$\sigma(\mu) = e - \alpha_c \sqrt{e^2 - 4 \text{Cov}(r_j, v_j)}$$

where

$$r_j = p(\mu)R_j(\mathbf{1}_{j=h}) + (1 - p(\mu))R_j(\mu).$$

Simple expression allows us to derive properties of spreads

Result (GM effect)

Spread is \cap -shaped in μ , maximized at $\mu = 1/2$.

Result (DGP effect)

Spread is decreasing in α_c .

Reservation Values and Search Frictions

How does a higher π affect spreads?

Crucial channel: effect of π on $R_h - R_l$:

$$R_h - R_l = (1 - \delta) (c_h - c_l) + \delta \mathbb{E}[R'_h - R'_l] + \delta \pi \mathbb{E}(\Omega'_h - \Omega'_l)$$

where Ω_j = option value of selling – option value of buying

Result

$R_h - R_l$ is decreasing in π .

- $\Omega'_h - \Omega'_l < 0$: Option to sell (buy) is worth less (more) when quality is high
- Higher π increases the weight of the net option value, bringing R_h and R_l closer
- Intuition: investors behave more alike in two states when more opportunities to trade
- \Rightarrow less adverse selection (given μ), but also *slower learning*

Result (Putting it all together)

- 1 *Spread big when uncertainty high ($\mu \approx 1/2$) (GM)*
- 2 $(R_h - R_l) \downarrow$ as $\pi \uparrow$
- 3 *Holding $\mu \in (0, 1)$ fixed, spread \downarrow as $\pi \uparrow$ (Static)*
- 4 *Learning occurs slower when $R_h - R_l$ is small (Dynamic)*

Therefore, two opposing effects on spread from decreasing search frictions ($\pi \uparrow$):

- **Static:** spread \downarrow as intertemporal competition \uparrow
- **Dynamic:** $(R_h - R_l) \downarrow \Rightarrow$ learning slows \Rightarrow more uncertainty \Rightarrow spread \uparrow

Search Frictions and Spreads

Numerical simulation: $j = h$, $\mu = 1/2$, $\pi \in \{0.25, .75\}$.

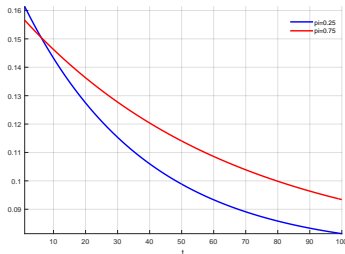


Figure: Average Spread Over Time

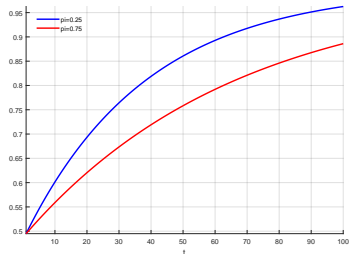


Figure: Average Beliefs Over Time

- $\pi \uparrow$ causes **static** fall in spread
- $\pi \uparrow$ causes slower learning, higher **“long-run”** spreads

Numerical Example

Generalized Version of Model

Relax previous assumptions on distributions, valuations:

- $\omega_t \sim N(0, \sigma_\omega^2)$ $\varepsilon_{i,t} \sim N(0, \sigma_\varepsilon^2)$
- $v_j = c_j + \xi$
- Additional, higher order terms complicate analysis

But, model easily solved computationally

- Guess $R_j(\mu)$ for $j = l, h$
- Given R_j , determine dealers' evolution of beliefs μ^+
- Given future beliefs and R_j , compute $A(\mu)$ and $B(\mu)$
- Update guess of R_j until convergence

