

# UNIT 6A Organizing Data: Lists

15110 Principles of Computing, Carnegie Mellon University

#### Data Structure

- The organization of data is a very important issue for computation.
- A **data structure** is a way of storing data in a computer so that it can be used efficiently.
  - Choosing the right data structure will allow us to develop certain algorithms for that data that are more efficient.
  - An array (or list) is a very simple data structure for holding a sequence of data.

#### 15110 Principles of Computing, Carnegie Mellon University - CORTINA

# Arrays in Memory

- Typically, array elements are stored in adjacent memory cells. The subscript (or index) is used to calculate an offset to find the desired element.
- Example: data = [50, 42, 85, 71, 99]
   Assume integers are stored using 4 bytes (32 bits).
- If we want data[3], the computer takes the address of the start of the array and adds the offset \* the size of an array element to find the element we want.
- Do you see why the first index of an array is 0 now?

Address	Contents
100	50
104	42
108	85
112	71
116	99

Location of data[3] is 100 + 3\*4 = 112

### Arrays: Pros and Cons

- Pros:
  - Access to an array element is fast since we can compute its location quickly.
- Cons:
  - If we want to insert or delete an element, we have to shift subsequent elements which slows our computation down.
  - We need a large enough block of memory to hold our array.

# Linked Lists

- Another data structure that stores a sequence of data values is the **linked list**.
- Data values in a linked list do not have to be stored in adjacent memory cells.
- To accommodate this feature, each data value has an additional "pointer" that indicates where the next data value is in computer memory.
- In order to use the linked list, we only need to know where the first data value is stored.

#### Linked List Example

• Linked list to store the sequence: 50, 42, 85, 71, 99

Assume each integer and pointer requires 4 bytes.

Starting Location of List (head) 124

address	data	next
100	42	148
108	99	0 (null)
116		
124	50	100
132	71	108
140		
148	85	132
156		

# Linked List Example

 To insert a new element, we only need to change a few pointers.

 Example: Insert 20 after 42.

> Starting Location of List (head) 124

address	data	next
100	42	156
108	99	0 (null)
116		
124	50	100
132	71	108
140		
148	85	132
156	20	148

# Drawing Linked Lists Abstractly

L = [50, 42, 85, 71, 99]



• Inserting 20 after 42:



15110 Principles of Computing, Carnegie Mellon University - CORTINA

# Linked Lists: Pros and Cons

- Pros:
  - Inserting and deleting data does not require us to move/shift subsequent data elements.
- Cons:
  - If we want to access a specific element, we need to traverse the list from the head of the list to find it which can take longer than an array access.
  - Linked lists require more memory. (Why?)

### Two-dimensional arrays

- Some data can be organized efficiently in a table (also called a matrix or 2-dimensional array)
- Each cell is denoted with two subscripts, a row and column indicator

two subscripts,	В	0	1	2	3	4
<i>i</i> and column	0	3	18	43	49	65
ator	1	14	30	32	53	75
	2	9	28	381	50	73
B[2][3] = 50	3	10	24	37	58	62
	4	7	19	40	46	66

#### 2D Arrays in Ruby

- data[0] => [1, 2, 3, 4]
- data[1][2] => 7
- data[2][5] => nil
- data[4][2] => undefined method '[]' for nil

### 2D Array Example in Ruby

 Find the sum of all elements in a 2D array def sumMatrix(table) number of rows in the table sum = 0for row in 0..table.length-1 do for col in 0..table[row].length-1 do sum = sum + table[row][col] end number of columns in the end given row of the table return sum end

#### Tracing the Nested Loop



15110 Principles of Computing, Carnegie Mellon University - CORTINA

# Stacks

- A **stack** is a data structure that works on the principle of Last In First Out (LIFO).
  - LIFO: The last item put on the stack is the first item that can be taken off.
- Common stack operations:
  - Push put a new element on to the top of the stack
  - Pop remove the top element from the top of the stack
- Applications: calculators, compilers, programming





# RPN

- Some modern calculators use Reverse Polish Notation (RPN)
  - Developed in 1920 by
     Jan Lukasiewicz
  - Computation of mathematical formulas can be done without using any parentheses
  - Example:
    (3+4)\*5 =
    becomes in RPN:
    34+5\*



#### **RPN Example**

# Convert the following standard mathematical expression into RPN:



# **Evaluating RPN with a Stack**



#### Example Step by Step

• RPN: 23 3 - 4 6 + /

• Stack Trace:



#### Stacks in Ruby

• You can treat arrays (lists) as stacks in Ruby.

	stack	x
<pre>stack = []</pre>	[]	
<pre>stack.push(1)</pre>	[1]	
stack.push(2)	[1,2]	
stack.push(3)	[1,2,3]	
x = stack.pop()	[1,2]	3
x = stack.pop()	[1]	2
x = stack.pop()	[]	1
x = stack.pop()	nil	nil

#### Queues

- A **queue** is a data structure that works on the principle of First In First Out (FIFO).
  - FIFO: The first item stored in the queue is the first item that can be taken out.
- Common queue operations:
  - Enqueue put a new element in to the rear of the queue
  - Dequeue remove the first element from the front of the queue
- Applications: printers, simulations, networks











# UNIT 6B Organizing Data: Hash Tables

# **Comparing Algorithms**

- You are a professor and you want to find an exam in a large pile of n exams.
- Search the pile using linear search.
  - Per student: O(n)
  - Total for n students:  $O(n^2)$
- Have an assistant sort the exams first by last name.
  - Assistant's work: O(n log n) using merge sort
  - Professor:
    - Search for one student: O(log n) using binary search
    - Total for n students: O(n log n)

# Another way

- Set up a large number of "buckets".
- Place each exam into a bucket based on some function.
  - Example: 100 buckets, each labeled with a value from 00 to 99. Use the student's last two digits of their student ID number to choose the bucket.
- Ideally, if the exams get distributed evenly, there will be only a few exams per bucket.
  - Assistant: O(n) putting n exams into the buckets
  - Professor: O(1) search for an exam by going directly to the relevant bucket and searching through a few exams.

