

## Homework 6 solutions:

1.

First compute moles of glucose consumed:  $26 \text{ g glucose} * (1 \text{ mol glucose}/180 \text{ g glucose}) = 0.14444 \text{ mol glucose}$  consumed with a standard deviation of  $.2 \text{ g} * (1 \text{ mol glucose}/180 \text{ g glucose}) = .0011 \text{ mole glucose}$

Now we note that the molecular weight of the yeast =  $144 \text{ g} = (6*12 + 10*1 + 1*14 + 3*16) \text{ g}$

$0.1444 \text{ mol glucose} * (0.48 \text{ mol dry cell/mol glucose}) * (144 \text{ g dry cell/mol dry cell}) = 9.95328 \text{ g dry cells}$  produced with a standard deviation of  $.0011 * (0.48 \text{ mol dry cell/mol glucose}) * (144 \text{ g dry cell/mol dry cell}) = .0768 \text{ g dry cells}$ .

Use yield coefficient to determine the amount of heat released into the fermenter.

$9.95328 \text{ g dry cells} * (1 \text{ kcal heat}/0.42 \text{ g dry cells}) = 23.6983 \text{ cal heat}$  with a standard deviation of  $.0768 \text{ g} * (1 \text{ kcal heat}/0.42 \text{ g dry cells}) = .182857 \text{ cal heat}$

Now determine the rise in temperature this leads to:

$(23.6983 \text{ kcal heat}/15 \text{ L broth}) * (1 \text{ degree C} * \text{L broth}/1 \text{ kcal heat}) = 1.58 \text{ degree Celsius}$  with a standard deviation of  $(.0768 \text{ kcal heat}/15 \text{ L broth}) * (1 \text{ degree C} * \text{L broth}/1 \text{ kcal heat}) = .005067 \text{ degrees Celsius}$

total answer:  $1.58 \pm .005067 \text{ degrees Celsius}$

Since half of the heat is released into the environment the final answer is  $1.58/2 \pm .005067/2$  which gives us  $.79 \pm .0025 \text{ degrees celsius}$

### 2. Energy Balances. MMD text chapter 4, problem 4.

$39 \text{ g glucose/can} * \text{mol glucose}/180 \text{ g} * 36 \text{ mol ATP/mole glucose} = 7.8 \text{ mol ATP/can}$ .

$7.8 \text{ mol ATP/can} * 30 \text{ g cell mass dw/mol ATP} * \text{g total}/0.3 \text{ g dw} = 780 \text{ g cells/can} \sim 0.8 \text{ kg tissue/can}$ .

### 3. Bioenergetics.

$\Delta G = RT \ln(C_1/C_2) + ZF\Delta\Psi$

34.5 nM on outside of cell

Efficiency = 59%

It takes 7.3 kcal/mol to convert ADP  $\rightarrow$  ATP

So  $0.59 = \Delta G / (7.3 \text{ kcal/mol})$  so  $\Delta G = 4.307 \text{ kcal/mol}$

So 4.307 kcal/per mol is available to overcome and unfavorable transfer of solute across the membrane (must be unfavorable if cell has to actively transport it across memberane)

$$F = 9.65 \times 10^{-4} \text{ C/mole}$$

$$Z = -1$$

$$\text{Assume } T = 37^\circ \text{C} = 310 \text{ K}$$

$$R = 0.001986 \text{ kcal / ( mol K)} = 1.986 \text{ cal/(mol)}$$

$$\Delta G = +4.301 \text{ kcal/mole} = RT \ln(C_1/35.5 \text{ nM}) + zF((-35 \text{ mV}) - (+75 \text{ mV}))$$

Therefore

$$4.301 - (zF((-35 \text{ mV}) - (+75 \text{ mV}))) = RT \ln(C_1/35.5 \text{ nM})$$

$$[4.301 - (zF((-35 \text{ mV}) - (+75 \text{ mV})))]/RT = \ln(C_1/35.5 \text{ nM})$$

$$e^{[4.301 - (zF((-35 \text{ mV}) - (+75 \text{ mV})))]/RT} = C_1/35.5 \text{ nM}$$

$$35.5 \text{ nM} * e^{[4.301 - (zF((-35 \text{ mV}) - (+75 \text{ mV})))]/RT} = C_1$$

$$C_1 = 1.2 * 10^{12} \text{ M}$$

4.