Parameterization

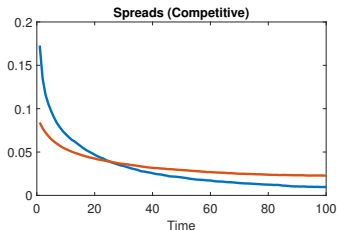
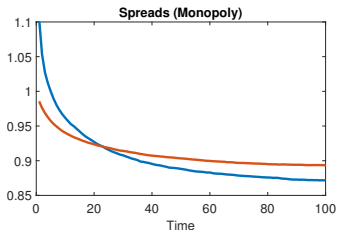
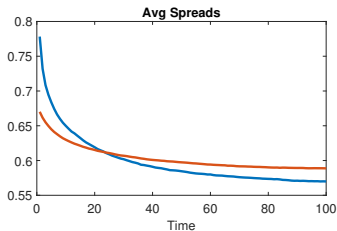
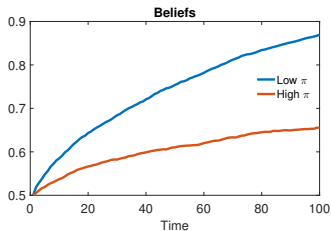
- Parameters approximate evidence from AAA-rated 5-year corporate bond evidence
- No gains to trade (on average) between dealers and traders ($\xi = 0$)
- Model period set to 1 week

Parameter	Value	Target	Source
$c_h - c_l$	\$1.16	Impact of Downgrade	Feldhutter (2012b)
μ_0	0.5	Probability of (AAA \rightarrow AA) Downgrade	S&P
$\sigma_\omega^2 = \sigma_\epsilon^2$	0.16	Avg. Gains to Trade	Feldhutter (2012a)
π	0.55	Match Rates given Poisson	Feldhutter (2012a)
α	0.35		
δ	0.9	sensitivity	

- $\delta = 0.9$ implies trading horizon (conditional on no trade) of 10 weeks

The Normal-Normal Model

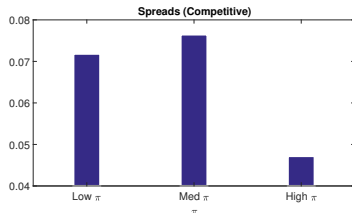
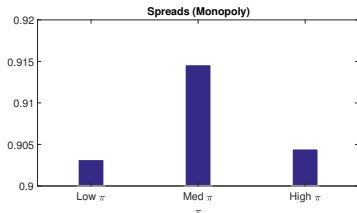
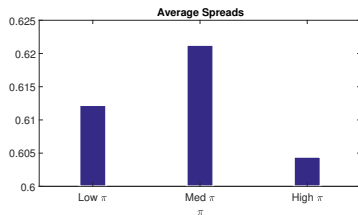
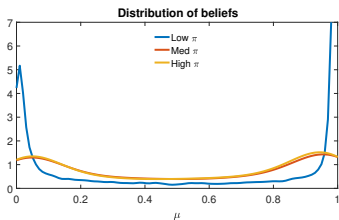
Effect of π (true state is $j = h$)



Higher $\pi \rightarrow$ Lower $(R_h - R_l) \rightarrow$ Less learning \rightarrow **Wider spreads eventually**

The Normal-Normal model: Stationary Version

- Asset quality j changes over time (with probability ρ)
- Other elements exactly the same as before
- \Rightarrow Non-trivial belief distribution in the long run (stochastic steady state)



Higher $\pi \rightarrow$ Lower $(R_h - R_l) \rightarrow$ Less learning \rightarrow Wider spreads

Search vs Info Frictions

Exercise: hit benchmark with shocks to π and $v_I \Rightarrow$ same Δ spread.

Question: are dynamic properties of spread *and* volume informative?