#### Strings and ASCII codes

```
s = "hello"
for i in 0..s.length-1 do
    print s[i], "\n"
end
```

104	You can treat a string like an array
101	in Ruby.
108	If you access the ith character,
108	you get the ASCII code for that
111	

#### Hash table

 Let's assume that we are going to store only lower case strings into an array (hash table).

table1 = Array.new(26)

### Hash table

 We could pick the array position where each string is stored based on the first letter of the string using this hash function:

```
def h(string)
   return string[0] - 97
end
```

```
The ASCII values of lowercase letters are:
"a" -> 97, "b" -> 98, "c" -> 99, "d" -> 100, etc.
```

# Inserting into Hash Table

 To insert into the hash table, we simply use the hash function h to determine which index ("bucket") to store the element.

```
def insert(table, name)
   table[h(name)] = name
end
```

```
insert(table1, "aardvark")
insert(table1, "beaver") ...
```

# Hash function (cont'd)

- Using the hash function h:
  - "aardvark" would be stored in an array at index 0
  - "beaver" would be stored in an array at index 1
  - "kangaroo" would be stored in an array at index 10
  - "whale" would be stored in an array at index 22

#### table1

# Hash function (cont'd)

- But if we try to insert "bunny" and "bear" into the hash table, each word overwrites the previous word since they all hash to index 1:
- >> insert(table1,"bunny")
- >> insert(table1, "bear")
- >> table1

#### **Revised Hash table**

- Let's make our hash table an array of arrays (an array of "buckets")
- Each bucket can hold more than one string.

```
table2 = Array.new(26)
```

```
for i in 0..25 do
```

```
table2[i] = []
```

#### end

#### **Revised insert function**

def insert(table, key)

# find the bucket (array) in the table
# array using the hash function h
bucket = table[h(key)]
# append the key string to the bucket
# array
bucket << key</pre>

end

#### Inserting into new hash table

insert(table2, "aardvark")

- >> insert(table2, "beaver")
- >> insert(table2, "kangaroo")
- >> insert(table2, "whale")
- >> insert(table2, "bunny")
- >> insert(table2, "bear")
- >> table2

# Collisions

- "beaver", "bunny" and "bear" all end up in the same bucket.
- These are collisions in a hash table.
- The more collisions you have in a bucket, the more you have to search in the bucket to find the desired element.
- We want to try to minimize the collisions by creating a hash function that distribute the keys (strings) into different buckets as evenly as possible.

# First Try

```
def h(string)
```

```
k = 0
for i in 0..string.length-1 do
    k = string[i] + k
    end
    return k
end
h("hello") => 532
h("olleh") => 532
```

Permutations still give same index (collision) and numbers are high.

# Second Try

```
def h(string)
  \mathbf{k} = \mathbf{0}
  for i in 0..string.length-1 do
    k = string[i] + k*256
  end
  return k
end
h("hello") => 448378203247
h("olleh") => 478560413032
```

Better, but numbers are still high. We probably don't want to (or can't) create arrays that have indices this large.

# Third Try

def h(string, tablesize)

```
k = 0
for i in 0..string.length-1 do
    k = string[i] + k*256
end
return k % tablesize
```

end

We can use the modulo operator to take the large values and map them to indices for a smaller array.

#### **Revised insert function**

def insert(table, key)

# find the bucket (array) in the table
# array using the hash function h
bucket = table[h(key, table.length)]
# append the key string to the bucket
# array
bucket << key</pre>

end

#### Final results

```
table3 = Array.new(13)
for i in 0..12 do table3[i] = [] end
[]]
>> insert(table3,"aardvark")
                                Still have one
>> insert(table3, "bear")
                                collision, but
>> insert(table3, "bunny")
                                b-words are
                                distributed better.
>> insert(table3, "beaver")
>> insert(table3,"dog")
>> table3
```

```
["aardvark", "bear"], ["dog"], ["beaver"]]
```

# Searching in a hash table

To search for a key, use the hash function to find out which bucket it should be in, if it is in the table at all.

def contains?(table, key)
 bucket = table[h(key,table.length)]
 for entry in bucket do
 return true if entry == key
 end
 return false

end

# Efficiency

- If the keys (strings) are distributed well throughout the table, then each bucket will only have a few keys and the search should take O(1) time.
- Example:

If we have a table of size 1000 and we hash 4000 keys into the table and each bucket has approximately the same number of keys (approx. 4), then a search will only require us to look at approx. 4 keys => O(1)

 But, the distribution of keys is dependent on the keys and the hash function we use!