#### Bioenergetics

Inlet pressure = 7 mmHg

Inlet diameter = 6.0 mm

Outlet pressure = 82 mmHg

Outlet diameter = 4.5 mm

a)  $\dot{V}$  is same for the inlet and outlet, and we know that  $\dot{V} = V \cdot A$  where  $V$  is linear velocity,  $A$  is cross sectional area. Thus,

For the inlet:

$$(3.2 \text{ L/min}) * (1000 \text{ cm}^3/\text{L}) * (1 / (\pi * (.3)^2 \text{ cm}^2)) * (1 \text{ min}/60 \text{ sec}) = 188.628 \text{ cm/sec.}$$

Two significant figures: 190 cm/sec

For the outlet:

$$(3.2 \text{ L/min}) * (1000 \text{ cm}^3/\text{L}) * (1 / (\pi * (.225)^2 \text{ cm}^2)) * (1 \text{ min}/60 \text{ sec}) = 335.338 \text{ cm/sec.}$$

Two significant figures: 340 cm/sec

b) Work is the only energy involved; kinetic and potential energies are negligible. We consider the equilibrium state, where  $d(\text{Energy})/dt = 0$ , so work  $w=0$ .

The work being done is  $F \cdot v$ , where the force in this case is pressure, and velocity is the volumetric flow rate. Total  $w = w(\text{done by pump}) + w(\text{flow})$ .

$$\text{So } w(\text{pump}) = w(\text{flow}) = (3.2 \text{ L/min})(7 \text{ mmHg} - 82 \text{ mmHg})$$

Unit conversion:

$$(3.2 \text{ L/min}) * (7 \text{ mmHg} - 82 \text{ mmHg}) * (1 \text{ min}/60 \text{ sec}) * (1 \text{ m}^3/1000 \text{ L}) * (10^5 \text{ Pa}/750.061 \text{ mmHg}) * (1 \text{ W}/(1 \text{ m}^3 \text{ Pa/sec})) = 0.5333 \text{ W, or } 0.53 \text{ watts to two sig. figures.}$$

c) We know that Watt = Amp \* Volt. So we can solve:

$$.53 \text{ W} * 5 \text{ days} * 24 \text{ hours/day} = 63.6 \text{ W hr}$$
$$63.6 / .38 = 167.368 \text{ W hr}$$

$$(167.368 \text{ W hr}) / (6 \text{ V}) * (1 \text{ A} / (\text{W/V})) * (1000 \text{ mA} / \text{A}) = 27894 \text{ mA hr}$$

With two significant figures, this works out to 28000 mA hr.

d) For this problem we use the solution in part c that has not been adjusted to account for significant figures.

So from before we know that 27894 mA hr leads to 120 hours (5 days) of operation

$$27894 * .007 = 195 \text{ mA hr}$$

Note that there is no error introduced from converting current capacity to operation time, so we can easily find the error in time.

$$(195 \text{ mA hr}) * (1 \text{ A} / 1000 \text{ mA}) * (1 \text{ W} / (\text{V mA})) * (6 \text{ V} / (.53 \text{ W})) * (1 \text{ day} / 24 \text{ hours}) = .035 \text{ days}$$

Note that this is the same as:  $5 \text{ days} * .007 = .035 \text{ days}$

Now we use the Z test. To test with 99.9999% confidence, we use a Z-value of 4.67.

$$(5 \pm x) / .035 = 4.67$$
$$\text{So } x = 5 - 0.16345 = 4.83655 \text{ days} * (24 \text{ hours} / \text{day}) = 116.07 \text{ hr.}$$

When converting to 2 significant figures, we do not round up. Rather, we need to this **down** to 2 significant figures since we want to have a certainty of at least 99.9999%. Thus, the final answer is 110 hr.

5.

**Binding.** MMD text chapter 5, problem 1.

- (a) P-L1 will be more prevalent because the protein binds it preferentially over L2.
- (b) Because binding is dynamic, a given protein molecule will bind different L1's and L2's.
- (c) This is akin to competitive inhibition. L2 still binds, so adding more will "distract" the protein from binding L1. Therefore, it will decrease, not increase the amount of P-L1 present.

6.

**Binding**

S4 binds to the first enzyme's binding site, which is enzyme inhibition. Thus S1 cannot bind with as much of the enzyme, which slows down the whole chain of reaction. Concentrations of S2, S3, S4 will drop. This is therefore an example of negative feedback.