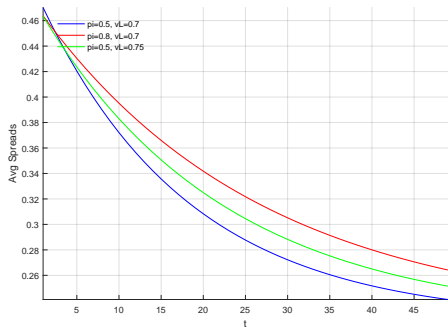


Figure: Spreads

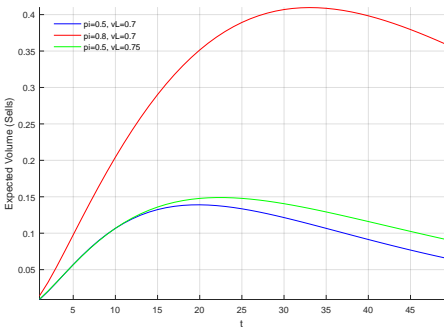


Figure: Volume

Conclusion

A dynamic model with two canonical frictions

- asymmetric information and infrequent trading opportunities/market power

Frictions interact in novel ways

- mitigating one could lead to wider spreads
- model helpful for understanding recent changes in OTC markets

Next steps

- Simulations suggest introduction of TRACE could widen spreads...
- disentangling the two frictions?....

Dealers

- Indexed by $i \in [0, 1]$
- They come into each period with $x_{i,t}$ units of the asset
- Payoff:

$$\sum_{s=t}^{\infty} (1 - \delta)^{s-t} [-d_{i,t} P_t + q_{i,t} p_t + \delta v_j(x_{i,t} + d_{i,t} + q_{i,t})]$$

where

$$d_{i,t} \in \{-1, 0, 1\}$$

$$P_t \in \{A_t, B_t\}$$

$$x_{i,t+1} = x_{i,t} + d_{i,t} + q_{i,t}$$

- p_t : price in the interdealer market; competitive

Dealers

- Conjecture that future bid and ask only a function of aggregate information and independent of individual positions.
- Radner: REE in the inter-dealer market $p_t = \mathbb{E}_t \left[v_j \mid \{d_{i,t}\}_{i \in [0,1]} \right]$.
- Dealers are small:

$$\mathbb{E}_t[v_j \mid p_t, d_{i,t}] = \mathbb{E}_t \left[v_j \mid \{d_{i,t}\}_{i \in [0,1]} \right]$$

- Act as if they are short-lived dealers and only care about $\mathbb{E}_t[v_j]$ where expectation is common across all dealers

Experimentation

- From individual trader, dealer can learn at most $R_j + \omega + \epsilon$
- From market volume, dealer will learn $R_j + \omega$
- Implies information in market volume dominates information that can be learned from a single trade
 - dominates in sense that dealer unwilling to pay any cost to learn $R_j + \omega + \epsilon$

Equilibrium

A recursive equilibrium is a set of functions: Start with a guess for Compute optimal prices: Update/verify the guess $R_j(\mu)$ $A(\mu)$ and $B(\mu)$ s.t. \rightarrow beliefs

$$\begin{aligned}R_j &= (1 - \delta) c_j + \delta \mathbb{E}[R_j(\mu'_j)] + \delta \pi \Omega_j(\mu) \\A &= \frac{\mathbb{E}v_j g(A - R_j(\mu'_j) - \omega) + 1 - \mathbb{E}G(A - R_j(\mu'_j) - \omega)}{\mathbb{E}g(A - R_j(\mu'_j) - \omega)} \\B &= \frac{\mathbb{E}v_j g(B - R_j(\mu'_j) - \omega) - \mathbb{E}G(B - R_j(\mu'_j) - \omega)}{\mathbb{E}g(B - R_j(\mu'_j) - \omega)}\end{aligned}$$

where

$$\mu'_j = \frac{\mu}{\mu + (1 - \mu) \mathcal{L}_j(\omega, R_h(\mu'_j) - R_l(\mu'_j))}$$

$$\Omega_j(\mu) = \mathbb{E} [\max(B(\mu) - R_j(\mu'_j) - \omega - \epsilon, 0) - \max(R_j(\mu'_j) + \omega + \epsilon - A(\mu), 0)]$$