

**Chem Engr. 06-607 Physical Chemistry of Colloids and Surfaces**

**Homework #7**

**4-9-02**

**Due: 4-18-02, beginning of class.**

1. Calculate the stability ratio for a monodisperse population of particles ( $R=100$  nm) in water ( $T=298\text{K}$ ) whose pair interaction potential in water is given by:

$$\frac{V(r)}{kT} = B \exp[-k(r - 2R^*)]$$

where  $k=0.18 \text{ nm}^{-1}$ ,  $r$  is the center-to-center distance between particles,  $k$  is the Boltzmann constant,  $T$  is the absolute temperature,  $B$  is a constant that depends on the particle's charge ( $B=40$ ), and  $R^*$  is some characteristic length that can be approximated by the particle radius. *You will need to use numerical integration for this.*

2. Problem 8.4, Evans.

3. If coagulation involves two spheres of different radius  $R_i$  and  $R_j$ , show that the expression for the flocculation rate constant ( $k_r$ ):

$$k_r = \frac{2kT}{3\mathbf{m}} (R_i + R_j) \left( \frac{1}{R_i} + \frac{1}{R_j} \right)$$

can be reduced to :

$$k_r = \frac{2kT}{3\mathbf{m}} \left[ 4 + \left( \sqrt{\frac{R_i}{R_j}} - \sqrt{\frac{R_j}{R_i}} \right)^2 \right]$$

Ottewill and Wilkins (*Trans. Faraday Soc.* 58:608, 1962) observed a  $k_r$  of  $2.9 \times 10^{-11} \text{ cm}^3/\text{s}$ . What ratio of two radii would account for this rate constant (use  $0.01 \text{ g/cm-s}$  for the viscosity of water,  $T=298 \text{ K}$ )?

4. The critical coagulation concentration (CCC) was measured for a  $\text{Fe}(\text{OH})_3$  sol in water ( $T=298\text{ K}$ ) using a series of electrolytes. The results were:

Electrolyte	CCC (mM)
NaCl	9.25
KBr	12.2
$\text{BaCl}_2$	4.8
$\text{K}_2\text{SO}_4$	0.20
$\text{MgSO}_4$	0.22

- Is the sol positively or negatively charged?
- Is the surface charge density relatively high or low?
- Estimate the surface potential.