

**Definition MunkTop.18.1:** If  $(X, T)$  and  $(Y, T')$  are topological spaces and  $f$  is in the set of maps from  $X$  to  $Y$  then  $f$  is *continuous* if and only if for every  $V \in T'$ , the range of the converse relation to  $f$  when restricted to  $V$  is in  $T$ .

**Definition MunkTop.18.2:** If  $(X, T)$  and  $(Y, T')$  are topological spaces and  $f$  is in the set of maps from  $X$  to  $Y$  and  $x \in X$  then  $f$  is *continuous* at  $x$  if and only if for every  $V$ , if  $V$  is a neighborhood of  $f(x)$  in  $(Y, T')$  then there exists  $U$  such that  $U$  is a neighborhood of  $x$  in  $(X, T)$  and the range of  $f$  when restricted to  $U$  is contained in  $V$ .

**Definition MunkTop.18.3:** If  $(X, T)$  and  $(Y, T')$  are topological spaces and  $f$  is a bijection from  $X$  to  $Y$  then  $f$  is a *homeomorphism* if and only if  $f$  and the converse relation to  $f$  are continuous.

**Definition MunkTop.18.3.5:** If  $(X, T)$  and  $(Y, T')$  are topological spaces then  $(X, T)$  is homeomorphic to  $(Y, T')$  if and only if there exists  $f$  such that  $f$  is a homeomorphism.

**Definition MunkTop.18.4:** If  $(X, T)$  and  $(Y, T')$  are topological spaces and  $f$  is an injection from  $X$  to  $Y$  and  $f$  is continuous then  $f$  is an *imbedding* if and only if  $f$  is a homeomorphism.