

### 1. Isomorphisms

Show that there are eleven nonisomorphic simple graphs on four vertices.

**Solution:**

### 2. Euler's Formula

A soccer ball is a convex polyhedron whose faces are either hexagons or pentagons. Prove that a soccer ball has exactly 12 pentagonal faces.

**Solution:**

### 3. Graph Induction

A tournament of  $n$  vertices is a complete directed graph with  $n$  vertices. Prove that there always exists a directed path that visits each vertex in the tournament exactly once.

**Solution:**